

Unit

9

Coordination Compounds

Objectives

After studying this Unit, you will be able to

- appreciate the postulates of Werner's theory of coordination compounds;
- know the meaning of the terms: coordination entity, central atom/ion, ligand, coordination number, coordination sphere, coordination polyhedron, oxidation number, homoleptic and heteroleptic;
- learn the rules of nomenclature of coordination compounds;
- write the formulas and names of mononuclear coordination compounds;
- define different types of isomerism in coordination compounds;
- understand the nature of bonding in coordination compounds in terms of the Valence Bond and Crystal Field theories;
- learn the stability of coordination compounds;
- appreciate the importance and applications of coordination compounds in our day to day life.

Coordination Compounds are the backbone of modern inorganic and bio-inorganic chemistry and chemical industry.

In the previous Unit we learnt that the transition metals form a large number of **complex compounds** in which the metal atoms are bound to a number of anions or neutral molecules. In modern terminology such compounds are called **coordination compounds**. The chemistry of coordination compounds is an important and challenging area of modern inorganic chemistry. New concepts of chemical bonding and molecular structure have provided insights into the functioning of vital components of biological systems. Chlorophyll, haemoglobin and vitamin B₁₂ are coordination compounds of magnesium, iron and cobalt respectively. Variety of metallurgical processes, industrial catalysts and analytical reagents involve the use of coordination compounds. Coordination compounds also find many applications in electroplating, textile dyeing and medicinal chemistry.

9.1 Werner's Theory of Coordination Compounds

Alfred Werner (1866-1919), a Swiss chemist was the first to formulate his ideas about the structures of coordination compounds. He prepared and characterised a large number of coordination compounds and studied their physical and chemical behaviour by simple experimental techniques. Werner proposed the concept of a **primary valence** and a **secondary valence** for a metal ion. Binary compounds such as CrCl₃, CoCl₂ or PdCl₂ have primary valence of 3, 2 and 2 respectively. In a series of compounds of cobalt(III) chloride with ammonia, it was found that some of the chloride ions could be precipitated as AgCl on adding excess silver nitrate solution in cold but some remained in solution.

| | | | |
|-------|--|------|------------|
| 1 mol | CoCl ₃ .6NH ₃ (Yellow) | gave | 3 mol AgCl |
| 1 mol | CoCl ₃ .5NH ₃ (Purple) | gave | 2 mol AgCl |
| 1 mol | CoCl ₃ .4NH ₃ (Green) | gave | 1 mol AgCl |
| 1 mol | CoCl ₃ .4NH ₃ (Violet) | gave | 1 mol AgCl |

These observations, together with the results of conductivity measurements in solution can be explained if (i) six groups in all, either chloride ions or ammonia molecules or both, remain bonded to the cobalt ion during the reaction and (ii) the compounds are formulated as shown in Table 9.1, where the atoms within the square brackets form a single entity which does not dissociate under the reaction conditions. Werner proposed the term **secondary valence** for the number of groups bound directly to the metal ion; in each of these examples the secondary valences are six.

Table 9.1: Formulation of Cobalt(III) Chloride-Ammonia Complexes

| Colour | Formula | Solution conductivity corresponds to |
|--------|---|--------------------------------------|
| Yellow | [Co(NH ₃) ₆] ³⁺ 3Cl [−] | 1:3 electrolyte |
| Purple | [CoCl(NH ₃) ₅] ²⁺ 2Cl [−] | 1:2 electrolyte |
| Green | [CoCl ₂ (NH ₃) ₄] ⁺ Cl [−] | 1:1 electrolyte |
| Violet | [CoCl ₂ (NH ₃) ₄] ⁺ Cl [−] | 1:1 electrolyte |

Note that the last two compounds in Table 9.1 have identical empirical formula, CoCl₃.4NH₃, but distinct properties. Such compounds are termed as isomers. Werner in 1898, propounded his theory of coordination compounds. The main postulates are:

1. In coordination compounds metals show two types of linkages (valences)-primary and secondary.
2. The primary valences are normally ionisable and are satisfied by negative ions.
3. The secondary valences are non ionisable. These are satisfied by neutral molecules or negative ions. The secondary valence is equal to the coordination number and is fixed for a metal.
4. The ions/groups bound by the secondary linkages to the metal have characteristic spatial arrangements corresponding to different coordination numbers.

