## Geometry Formulas

### 3.1. Right Triangle



Area of a right triangle $=\frac{1}{2}$ bh
Perimeter of a right triangle $=a+b+c$
Pythagoras Theorem $=$ Hypotenuse $^{2}=$ Perpendicular $^{2}+$ base $^{2}$
Where, $b$ is the base of a triangle
$h$ is the height of the triangle

### 3.2. Isosceles Triangle



Area of Isosceles Triangle Formula $=\frac{1}{2}$ bh

Altitude of an Isosceles Triangle $=\sqrt{a^{2}-\frac{b^{2}}{4}}$

### 3.3. Equilateral Triangle



Area of an Equilateral Triangle $=\frac{\sqrt{3}}{4} a^{2}$
Perimeter of an Equilateral Triangle=3a
Semi Perimeter of an Equilateral Triangle =3a / 2
Height of an Equilateral Triangle $=\frac{\sqrt{3}}{2} a$

### 3.4. Scalene Triangle

Area of Triangle $=1 / 2 \mathbf{x} \mathbf{b x h}$
When all the sides are given, $A=\sqrt{s(s-a)(s-b)(s-c)}$
Where $s=(a+b+c) / 2$


## Area $=\mathbf{a} \times \mathbf{a}$

Area of a Square $=\mathrm{a}^{2}$
Perimeter of a Square $(p)=4 a$
3.6. Rectangle


Rectangle
Area of a Rectangle, $A=1 \times b$
Perimeter of a Rectangle, $\mathrm{P}=2(\mathrm{I}+\mathrm{b})$
Diagonal of a Rectangle, $\mathrm{D}=\sqrt{l^{2}+b^{2}}$

### 3.7. Parallelogram



Area $=b \times h$
Perimeter of a Parallelogram=2(Base+Height)
Height of a Parallelogram, Height=Area/Base
Diagonal of Parallelogram $=p^{2}+q^{2}=2\left(a^{2}+b^{2}\right)$

### 3.8. Rhombus



Area of a Rhombus $=\frac{d_{1} d_{2}}{2}$
$d_{1}$ is the length of a diagonal
$\mathbf{d}_{\mathbf{2}}$ is the length of the other diagonal

Perimeter of a rhombus $=4 \times a$
Where,
$a$ is the side.
Area $=4 \times 1 / 2(a b)$

Where,
$b$ is the length of the base
$a$ is the altitude (height).
Area $=\operatorname{Sin}^{2} \sin x$
$s$ is the length of any side
$\mathbf{x}$ is an interior angle
sin is the sine function

### 3.9. Trapezoid



Area of a Trapezoid $=\frac{a+b}{2} h$
Perimeter of a Trapezoid, $\mathrm{P}=\mathrm{a}+\mathrm{b}+\mathrm{c}+\mathrm{d}$

## Perimeter of a Trapezoid

$\mathrm{h}=$ height (Note - This is the perpendicular height, not the length of the legs.)
a = the short base
b = the long base
Height (altitude) $=2 a /\left(b_{1}+b_{2}\right)$
Base length $=(2 a / h)-b$
Centroid of a Trapezoid, $x=\frac{b+2 a}{3(a+b)} h$

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3.10. Isosceles Trapezoid


Area of Isosceles Trapezoid $=\frac{a+b}{2} h$
Perimeter of Isosceles Trapezoid $=a+b+2 c$
3.13. Kite


Area of a Kite $=(1 / 2) \times$ Diagonal
Perimeter of a Kite= $2 a+2 b W h e r e$,
$a=$ The length of First pair
$b=$ The length of second pair

### 3.14. Cyclic Quadrilateral

Cyclic Quadrilateral $=\sqrt{(s-a)(s-b)(s-c)(s-d)}$
Where $s$ is called the semi-perimeter,
$\mathrm{s}=(\mathrm{a}+\mathrm{b}+\mathrm{c}+\mathrm{d}) / 2$

### 3.15. Tangential Quadrilateral



Area $=\sqrt{a b c d}$ (or)
$A=r s$
Where,
$r=$ radius of inscribed circle
$s=$ semi-perimeter $=(a+b+c+d)$

### 3.16. General Quadrilateral

Area of a Square $=(\text { side })^{2}$
Area of a Kite $=(1 / 2) \times$ Diagonal
Area of a Parallelogram $=$ Base $\times$ Height
Area of a Rectangle $=$ Base $\times$ Height
Area of a Trapezoid $=\frac{\text { base } 1+\text { base } 2}{2} \mathrm{~h}$

### 3.17. Regular Hexagon



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Area of hexagon $=\frac{3 \sqrt{3}}{2} a^{2}$
Where $a$ is the length of each side of the hexagon

### 3.18. Regular Polygon



The formula for area of a regular polygon is given as,
$\mathrm{A}=\frac{l^{2} n}{4 \tan \frac{\pi}{n}}$
Where,
I is the side length
n is the number of sides

### 3.19. Circle



Area of a Circle $=\pi r^{2}$
Circumference of a circle $=2 \pi r$
Where, $r$ is the radius of the circle.
$d$ is the diameter of the circle.
C is the circumference of the circle.

