

Class – XI
MATH SAMPLE PAPERS

Time Duration: 3 hours

M.M.100

Section - A

(Question No 1 Compulsory and Attempt **five** other questions)

Question 1

(3*10 = 30)

1. If $\log_{10}x = a$, find the value of 10^{2a-1} in terms of x .
2. If $p(11,r) = p(12,r-1)$ find r
3. $f:R \rightarrow R$ be defined as $f(x) = x^2+1$ find $f^{-1}(-5) = x$
4. Find the angle between the lines whose direction ratios are proportional to 4,-3,5 and 3,4,5.
5. show that $f(x) = (x-1)e^x+1$ is an increasing function on $(-\frac{\pi}{2}, \frac{\pi}{2})$
6. Evaluate $\lim_{x \rightarrow 0} \frac{\cos x - \cos y}{\cot x - \cot y}$
7. Show that the origin is equidistance from the line $4x+3y+10 = 0$; $5x-12y+26=0$ and $7x+24y = 50$
8. Find the sum and product of the roots $3x^2-4x+9$
9. Find two positive numbers whose difference is 12 and whose A.M exceeds the G.M by 3.
10. Find the antilogarithm of a) 1.23 b) 2.5647

Question 2:

1. Evaluate the following [5m]
 $\log_{10}10 + \log_{10}100 + \log_{10}1000 + \log_{10}10000$
2. If $a^x = b^y = c^z$ and x,y,z are in G.P prove that $\log_b a = \log_c b$ [3m]
3. $a = b^2 = c^3 = d^4$, prove that $(abcd) = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4}$ [3m]

Question 3:

1. Find the value of x and y if $\frac{x-1}{3+i} + \frac{y-1}{3+i} = i$ [5m]
2. Find the modulus and argument of the following complex number and write in polar form of $\frac{1+3i}{1-2i}$ [5m]

Question 4:

1. If a,b,c are in A.P, prove that $a^2+c^2+4ac = 2(ab+bc+ca)$ [5m]
2. Find the sum to n terms of the sequence $(x + \frac{1}{x})^2, (x^2 + \frac{1}{x^2})^2, (x^3 + \frac{1}{x^3})^2, \dots$ [3m]

3. Find the number of permutation of different things taken r at a time such that two specified things occur together [2m]

Question 5:

1. Sketch the graph of the given function $y = 2\cot 2x$ [4m]
2. Prove that $2\sin^2 \frac{\pi}{6} + \operatorname{cosec}^2 \frac{7\pi}{6} \cos^2 \frac{\pi}{3} = \frac{3}{2}$ [3m]
3. Find the radian measure corresponding to degree measures: [3m]
a) 300° b) -56°

Question 6:

- 1) Find the value of the function $f(x) = 1 + ax$, $a \neq 0$ is the inverse of the function. [4m]
- 2) For any set A, B, C, D prove that: $(A \times B) \cap (C \times D) = (A \cap C) \times (B \cap D)$ [3m]
- 3) Find the center and radius of the circle $x^2 + y^2 - 4x + 6y = 12$ [3m]

Question 7:

1. Evaluate $\int \sec^3 x \tan x \, dx$ [5m]
2. Find the image of the point (8, -12) with respect to the line mirror $4x + 7y + 13 = 0$ [5m]

Question 8:

1. Find the domain of the function $f(x)$ given by $f(x) = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$ [5m]
2. If $f(x) = \cos(\log x)$, then find the value of $f(x)f(y) - \frac{1}{2}[f(x/y) + f(xy)]$ [5m]

Section - B

(Attempt any two questions)

Question 9:

1. Determine the values of x for which $f(x) = x^x$, $x > 0$ is increasing or decreasing [4m]
2. Find the derivative of the function using first principles: $\cot \sqrt{x}$ [3m]
3. Discuss the differentiation of $f(x) = x^{|x|}$ at $x = 0$ [3m]

Question 10:

1. The mean and standard deviation of 15 observations are found to be 8 and 10 respectively. On rechecking it was found that an observation 4 was incorrect. Calculate the correct mean and standard deviation in the cases. [5m]
 2. Calculate the median of the given table [5m]
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|-----------|-------|-------|-------|-------|-------|-------|
| variables | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 |
| Frequency | 46 | 32 | 36 | 60 | 54 | 62 |

Question 11:

1. Find the average due date of the following bills: [5m]

Amount of the bill (Rs)	Date of acceptance of the bill	Period of the bill
5000	10-1-2013	3 months
4500	12-2-2013	2 months
3000	15-3-2013	1 months
2000	20-3-2013	2 months
1000	10-5-2013	3 months
750	13-6-2013	2 months

2. Find the median of the following distribution

[5m]

x:	0	1	2	3	4	5	6
f:	15	35	60	84	96	127	198