In modern formulations, such spatial arrangements are called coordination *polyhedra*. The species within the square bracket are coordination entities or complexes and the ions outside the square bracket are called counter ions.

He further postulated that octahedral, tetrahedral and square planar geometrical shapes are more common in coordination compounds of transition metals. Thus, [Co(NH₃)₆]³⁺, [CoCl(NH₃)₅]²⁺ and [CoCl₂(NH₃)₄]⁺ are octahedral entities, while [Ni(CO)₄] and [PtCl₄]^{2−} are tetrahedral and square planar, respectively.

On the basis of the following observations made with aqueous solutions, [Example 9.1](#)
assign secondary valences to metals in the following compounds:

| Formula | Moles of AgCl precipitated per mole of the compounds with excess AgNO ₃ |
|---|--|
| (i) PdCl ₂ .4NH ₃ | 2 |
| (ii) NiCl ₂ .6H ₂ O | 2 |
| (iii) PtCl ₄ .2HCl | 0 |
| (iv) CoCl ₃ .4NH ₃ | 1 |
| (v) PtCl ₂ .2NH ₃ | 0 |

(i) Secondary 4
(iii) Secondary 6

(ii) Secondary 6
(iv) Secondary 6

(v) Secondary 4

[Solution](#)

Difference between a double salt and a complex

Both double salts as well as complexes are formed by the combination of two or more stable compounds in stoichiometric ratio. However, they differ in the fact that double salts such as carnallite, KCl.MgCl₂.6H₂O, Mohr's salt, FeSO₄.(NH₄)₂SO₄.6H₂O, potash alum, KAl(SO₄)₂.12H₂O, etc. dissociate into simple ions completely when dissolved in water. However, complex ions such as [Fe(CN)₆]⁴⁻ of K₄[Fe(CN)₆] do not dissociate into Fe²⁺ and CN⁻ ions.



1866-1919

Werner was born on December 12, 1866, in Mülhouse, a small community in the French province of Alsace. His study of chemistry began in Karlsruhe (Germany) and continued in Zurich (Switzerland), where in his doctoral thesis in 1890, he explained the difference in properties of certain nitrogen containing organic substances on the basis of isomerism. He extended van Hoff's theory of tetrahedral carbon atom and modified

it for nitrogen. Werner showed optical and electrical differences between complex compounds based on physical measurements. In fact, Werner was the first to discover optical activity in certain coordination compounds.

He, at the age of 29 years became a full professor at Technische Hochschule in Zurich in 1895. Alfred Werner was a chemist and educationist. His accomplishments included the development of the theory of coordination compounds. This theory, in which Werner proposed revolutionary ideas about how atoms and molecules are linked together, was formulated in a span of only three years, from 1890 to 1893. The remainder of his career was spent gathering the experimental support required to validate his new ideas. Werner became the first Swiss chemist to win the Nobel Prize in 1913 for his work on the linkage of atoms and the coordination theory.

(a) **Coordination entity**

A coordination entity constitutes a central metal atom or ion bonded to a fixed number of ions or molecules. For example, $[\text{CoCl}_3(\text{NH}_3)_3]$ is a coordination entity in which the cobalt ion is surrounded by three ammonia molecules and three chloride ions. Other examples are $[\text{Ni}(\text{CO})_4]$, $[\text{PtCl}_2(\text{NH}_3)_2]$, $[\text{Fe}(\text{CN})_6]^{4-}$, $[\text{Co}(\text{NH}_3)_6]^{3+}$.

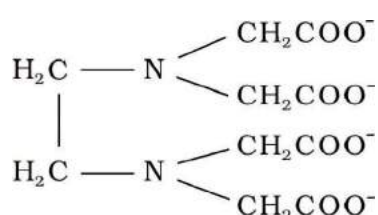
(b) **Central atom/ion**

In a coordination entity, the atom/ion to which a fixed number of ions/groups are bound in a definite geometrical arrangement around it, is called the central atom or ion. For example, the central atom/ion in the coordination entities: $[\text{NiCl}_2(\text{H}_2\text{O})_4]$, $[\text{CoCl}(\text{NH}_3)_5]^{2+}$ and $[\text{Fe}(\text{CN})_6]^{3-}$ are Ni^{2+} , Co^{3+} and Fe^{3+} , respectively. These central atoms/ions are also referred to as **Lewis acids**.

