

CBSE QUESTION PAPER

CLASS-X

MATHS

SECTION - A

Question 1. Which of the following numbers has terminating decimal expansion?

(a) $\frac{37}{45}$

(b) $\frac{21}{2^3 5^6}$

(c) $\frac{17}{49}$

(d) $\frac{89}{2^2 3^2}$

Question 2:

If one of the zeroes of the quadratic polynomial $(k - 1)x^2 + kx + 1$ is -3 , then the value of k is

(a) $-\frac{4}{3}$

(b) $\frac{4}{3}$

(c) $\frac{2}{3}$

(d) $-\frac{2}{3}$

Question 3:

If a rational number x is expressed as $x = \frac{p}{q}$, where p, q are integers, $q \neq 0$ and p, q have no common factor (except 1), then the decimal expansion of x is terminating if and only if q has a prime factorization of the form:

(a) $2^m \cdot 5^n$

(b) $2^m 3^n$

(c) $2^m \cdot 7^n$

(d) $5^m \cdot 3^n$

Where m and n are non-negative integers.

Question 4:

If $0^\circ < x < 90^\circ$ and $2 \sin^2 x = \frac{1}{2}$, then the value of x is

(a) 90°

(b) 30°

(c) 15°

(d) 60°

Question 5:

If $\tan \theta = \frac{1}{\sqrt{7}}$, then the value of $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta}$ is

(a) $\frac{1}{5}$

(b) $\frac{3}{4}$

(c) $\frac{6}{4}$

(d) $\frac{4}{\sqrt{7}}$

Question 6:

Which of the following numbers has non-terminating repeating decimal expansion?

(a) $\frac{7}{80}$

(b) $\frac{17}{320}$

(c) $\frac{20}{100}$

(d) $\frac{93}{420}$

Question 7:

The value of p for which the polynomial $x^3 + 4x^2 - px + 8$ is exactly divisible by $(x - 2)$ is

- (a) 1
- (b) 0
- (c) 15
- (d) 16

Question 8:

$n^2 - 1$ is divisible by 8, if n is

- (a) an integer
- (b) a natural number
- (c) an odd integer
- (d) an even integer

Question 9:

If $\cot \theta + \frac{1}{\cot \theta} = 2$, then the value of $\cot^2 \theta + \frac{1}{\cot^2 \theta}$ is

- (a) -1
- (b) 1
- (c) 2
- (d) -2

Question 10:

The value of $\operatorname{cosec}^2 30^\circ \sin^2 45^\circ - \sec^2 60^\circ$ is

- a. -1
- b. 1
- c. -2
- d. 2

SECTION - B

Question 11: Use Euclid's division algorithm to find HCF of 870 and 225.

Question 12: Explain $5 \times 4 \times 3 \times 2 \times 1 + 3$ is a composite number.

Question 13:

If α and β are the zeroes of the quadratic polynomial $p(x) = x^2 - ax + b$, then find the value of $\alpha^2 + \beta^2$.

Question 14: Solve $37x + 43y = 123$, $43x + 37y = 117$

OR

Solve $x + \frac{6}{y} = 6$, $3x - \frac{8}{y} = 5$.

Question 15: In figure, $\triangle ABD$ is a right triangle, right-angled at A and $AC \perp BD$. Prove that $AB^2 = BC \cdot BD$

Question 16:

Without using trigonometric tables, find the value of

$$\frac{\cos 70^\circ}{\sin 20^\circ} + \cos 57^\circ \operatorname{cosec} 33^\circ - 2 \cos 60^\circ$$

OR

If A, B, C are interior angles of $\triangle ABC$, then show that

$$\cos\left(\frac{B+C}{2}\right) = \sin\frac{A}{2}$$

Question 17:

The following frequency distribution gives the monthly consumption of electricity of 68 consumers of a locality.

<i>Monthly Consumption (in units)</i>	65-85	85-105	105-125	125-145	145-165	165-185	185-205
<i>Number of consumers</i>	4	5	13	20	14	8	4

Write the above distribution as less than type cumulative frequency distribution.