### 3.20. Sector of a Circle



Area of sector $=\frac{\theta}{360^{0}} \pi r^{2}$
Length of an arc of a sector $=\frac{\theta}{360^{0}} 2 \pi r$
Where, $r$ is the circle radius

### 3.21. Segment of a Circle



Area of a Segment in Radians $=A=\frac{1}{2} r^{2}(\theta-\sin \theta)$
Area of a Segment in Degrees $=A=\frac{1}{2} r^{2}\left(\frac{\pi}{180} \theta-\sin \theta\right)$
Where, $r$ is the radius of a circle

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3.22. Cube


$$
\begin{aligned}
& \text { x = Length of the sides } \\
& \mathrm{D}=\text { Diagonals }
\end{aligned}
$$

Surface area of Cube $=6 x^{2}$
Volume of a cube $=x^{3}$
Diagonal of a Cube $=\sqrt{3} x$
Where, $x$ is the side length of the cube.

The Cube Formula for any value ' $x$ ' is given as, $x^{3}=x \times x \times x$

### 3.23. Rectangular Parallelepiped

Surface area $=2 a b+2 b c+2 a c$
Volume = abc
Diagonal $=\sqrt{a^{2}+b^{2}}$
3.24. Prism

## Rectangular Prism



Surface Area of a Rectangular Prism = 2(bl+|h+hb)
Volume of a Rectangular Prism=lbh
Base Area of a Rectangular Prism =bl

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Where,
$b$ - base length of the rectangular prism.
I- base width of the rectangular prism.
$h$ - height of the rectangular prism.

## Triangular Prism



Surface Area of a triangular Prism= $a b+3 b h$
Volume of triangular prism $=\frac{1}{2} \mathrm{abh}$
Base area of a Triangular Prism =12ab
Where,
a - apothem length of the prism.
b-base length of the prism.
I- base width of the rectangular prism.
$h$ - height of the prism.

## Pentagonal Prism



Surface Area of a pentagonal Prism $=5 a b+5 b h$
Volume of a Pentagonal Prism $=\frac{5}{2}$ abh
Base Area of Pentagonal Prism $=\frac{5}{2} a b$
Where,
a - apothem length of the pentagonal prism.
$b$ - base length of the pentagonal prism.
$h$ - height of the pentagonal prism.

## Hexagonal Prism



Surface Area of a hexagonal Prism = 6ab +6bh
Volume of a HexagonalPrism=3abh
Base area of hexagonal prism=3a
Where,
a - apothem length of the hexagonal prism.
$b$ - base length of the hexagonal prism.
h - height of the hexagonal prism.
3.25. Regular Tetrahedron

Area of One Face of Regular Tetrahedron, $A=\frac{1}{4} \sqrt{3} a^{2}$
Total Surface Area of Regular Tetrahedron $A=\sqrt{3} a^{2}$
Slant Height of a Regular Tetrahedron $=a \frac{\sqrt{3}}{2}$
Altitude of a Regular Tetrahedron, $h=\frac{a \sqrt{6}}{3}$
Volume of a Regular Tetrahedron, $v=\frac{a^{3} \sqrt{2}}{12}$
3.26. Regular Pyramid


Surface Area of a Pyramid=Base Area $+\frac{1}{2}$ (Number of Base Sides $\times$ Slant Height $\times$ Base Length)
Volume of a Pyramid $=\frac{1}{2} \times$ Base Area $\times$ Height

## Square Pyramid



Surface Area of a Square Pyramid=2bs+b2
Volume of a Square Pyramid $=\frac{1}{3} b^{2} h$
Base Area of a Square Pyramid $=b^{2}$
Where,
b - base length of the square pyramid.
$s$ - slant height of the square pyramid.
$h$ - height of the square pyramid.