(c) **Ligands**

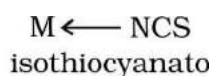
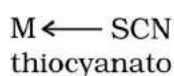
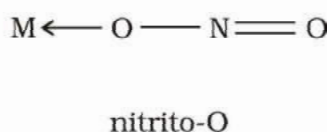
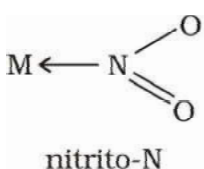
The ions or molecules bound to the central atom/ion in the coordination entity are called ligands. These may be simple ions such as Cl^- , small molecules such as H_2O or NH_3 , larger molecules such as $\text{H}_2\text{NCH}_2\text{CH}_2\text{NH}_2$ or $\text{N}(\text{CH}_2\text{CH}_2\text{NH}_2)_3$ or even macromolecules, such as proteins.

When a ligand is bound to a metal ion through a single donor atom, as with Cl^- , H_2O or NH_3 , the ligand is said to be **unidentate**.



When a ligand can bind through two donor atoms as in $\text{H}_2\text{NCH}_2\text{CH}_2\text{NH}_2$ (ethane-1,2-diamine) or $\text{C}_2\text{O}_4^{2-}$ (oxalate), the ligand is said to be **didentate** and when several donor atoms are present in a single ligand as in $\text{N}(\text{CH}_2\text{CH}_2\text{NH}_2)_3$, the ligand is said to be **polydentate**. Ethylenediaminetetraacetate ion (EDTA^{4-}) is an important hexadentate ligand. It can bind through two nitrogen and four oxygen atoms to a central metal ion.

When a di- or polydentate ligand uses its two or more donor atoms to bind a single metal ion, it is said to be a **chelate** ligand. The number of such ligating groups is called the **denticity** of the ligand. Such complexes, called chelate complexes tend to be more stable than similar complexes containing unidentate ligands (for



reasons see Section 9.8). Ligand which can ligate through two different atoms is called **ambidentate ligand**. Examples of such ligands are the NO_2^- and SCN^- ions. NO_2^- ion can coordinate either through nitrogen or through oxygen to a central metal atom/ion. Similarly, SCN^- ion can coordinate through the sulphur or nitrogen atom.

(d) **Coordination number**

The coordination number (CN) of a metal ion in a complex can be defined as the number of ligand donor atoms to which the metal is directly bonded. For example, in the complex ions, $[\text{PtCl}_6]^{2-}$ and $[\text{Ni}(\text{NH}_3)_4]^{2+}$, the coordination number of Pt and Ni are 6 and 4 respectively. Similarly, in the complex ions, $[\text{Fe}(\text{C}_2\text{O}_4)_3]^{3-}$ and $[\text{Co}(\text{en})_3]^{3+}$, the coordination number of both, Fe and Co, is 6 because $\text{C}_2\text{O}_4^{2-}$ and en (ethane-1,2-diamine) are didentate ligands.

It is important to note here that coordination number of the central atom/ion is determined only by the number of sigma bonds formed by the ligand with the central atom/ion. Pi bonds, if formed between the ligand and the central atom/ion, are not counted for this purpose.

(e) Coordination sphere

The central atom/ion and the ligands attached to it are enclosed in square bracket and is collectively termed as the **coordination sphere**. The ionisable groups are written outside the bracket and are called counter ions. For example, in the complex $K_4[Fe(CN)_6]$, the coordination sphere is $[Fe(CN)_6]^{4-}$ and the counter ion is K^+ .

(f) Coordination polyhedron

The spatial arrangement of the ligand atoms which are directly attached to the central atom/ion defines a coordination polyhedron about the central atom. The most common coordination polyhedra are octahedral, square planar and tetrahedral. For example, $[Co(NH_3)_6]^{3+}$ is octahedral, $[Ni(CO)_4]$ is tetrahedral and $[PtCl_4]^{2-}$ is square planar. Fig. 9.1 shows the shapes of different coordination polyhedra.

