

DESIGN OF QUESTION PAPER

MATHEMATICS

CLASS XII

Time : 3 Hours

Max. Marks : 100

Weightage of marks over different dimensions of the question paper shall be as follows:

A. Weightage to different topics/content units

S.No.	Topics	Marks
1.	Relations and Functions	10
2.	Algebra	13
3.	Calculus	44
4.	Vectors & three-dimensional Geometry	17
5.	Linear programming	06
6.	Probability	10
	Total	100

B. Weightage to different forms of questions

S.No.	Forms of Questions	Marks for each question	No. of Questions	Total marks
1.	Very Short Answer questions (VSA)	01	10	10
2.	Short Answer questions (SA)	04	12	48
3.	Long answer questions (LA)	06	07	42
	Total		29	100

C. Scheme of Options

There will be no overall choice. However, internal choice in any four questions of four marks each and any two questions of six marks each has been provided.

D. Difficulty level of questions

S.No.	Estimated difficulty level	Percentage of marks
1.	Easy	15
2.	Average	70
3.	Difficult	15

Based on the above design, separate sample papers along with their blue prints and Marking schemes have been included in this document. About 20% weightage has been assigned to questions testing higher order thinking skills of learners.

CBSE SAMPLE PAPER - I
CLASS XII MATHEMATICS
BLUE PRINT - I

S. No.	Topics	VSA	SA	LA	Total
1. (a)	Relations and Functions	1(1)	4(1)	-	
(b)	Inverse Trigonometric Functions	1(1)	4(1)	-	10(4)
2. (a)	Matrices	2(2)	-	6(1)	
(b)	Determinants	1(1)	4(1)	-	13(5)
3. (a)	Continuity and differentiability	-	8(2)	-	
(b)	Applications of derivatives	-	4(1)	6(1)	
(c)	Integration	2(2)	4(1)	6(1)	
(d)	Applications of Integrals	-	-	6(1)	
(e)	Differential Equations	-	8(2)	-	44(11)
4. (a)	Vectors	2(2)	4(1)	-	
(b)	3-dimensional Geometry	1(1)	4(1)	6(1)	17(6)
5.	Linear - Programming	-	-	6(1)	6(1)
6.	Probability	-	4(1)	6(1)	10(2)
	Total	10(10)	48(12)	42(7)	100(29)

SAMPLE PAPER - I

MATHEMATICS

CLASS - XII

Time : 3 Hours

Max. Marks : 100

General Instructions

1. All questions are compulsory.
2. The question paper consists of 29 questions divided into three sections A, B and C. Section A comprises of 10 questions of one mark each, section B comprises of 12 questions of four marks each and section C comprises of 07 questions of six marks each.
3. All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
4. There is no overall choice. However, internal choice has been provided in 04 questions of four marks each and 02 questions of six marks each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculators is not permitted. You may ask for logarithmic tables, if required.

SECTION A

1. Give an example to show that the relation R in the set of natural numbers, defined by $R = \{(x, y), x, y \in \mathbb{N}, x \leq y^2\}$ is not transitive.
2. Write the principal value of $\cos^{-1}(\cos \frac{5\pi}{3})$.
3. Find x, if $\begin{pmatrix} 5 & 3x \\ 2y & z \end{pmatrix} = \begin{pmatrix} 5 & 4 \\ 12 & 6 \end{pmatrix}^T$.
4. For what value of a, $\begin{pmatrix} 2a & -1 \\ -8 & 3 \end{pmatrix}$ is a singular matrix?
5. A square matrix A, of order 3, has $|A| = 5$, find $|A \cdot \text{adj}A|$.
6. Evaluate $\int 5^x dx$
7. Write the value of $\int_{-\pi/2}^{\pi/2} \sin^5 x dx$.
8. Find the position vector of the midpoint of the line segment joining the points $A(5\hat{i} + 3\hat{j})$ and $B(3\hat{i} - \hat{j})$.
9. If $\vec{a} = 2\hat{i} - \hat{j} + 3\hat{k}$ and $\vec{b} = (6\hat{i} + \lambda\hat{j} + 9\hat{k})$ and $\vec{a} \parallel \vec{b}$, find the value of λ .
10. Find the distance of the point (a,b,c) from x-axis.

