

Mathematics – Test Paper

Time Allowed : 2 ½ hours

Max. Marks : 80

General Instructions :

Attempt all questions from **Section A** and any **four** questions from **Section B**.
All working, including rough work, must be clearly shown and must be done on the same sheet as the rest of the answer. Omission of essential working will result in the loss of marks.
Mathematical tables are provided.

Section A (40 Marks)

Attempt all questions from this section

1. (a) Find the value of a and b if $x - 1$ and $x - 2$ are factors of $x^3 - ax + b$. [3]

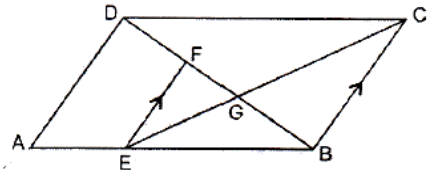
- (b) In the figure given below, ABCD is a parallelogram. E is a point on AB.

CE intersects the diagonal BD at G and EF is parallel to BC.

If $AE : EB = 1 : 2$ find

(i) $EF : AD$

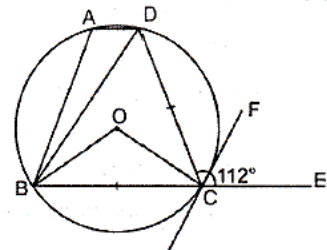
(ii) area of triangle BEF : area of triangle ABD [3]



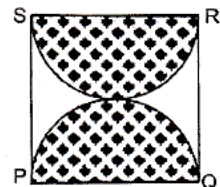
- (c) On a certain sum of money, the difference between the compound interest for a year, payable half yearly, and the simple interest for a year is Rs 16. Find the sum lent out, if the rate of interest in both cases is 8 % . [4]

2. (a) Plot the points A(9, 6) and B(5, 9) on the graph paper. These two points are the vertices of a figure ABCD which is symmetrical about $x = 5$ and $y = 6$. Complete the figure on the graph. Write down the geometrical name of the figure. [3]

- (b) In the figure, ABCD is a cyclic quadrilateral in which $BC = CD$ and CF is a tangent to the circle at C. BC is produced to E and $\angle DCE = 112^\circ$. If O is the centre of the circle, find (i) $\angle BOC$
(ii) $\angle DCF$. [3]



- (c) PQRS is a square piece of land of side 56 m. Two semicircular grass covered lawns are made on two of its opposite sides as shown in the figure. Calculate the area of the uncovered portion. [4]



3. (a) If $A = \begin{bmatrix} 4 & 4 \\ -2 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 1 \\ 3 & -2 \end{bmatrix}$, find the matrix D such that $3A - 2B + 2D = 0$ [3]

(b) A point P(a, b) is reflected in the y-axis to P'(-3, 1). Write down the values of a and b.

P'' is the image of P when reflected in the x axis. Write down the coordinates of P'.

P''' is the image of P when reflected in the line $x = 5$. Write down the coordinates of P'''. [3]

(c) Given : $A = \{x : 3 < 2x - 1 < 9, x \in \mathbb{R}\}$, $B = \{x : 11 \leq 3x + 2 \leq 23, x \in \mathbb{R}\}$, where R is the set of real numbers.

(i) Represent A and B on number lines

(ii) On the number line also mark $A \cap B$. [4]

4. (a) Without using a trigonometric table calculate: [3]

$$4 \frac{\sin 32^\circ}{\cos 58^\circ} + 5 \frac{\tan 48^\circ}{\cot 42^\circ} - 8 \frac{\sec 72^\circ}{\operatorname{cosec} 18^\circ}$$

(b) Mr. Jacob has a two years recurring deposit account in State Bank of India and deposits ₹ 1500 per month. If he receives ₹ 37,875 at the time of maturity, find the rate of interest. [3]

(c) Calculate the arithmetic mean, correct to one decimal place, for the following frequency distribution of marks obtained in a Geometry test.

Marks	0-10	10-20	20-30	30-40	40-50
No of students	7	13	15	12	3

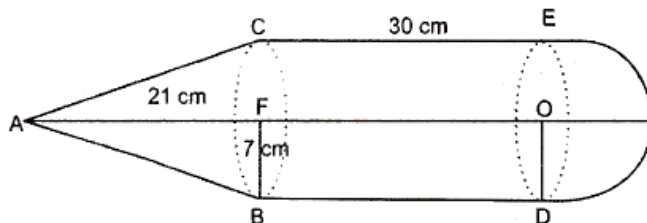
[4]

SECTION - B (40 Marks)

(Attempt any four questions from this section)

5. (a) If $\begin{bmatrix} 2 & 4 \\ 6 & 2 \end{bmatrix} \begin{bmatrix} 3x \\ 2 \end{bmatrix} + 2 \begin{bmatrix} 3 \\ 4 \end{bmatrix} = 5 \begin{bmatrix} 4 \\ y \end{bmatrix}$, find the values of x and y [3]

(b) In the diagram given below, if AF = 21 cm, CE = 30 cm and FB = 7 cm, find the volume of the figure. [3]