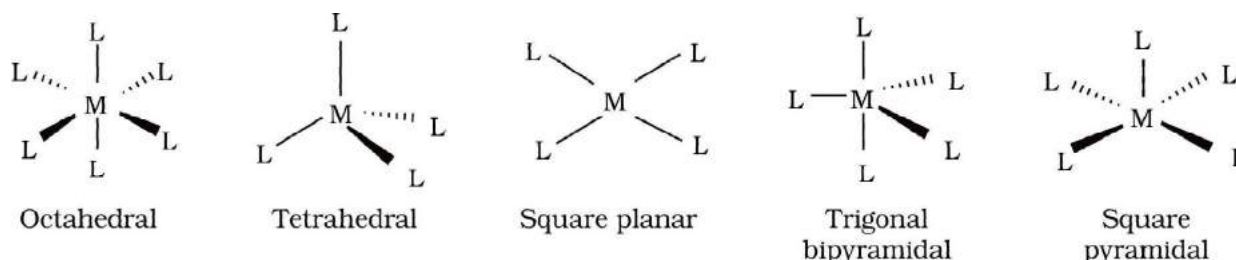


Fig. 9.1: Shapes of different coordination polyhedra. *M* represents the central atom/ion and *L*, a unidentate ligand.

(g) Oxidation number of central atom

The oxidation number of the central atom in a complex is defined as the charge it would carry if all the ligands are removed along with the electron pairs that are shared with the central atom. The oxidation number is represented by a Roman numeral in parenthesis following the name of the coordination entity. For example, oxidation number of copper in $[Cu(CN)_4]^{3-}$ is +1 and it is written as Cu(I).

(h) Homoleptic and heteroleptic complexes

Complexes in which a metal is bound to only one kind of donor groups, *e.g.*, $[Co(NH_3)_6]^{3+}$, are known as homoleptic. Complexes in which a metal is bound to more than one kind of donor groups, *e.g.*, $[Co(NH_3)_4Cl_2]^+$, are known as heteroleptic.

9.1 Nomenclature of Coordination Compounds

Nomenclature is important in Coordination Chemistry because of the need to have an unambiguous method of describing formulas and writing systematic names, particularly when dealing with isomers. The formulas and names adopted for coordination entities are based on the recommendations of the International Union of Pure and Applied Chemistry (IUPAC).

9.3.1 Formulas of Mononuclear Coordination Entities

The formula of a compound is a shorthand tool used to provide basic information about the constitution of the compound in a concise and convenient manner. Mononuclear coordination entities contain a single central metal atom. The following rules are applied while writing the formulas:

- (i) The central atom is listed first.
- (ii) The ligands are then listed in alphabetical order. The placement of a ligand in the list does not depend on its charge.
- (iii) Polydentate ligands are also listed alphabetically. In case of abbreviated ligand, the first letter of the abbreviation is used to determine the position of the ligand in the alphabetical order.
- (iv) The formula for the entire coordination entity, whether charged or not, is enclosed in square brackets. When ligands are polyatomic, their formulas are enclosed in parentheses. Ligand abbreviations are also enclosed in parentheses.
- (v) There should be no space between the ligands and the metal within a coordination sphere.
- (vi) When the formula of a charged coordination entity is to be written without that of the counter ion, the charge is indicated outside the square brackets as a right superscript with the number before the sign. For example, $[\text{Co}(\text{CN})_6]^{3-}$, $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$, etc.
- (vii) The charge of the cation(s) is balanced by the charge of the anion(s).

Note: The 2004 IUPAC draft recommends that ligands will be sorted alphabetically, irrespective of charge.

