

S.S.L.C. EXAMINATION, MARCH - 2015
MATHEMATICS (English)

Time : 2½ Hours

Total Score : 80

Instructions :

- 1) Read questions carefully, understand each question and then answer.
- 2) Give explanations wherever necessary.
- 3) If there is an OR between any two questions, you may answer only one among them.
- 4) 15 minutes will be given at the beginning as cool off time. This time may be utilised to read and understand the questions.
- 5) Simplification using irrationals like $\sqrt{2}, \pi$ etc. with their approximate values is not required if not specified in the question.

[SCORE]

- 1) First term of an arithmetic sequence is 10 and its common difference 3. Write the first three terms of the sequence. Verify whether 100 is a term of this sequence. [2]
- 2) Which number added to the polynomial $3x^2 - 4x - 1$ gives a polynomial with $(x - 1)$ as a factor. [2]
- 3) If the equation $x^2 + kx + k = 0$ has only one solution, find the possible values of k . [2]
- 4) Draw x and y axes and mark the points $A(-1, 2)$, $B(6, 3)$. [2]

5) The scores obtained by 50 students in an examination is tabulated as shown below:

[3]

Score	Number of students
below 10	3
below 20	7
below 30	13
below 40	22
below 50	32
below 60	40
below 70	46
below 80	50

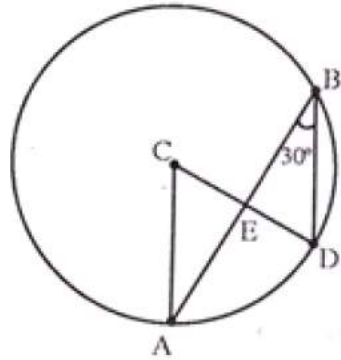
Find the median score.

6)

Sum of first n terms of an arithmetic sequence is $3n^2 + n$. Find the first term and common difference of this sequence.

[3]

7)



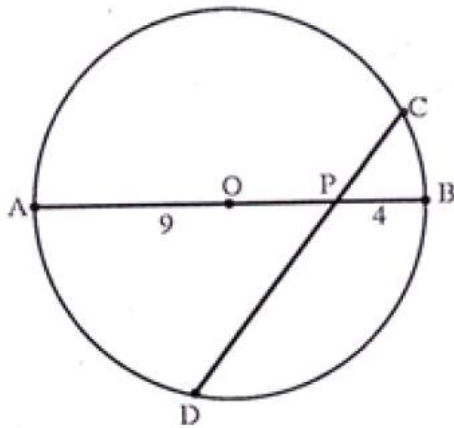
In the figure, C is the centre of the circle and $\angle ABD = 30^\circ$

[3]

- What is the measure of $\angle ACD$?
- If $\angle ABD = \angle CAB$ and $AB = 6$ cm, find the radius of the circle.

[SCORE]

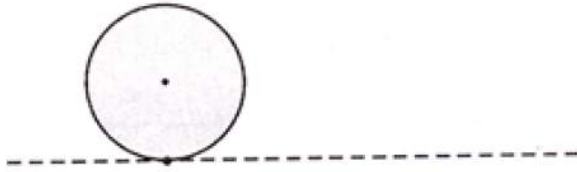
OR



In the figure O is the centre of the circle. CD is a chord which is not perpendicular to the diameter AB. $PA = 9$ cm and $PB = 4$ cm.

- What is $PC \times PD$?
- Show that the length of PC and PD cannot be natural numbers at a time.

Q8)



There is a mark on the outermost part of a wheel of radius 30 centimetres. Now the mark is close to the ground as shown in the figure. If the wheel rolls 31.4 centimetres on a straight line, then [3]

- a) Find the angle by which the wheel rotates (use $\pi = 3.14$ as an approximation).
- b) What will be the height of the mark from the ground?

9)

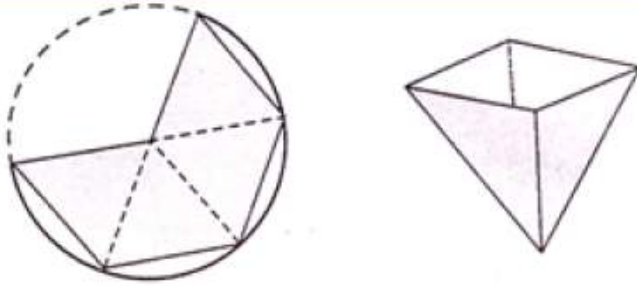
A box contains 8 black beads and 12 white beads. Another box contains 9 black beads and 6 white beads. One bead from each box is taken. [4]

- a) What is the probability that both beads are black?
- b) What is the probability of getting one black bead and one white bead?

10)

Write the polynomial $3x^2 - 5x - 2$ as a product of two first degree polynomials. [4]

11)



From a tin sheet, a sector of radius 20 centimetres and central angle 240° is divided into four equal parts as shown in the figure. Then the shaded portion is cut off. Using this, a vessel in the shape of a square pyramid is made. What is the capacity of this vessel?

[4]

12) The table below shows the classification of students participated in a camp, according to their height. Calculate the mean height of the students.