(c) A man bought 200 shares each of face value ₹10 at ₹ 12 per share. At the end of the year, the company from which he bought the shares declares a dividend of 15%. Calculate:

(i) the amount of money invested by the man

(ii) the amount of dividend he received

(iii) the percentage return on his outlay. [4]

6. (a) Solve the following quadratic equation for x and give your answer correct to three significant figures:

$$2x^2 - 4x - 3 = 0 \quad [3]$$

- (b) An integer is chosen at random from 1 to 50. Find the probability that the number is:

(i) divisible by 5 (ii) a perfect cube (iii) a prime number. [3]

- (c) Find x from the following equation using properties of proportion: [4]

$$\frac{x^2 - x + 1}{x^2 + x + 1} = \frac{14(x - 1)}{13(x + 1)}$$

7. (a) Bosco wishes to start a 200 m^2 rectangular vegetable garden. Since he has only 50 m barbed wire, he fences three sides of the rectangular garden letting his house compound wall act as the fourth side of the fence. Find the dimensions of the garden. [3]

- (b) Construct a triangle ABC, with $AB = 6 \text{ cm}$, $BC = 7 \text{ cm}$ and $\angle ABC = 60^\circ$.

Locate by construction the point P such that

(i) P is equidistant from B and C.

(ii) P is equidistant from AB and BC

(iii) Measure and record the length of PA. [3]

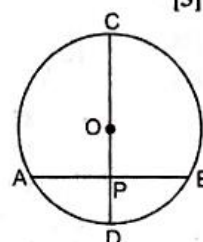
- (c) Mr. A. Ramchander has an account with Central Bank of India. The following entries are from his passbook:

Date	Particulars	Withdrawal	Deposits	Balance
05.01.2009	B/F			8000
20.01.2009	To self	2500		
04.02.2009	By cash		9000	
20.02.2009	By cash		3000	
04.03.2009	To self	1000		
15.04.2009	By cash		12000	

Complete the above page of his passbook and calculate the interest accumulated in four months, January to April at the rate of 3.5% per annum. If the interest is added on 30th April, find his balance on that date. [4]

8. (a) Prove that $\frac{1}{\sec x - \tan x} + \frac{1}{\sec x + \tan x} = \frac{2}{\cos x}$

- (b) In the figure given below, CD is the diameter of the circle which meets the chord AB at P such that $AP = BP = 12 \text{ cm}$. If $DP = 8 \text{ cm}$, find the radius of the circle. [3]



- (c) Prove that $A(2, 1)$, $B(0, 3)$ and $C(-2, 1)$ are the three vertices of an isosceles right angled triangle. Hence find the coordinates of a point D, if ABCD is a square. [4]

9. (a) A fair dice is rolled. Find the probability of getting
- 3 on the face of the dice
 - an odd number on the face of the dice
 - a number greater than 1 on the face of the dice. [3]
- (b) A (4, 2), B(6, 8) and C (8, 4) are the vertices of a triangle ABC. Write down the equation of the median of the triangle through A. [3]
- (c) The angle of elevation of an aeroplane from a point P on the ground is 60° . After 12 seconds from the same point P, the angle of elevation of the same plane changes to 30° . If the plane is flying horizontally at a speed of $600\sqrt{3}$ km/h, find the height at which the plane is flying. [4]

10. (a) The following table shows the distribution of the heights of a group of students:

Height (cm)	140-145	145-150	150-155	155-160	160-165	165-170	170-175
No of students	8	12	18	22	26	10	4

Use a graph sheet to draw an ogive for the distribution.

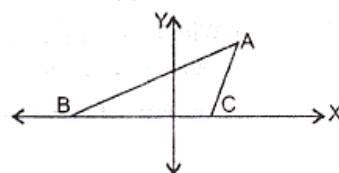
Use the ogive to find:

- the inter quartile range
 - the number of students whose height is more than 168 cm.
 - the number of students whose height is less than 148 cm. [6]
- (b) The manufacturer sold a TV to a wholesaler for ₹ 7000. The wholesaler sold it to a trader at a profit of ₹ 1000. If the trader sold it to the customer at a profit of ₹ 1500, find:
- the total VAT (value added tax) collected by the state government at the rate of 5%. [4]
 - the amount that the customer pays for the TV.

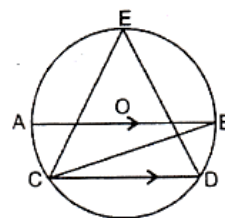
11. (a) In the diagram given below, equation of AB is $x - \sqrt{3}y + 1 = 0$ and equation of AC is $x - y - 2 = 0$

- Write down the angles that the lines AC and AB make with the positive direction of x-axis.

- Find $\angle BAC$. [3]



- (b) In the figure given below, O is the center of the circle. Chord CD is parallel to the diameter AB. If $\angle ABC = 35^\circ$, calculate $\angle CED$. [3]



- (c) Construct a triangle ABC, given that $AB = 6$ cm, $BC = 8$ cm and median $AD = 5$ cm. Construct an incircle to triangle ABC and measure its radius. [4]