

266

Total No. of Questions-24

Total No. of Printed Pages-4

Regd. No.

Part III

MATHEMATICS

Paper II(A)

(English Version)

Time: 3 Hours Max. Marks: 75

Note :- This question paper consists of THREE sections A, B and C.

SECTION A

 $10 \times 2 = 20$

- I. Very Short Answer Type Questions :
 - (i) Answer ALL questions.
 - (ii) Each question carries TWO marks.

1. Write the complex number (2-3i)(3+4i) in the form A + iB.

2/e If $z_1 = -1$ and $z_2 = i$, then find $Arg\left(\frac{z_1}{z_2}\right)$.

3. If 1, w, w^2 are the cube roots of unity, prove that :

$$(a + b) (aw + bw^2) (aw^2 + bw) = a^3 + b^3.$$

Find the values of m for which the equation $x^2 - 15 - m(2x - 8) = 0$ have equal roots.

5/ If the product of the roots of $4x^3 + 16x^2 - 9x - a = 0$ is 9, then find a.

6.7 Find the number of different chains that can be prepared using 7 different coloured beads.

 n If n P_r = 5040, n C_r = 210, find n and r.

Find the set E of the values of x for which the binomial expansion of $(3-4x)^{\frac{3}{4}}$ is valid.

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P.T.O.

Find the mean deviation about the median for the following data:

The probability that a person chosen at random is left handed (in hand writing) is 0.1. What is the probability that in a group of 10 people, there is one who is left handed?

SECTION B

 $5 \times 4 = 20$

- II. Short Answer Type Questions:
 - (i) Answer ANY FIVE questions.
 - (ii) Each question carries FOUR marks.
- 11. If the point P denotes the complex number z = x + iy in the Argand plane and if $\frac{z-i}{z-1}$ is a purely imaginary number, find the locus of P.
- Prove that $\frac{1}{3x+1} + \frac{1}{x+1} \frac{1}{(3x+1)(x+1)}$ does not lie between 1 and 4 if x is real.
 - 13 If the letters of the word PRISON are permuted in all possible ways and the words thus formed are arranged in dictionary order, find the rank of the word PRISON.
 - 14 Simplify ${}^{34}C_5 + \sum_{r=0}^4 {}^{(38-r)}C_4$.

Assolve $\frac{x^2-3}{(x+2)(x^2+1)}$ into partial fractions.

16. State and prove Addition theorem on probability.

Suppose A and B are independent events with P(A) = 0.6, P(B) = 0.7. Then compute:

- (i) $P(A \cap B)$
- (ii) P(A ∪ B)
- (iii) P(B/A)
- (iv) $P(A^C \cap B^C)$.



SECTION C

 $5 \times 7 = 35$

III. Long Answer Type Questions :

- (i) Answer ANY FIVE questions.
- (ii) Each question carries SEVEN marks.

18. If n is an integer, then show that :

$$(1 + \cos \theta + i \sin \theta)^n + (1 + \cos \theta - i \sin \theta)^n = 2^{n+1} \cos^n \left(\frac{\theta}{2}\right) \cos\left(\frac{n\theta}{2}\right).$$

19 Solve the equation :

$$2x^5 + x^4 - 12x^3 - 12x^2 + x + 2 = 0.$$

20. If the coefficients of 4 consecutive terms in the expansion of $(1 + x)^n$ are a_1 , a_2 , a_3 , a_4 respectively, then show that:

$$\frac{a_1 \cdot}{a_1 + a_2} + \frac{a_3}{a_3 + a_4} = \frac{2a_2}{a_2 + a_3}$$

If
$$x = \frac{1.3}{3.6} + \frac{1.3.5}{3.6.9} + \frac{1.3.5.7}{3.6.9.12} + \dots$$
, then prove that : $9x^2 + 24x = 11$.

22. Find the mean deviation about the mean for the following data :

Marks Obtained	No. of Students		
0—10	5		
10—20	8		
20—30	15		
30—40	16 ~		
40—50	6		

23.

Three urns have the following composition of balls :

Urn I : 1 white, 2 black

Urn II : 2 white, 1 black

Urn III : 2 white, 2 black

One of the urns is selected at random and a ball is drawn. It turns out to be white. Find the probability that it came from urn III.

24. The probability distribution of a random variable X is given below

$X = x_i$				4	$P(X = x_i)$		
		1			- 72	k	76 T
		2	10.0			2k	12. Take 1
		3				3k	
		4		- L	e di gra	4k	
		5		4		5k	

Find the value of k and the mean and variance of X.