Height (cm)	Number of students
130-135	8
135-140	12
140-145	20
145-150	28
150-155	32
155-160	22
160-165	16
165-170	12

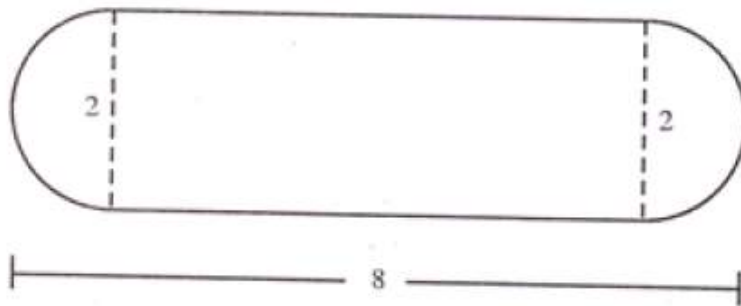
13)

- a) What is the volume of a solid metal cylinder of height 4 centimetres and radius 5 centimetres?
- b) This solid is melted and recast in to 5 cones of equal height and radius 2 centimetres. Find the height of such a cone.

OR

[4]

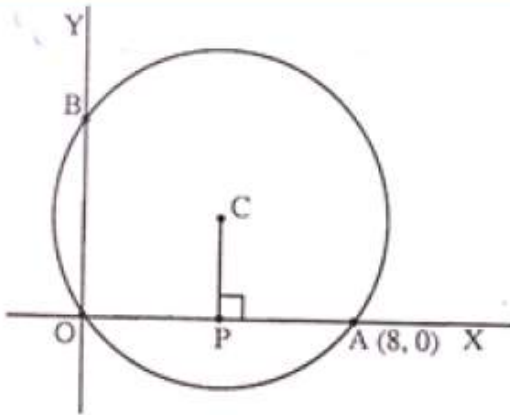
A tank is in the shape of a cylinder with two hemispheres attached to both ends as shown in the figure.



Its common diameter is 2 metres and total length is 8 metres. Find the total cost of painting the outer surface of this tank at the rate of 60 rupees per square metre.

(use $\pi = 3.14$ as an approximation)

14)



In the figure the radius of the circle centred at C is 5. The circle passes through the point A(8,0). If PC is perpendicular to x axis, find the coordinates of the points P, B and C.

[4]

15) The terms of an arithmetic sequence with common difference 4 are natural numbers.

[4]

- If x is a term in this sequence, what is the next term?
- If the sum of reciprocals of two consecutive terms of this sequence is $\frac{4}{15}$, find those terms.

OR

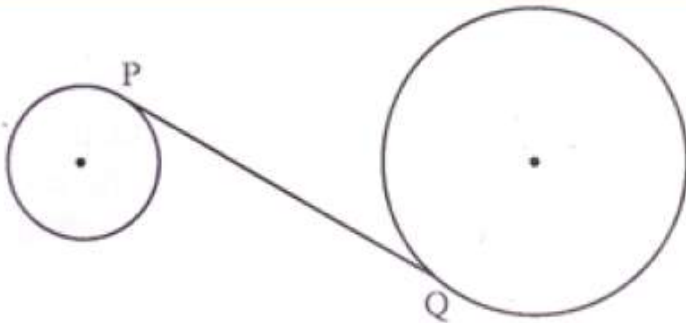
- Lengths of sides of a right angled triangle are in arithmetic sequence with common difference d . If the length of the smallest side of the triangle is $x-d$, write the length of its other two sides.
- Show that any right angled triangle with sides in arithmetic sequence is similar to the right angled triangle with sides 3, 4 and 5.

- 16) Draw a triangle of sides 5cm, 6cm and 7cm. Draw its incircle. Measure and read the radius of the incircle. [4]

- 17) A line of slope 2 passes through the point A (1, 3) [4]

- a) Check whether B(3,7) is a point on this line.
- b) Write down the equation of this line.
- c) Find the coordinates of a point C on the line such that $BC = 2AB$.

18)



In the figure, the radius of the smaller circle is 3 centimetres, that of the bigger circle is 6 centimetres and the distance between the centres of the circles is 15 centimetres. PQ is a tangent to both the circles. Find its length.

[4]

19) Consider the arithmetic sequence 9, 15, 21,.....

[5]

- Write the algebraic form of this sequence.
- Find the twenty fifth term of this sequence.
- Find the sum of terms from twenty fifth to fiftieth of this sequence.
- Can the sum of some terms of this sequence be 2015? Why?

20)

In triangle ABC, $AB = 5$ cm. $\angle A = 80^\circ$ and $\angle B = 70^\circ$. Calculate the radius of the circumcircle and length of the other two sides. (Necessary values can be taken from the following table)

[5]

Angle	sin	cos	tan
70°	0.94	0.34	2.75
80°	0.98	0.17	5.67

[SCORE]

OR

Gopi and Gautham stand on opposite sides of a tower. The children and the tower are on a straight line also. Gopi sees the top of the tower at an angle of elevation of 36° and Gautham sees it at an angle of elevation of 52° . The distance between the children is 60 metres.

- Draw a rough figure according to the given information.
- Find the height of the tower. (Height of children can be neglected. Necessary values can be taken from the following table).

Angle	sin	cos	tan
36°	0.59	0.81	0.72
52°	0.79	0.62	1.28

21) Equation of a line is $y=2x$

[5]

- A is a point on the line. If the x coordinate of A is -2 , find its y coordinate.
- Verify whether a circle of radius 5 centred at A passes through the point B(5, 5).
- Radius of a circle passing through B is 5 and its centre is on the above mentioned line. Find the coordinates of its centre.

22) Draw a triangle with sides 5cm, 6cm and 6cm. Draw a square having the same area of the triangle.

[5]

xxxxx