Question 18:

Find the mode of the following data:

<i>Class</i>	0-20	20-40	40-60	60-80
<i>Frequency</i>	15	6	18	10

SECTION-C

Question19:

Prove that $3 + \sqrt{2}$ is an irrational number

Prove that $5\sqrt{2}$ is irrational number.

Question 20:

Show that 5^n can't end with the digit 2 for any natural number n.

Question 21

A and B are friends and their ages differ by year. A's father D is twice as old as A and B is twice as old as his sister C. The age of D and C differ by 40 years. Find the ages of A and B.

OR

Solve the following pair of equations:

$$\frac{5}{x-1} + \frac{1}{y-2} = 2$$

$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

Question 22:

Obtain all zeroes of the polynomial $f(x) = x^4 - 3x^2 = x^2 + 9x$ if two of its zeroes are $-\sqrt{3}$, and $\sqrt{3}$.

Question 23:

In figure, $\triangle ABC$ is right-angled at B, $BC=7\text{cm}$ and $AC - AB = 1\text{cm}$. Find the value of $\cos A - \sin A$.

Question 24:

$$\frac{\cos \theta}{\operatorname{cosec} \theta + 1} + \frac{\cos \theta}{\operatorname{cosec} \theta - 1} = 2 \tan \theta$$

Question 25:

$$\sqrt{\frac{1 + \sin \theta}{1 - \sin \theta}} + \sqrt{\frac{1 - \sin \theta}{1 + \sin \theta}} = 2 \sec \theta$$

Question 26:

In the figure, ABC is a triangle with $\angle B = 90^\circ$, Medians AE and CD of respective lengths $\sqrt{40}$ cm and 5cm are drawn. Find the length of the hypotenuse AC.

Question 27: Compute the median for the following cumulative frequency distribution :

Weight	Less than 38	Less than 40	Less than 42	Less than 44	Less than 46	Less than 48	Less than 50	Less than 52
Number of students	0	3	5	9	14	28	32	35

OR

Find the missing frequencies in the following frequency distribution table, if $N = 100$ and median is 32.

Marks obtained	0-10	10-20	20-30	30-40	40-50	50-50	Total
No. of students	10	?	25	30	?	10	100

Question 28: The mean of- the following frequency distribution is 25.2. Find the missing frequency x

C.I.	0-10	10-20	20-30	30-40	40-50
Frequency	8	X	10	11	9

SECTION - D

Question 29:

Divide $30x^4 + 11x^3 - 82x^2 - 12x + 48$ by $(3x^2 + 2x - 4)$ and verify the result by division algorithm.

Question 30:

If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, prove that the other two sides are divided in the same ratio. Solution. Given : A triangle ABC in which a line parallel to BC intersects other two sides AB and AC at D and E respectively.

OR

Prove that in a triangle, if the square of one side is equal to the sum of the squares of the other two sides, then the angle opposite to the first side is a right angle. Solution. Given : A triangle ABC such that :

Question 31. Without using trigonometric tables, evaluate the following :

$$\frac{\sec 37^\circ}{\operatorname{cosec} 53^\circ} + 2 \cot 15^\circ \cot 25^\circ \cot 45^\circ \cot 75^\circ \cot 65^\circ - 3(\sin^2 18^\circ + \sin^2 72^\circ)$$

OR

Prove that : $\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta} = 1 + \sec \theta \operatorname{cosec} \theta$

Question 32.

Form the pair of linear equations in the following problem, and find their solutions graphically. 10 students of Class X took part in a Mathematics quiz. If the number of girls is 4 more than the number of boys, find the number of boys and girls who took part in the quiz.

Question 33:

prove that $\sqrt{\frac{1+\sin A}{1-\sin A}} = \sec A + \tan A.$

Question 34:

m3.30. Solve the following system of linear equations graphically : $x+y=8$ $3x-2y=12$ Also find the coordinates of the points where the lines meet the z-axis.