## Triangular Pyramid



Surface Area of a Triangular Pyramid $=\frac{1}{2} \mathrm{ab}+\frac{3}{2} \mathrm{bs}$
Volume of a Triangular Pyramid $=\frac{1}{6}$ abh

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Base Area of a Triangular Pyramid $=\frac{1}{2} \mathrm{ab}$
Where,
a - apothem length of the triangular pyramid.
$b$ - base length of the triangular pyramid.
$s$ - slant height of the triangular pyramid.
h - height of the triangular pyramid

## Pentagonal Pyramid



Surface Area of a Pentagonal Pyramid $=\frac{5}{2} \mathrm{ab}+\frac{5}{2} \mathrm{bs}$
Volume of a Pentagonal Pyramid $=\frac{5}{6}$ abh
Base Area of a Pentagonal Pyramid $=\frac{5}{2} a b$
Where,
a - apothem length of the pentagonal pyramid.
$b$ - base length of the pentagonal pyramid.
$s-$ slant height of the pentagonal pyramid.
h - height of the pentagonal pyramid.

## Hexagonal Pyramid



Surface Area of a Hexagonal Pyramid=3ab+3bs
Volume of a Hexagonal Pyramid=abh
Base Area of a Hexagonal Pyramid=3ab
Where,
a - Apothem length of the hexagonal pyramid.
$b$ - Base length of the hexagonal pyramid.
s - Slant height of the hexagonal pyramid.
$h$ - Height of the hexagonal pyramid.

### 3.27. Frustum of a Regular Pyramid

Volume of Frustum of a Regular Pyramid, $\mathrm{V}=\frac{h\left(B_{1}+B_{2}+\sqrt{\left.B_{1} B_{2}\right)}\right.}{3}$
Lateral Surface of Frustum of a Regular Pyramid, $\mathrm{S}=\frac{s\left(P_{1}+P_{2}\right)}{2}$
Where,
$\mathrm{s}=$ Slant height
$P_{1}$ and $P_{2}=$ Perimeter of Bases
$\mathrm{h}=$ Height
$\mathrm{B}_{1}$ and $\mathrm{B}_{2}=$ Base Areas

### 3.28. Platonic Solids

## Tetrahedron



Surface Area $=\sqrt{3} a^{3}$
Volume $=\frac{\sqrt{2}}{12} a^{3}$

## Cube



Surface Area $=4 a^{2}$
Volume $=a^{3}$
Diagonal $=\sqrt{3} a$

## Octahedron



Surface Area $=2 \sqrt{3} a^{2}$
Volume $=\frac{\sqrt{2}}{3} a^{3}$
Dodecahedron


Surface Area $=30 \times a \times a p$
Volume $=\frac{1}{4}(15+7 \sqrt{5}) a^{3}$

## Icosahedron



Surface Area $=5 \sqrt{3} a^{2}$
Volume $=\frac{5}{12}\left(3+\sqrt{5} a^{3}\right)$
3.33. Frustum of a Right Circular Cone

$A=\pi\left(R_{1}+R_{2}\right) s$
$V=\frac{\pi h}{3}\left(R^{2}+R r+r^{2}\right)$
3.34. Sphere


Surface Area of a Sphere $=4 \pi r^{2}$
Volume of a sphere $=\frac{4}{3} \pi^{3}$
Where, $r$ is the radius of the sphere

### 3.35. Spherical Cap



The volume of the spherical cap with base radius, $\mathrm{V}=\frac{\pi}{3} \mathrm{H}^{2}\left(3 \mathrm{R}^{2}=\mathrm{H}^{2}\right)$
Where,
$\mathrm{H}=$ height
$\mathrm{S}=$ sphere radius
A = base radius
$R=$ sphere radius

### 3.36. Spherical Sector

Surface Area of the spherical sector, $A=\pi r(2 h+a)$
Volume of the Spherical Sector, $V=\frac{2 \pi r^{2} h}{3}$

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3.37. Spherical Segment


Surface Area of the spherical segment, $A=2 \pi R h$
Volume of the Spherical segment, $\mathrm{V}=\frac{\pi h}{6}\left(3 r_{1}^{2}+3 r_{2}^{2}+h^{2}\right)$
3.38. Spherical Wedge

Surface Area $=2 R^{2} \theta$
Volume $={ }_{-}^{2} \mathrm{R}^{3} \theta$
Arc Length at the equator $=\mathrm{R} \theta$
3.39. Ellipsoid


Volume of an Ellipsoid, $\mathrm{V}=\frac{4}{3} \pi \mathrm{rabc}$ (or)
$V=\frac{4}{3} \pi r_{1} r_{2} r_{3}$
Where,
r1= radius of the ellipsoid 1
r2= radius of the ellipsoid 2
r3= radius of the ellipsoid 3