SECTION B

11. Let N be the set of all natural numbers and R be the relation in $\mathbb{N} \times \mathbb{N}$ defined by (a,b) R (c,d) if $ad=bc$. Show that R is an equivalence relation.
12. Prove that $\tan^{-1}\left(\frac{1}{4}\right) + \tan^{-1}\left(\frac{2}{9}\right) = \frac{1}{2} \cos^{-1}\left(\frac{3}{5}\right)$.

OR

Solve for x : $\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2}$.

13. Using properties of determinants, prove that :

$$\begin{vmatrix} a^2+1 & ab & ac \\ ab & b^2+1 & bc \\ ca & cb & c^2+1 \end{vmatrix} = (1+a^2+b^2+c^2).$$

14. For what values of a and b, the function f defined as :

$$f(x) = \begin{cases} 3ax+b, & \text{if } x < 1 \\ 11, & \text{if } x = 1 \\ 5ax-2b, & \text{if } x > 1 \end{cases} \text{ is continuous at } x=1$$

15. If $x^y + y^x = a^b$, find $\frac{dy}{dx}$.

OR

If $x = a(\cos t + t \sin t)$ and $y = b(\sin t - t \cos t)$, find $\frac{d^2y}{dx^2}$.

16. Find the intervals in which the following function is strictly increasing or strictly decreasing :

$$f(x) = 20 - 9x + 6x^2 - x^3$$

OR

For the curve $y = 4x^3 - 2x^5$, find all points at which the tangent passes through origin.

17. Evaluate: $\int \frac{\sin x + \cos x}{\sqrt{\sin x \cos x}} dx$

OR

Evaluate: $\int e^x \left(\frac{x^2+1}{(x+1)^2} \right) dx$

18. Form the differential equation of the family of circles having radii 3.

19. Solve the following differential equation:

$$\sqrt{1+x^2+y^2+x^2y^2} + xy \frac{dy}{dx} = 0.$$

20. If the sum of two unit vectors is a unit vector, show that the magnitude of their difference is $\sqrt{3}$.

21. Find whether the lines $\vec{r} = (\hat{i} - \hat{j} - \hat{k}) + \lambda (2\hat{i} + \hat{j})$ and $\vec{r} = (2\hat{i} - \hat{j}) + \mu(\hat{i} + \hat{j} - \hat{k})$ intersect or not. If intersecting, find their point of intersection.
22. Three balls are drawn one by one without replacement from a bag containing 5 white and 4 green balls. Find the probability distribution of number of green balls drawn.

SECTION C

23. If $A = \begin{pmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{pmatrix}$, find A^{-1} and hence solve the following system of equations :

$$2x + y + 3z = 3$$

$$4x - y = 3$$

$$-7x + 2y + z = 2$$

OR

Using elementary transformations, find the inverse of the matrix :

$$\begin{pmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{pmatrix}$$

24. If the lengths of three sides of a trapezium, other than the base are equal to 10cm each, then find the area of trapezium when it is maximum.
25. Draw a rough sketch of the region enclosed between the circles $x^2 + y^2 = 4$ and $(x-2)^2 + y^2 = 1$. Using integration, find the area of the enclosed region.
26. Evaluate $\int_1^2 (x^2 + x + 2) dx$ as a limit of sums.

OR

Evaluate $\int_0^1 \sin^{-1}(x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2}) dx, 0 \leq x \leq 1$

27. Find the coordinates of the foot of the perpendicular and the perpendicular distance of the point (1, 3, 4) from the plane $2x - y + z + 3 = 0$. Find also, the image of the point in the plane.
28. An aeroplane can carry a maximum of 200 passengers. A profit of Rs. 1000 is made on each executive class ticket and a profit of Rs. 600 is made on each economy class ticket. The airline reserves at least 20 seats for the executive class. However, at least 4 times as many passengers prefer to travel by economy class, than by the executive class. Determine how many tickets of each type must be sold, in order to maximise profit for the airline. What is the maximum profit? Make an L.P.P. and solve it graphically.

29. A fair die is rolled. If 1 turns up, a ball is picked up at random from bag A, if 2 or 3 turns up, a ball is picked up at random from bag B, otherwise a ball is picked up from bag C. Bag A contains 3 red and 2 white balls, bag B contains 3 red and 4 white balls and bag C contains 4 red and 5 white balls. The die is rolled, a bag is picked up and a ball is drawn from it. If the ball drawn is red, what is the probability that bag B was picked up?