9.3.2 Naming of Mononuclear Coordination Compounds

The names of coordination compounds are derived by following the principles of additive nomenclature. Thus, the groups that surround the central atom must be identified in the name. They are listed as prefixes to the name of the central atom along with any appropriate multipliers. The following rules are used when naming coordination compounds:

- (i) The cation is named first in both positively and negatively charged coordination entities.
- (ii) The ligands are named in an alphabetical order before the name of the central atom/ion. (This procedure is reversed from writing formula).
- (iii) Names of the anionic ligands end in -o, those of neutral and cationic ligands are the same except aqua for H_2O , ammine for NH_3 , carbonyl for CO and nitrosyl for NO . These are placed within enclosing marks () when written in the formula of coordination entity.
- (iv) Prefixes mono, di, tri, etc., are used to indicate the number of the individual ligands in the coordination entity. When the names of the ligands include a numerical prefix, then the terms, *bis*, *tris*, *tetrakis* are used, the ligand to which they refer being placed in parentheses. For example, $[\text{NiCl}_2(\text{PPh}_3)_2]$ is named as dichloridobis(triphenylphosphine)nickel(II).
- (v) Oxidation state of the metal in cation, anion or neutral coordination entity is indicated by Roman numeral in parenthesis.
- (vi) If the complex ion is a cation, the metal is named same as the element. For example, Co in a complex cation is called cobalt and Pt is called platinum. If the complex ion is an anion, the name of the metal ends with the suffix -ate. For example, Co in a complex anion, $[\text{Co}(\text{SCN})_4]^{2-}$ is called cobaltate. For some metals, the Latin names are used in the complex anions, e.g., ferrate for Fe.

Note: The 2004 IUPAC draft recommends that anionic ligands will end with -ido so that chloro would become chlorido, etc.

(vii) The neutral complex molecule is named similar to that of the complex cation.

The following examples illustrate the nomenclature for coordination compounds.

1. $[\text{Cr}(\text{NH}_3)_3(\text{H}_2\text{O})_3]\text{Cl}_3$ is named as:

triamminetriaquachromium(III) chloride

Explanation: The complex ion is inside the square bracket, which is a cation. The amine ligands are named before the aqua ligands according to alphabetical order. Since there are three chloride ions in the compound, the charge on the complex ion must be +3 (since the compound is electrically neutral). From the charge on the complex ion and the charge on the ligands, we can calculate the oxidation number of the metal. In this example, all the ligands are neutral molecules. Therefore, the oxidation number of chromium must be the same as the charge of the complex ion, +3.

2. $[\text{Co}(\text{H}_2\text{NCH}_2\text{CH}_2\text{NH}_2)_3]_2(\text{SO}_4)_3$ is named as:

tris(ethane-1,2-diamine)cobalt(III) sulphate

Explanation: The sulphate is the counter anion in this molecule. Since it takes 3 sulphates to bond with two complex cations, the charge on each complex cation must be +3. Further, ethane-1,2-diamine is a neutral molecule, so the oxidation number of cobalt in the complex ion must be +3. Remember that you never have to indicate the number of cations and anions in the name of an ionic compound.

3. $[\text{Ag}(\text{NH}_3)_2][\text{Ag}(\text{CN})_2]$ is named as:

diamminesilver(I) dicyanidoargentate(I)

Notice how the name of the metal differs in cation and anion even though they contain the same metal ions.

Example 9.

Write the formulas for the following coordination compounds:

- Tetraammineaquachloridocobalt(III) chloride
- Potassium tetrahydroxidozincate(II)
- Potassium trioxalatoaluminate(III)
- Dichloridobis(ethane-1,2-diamine)cobalt(III)
- Tetracarbonylnickel(0)

Solution

- $[\text{Co}(\text{NH}_3)_4(\text{H}_2\text{O})\text{Cl}]\text{Cl}_2$
- $\text{K}_2[\text{Zn}(\text{OH})_4]$
- $\text{K}_3[\text{Al}(\text{C}_2\text{O}_4)_3]$
- $[\text{CoCl}_2(\text{en})_2]^+$
- $[\text{Ni}(\text{CO})_4]$

Example 9.

Write the IUPAC names of the following coordination compounds:

- $[\text{Pt}(\text{NH}_3)_2\text{Cl}(\text{NO}_2)]$
- $\text{K}_3[\text{Cr}(\text{C}_2\text{O}_4)_3]$
- $[\text{CoCl}_2(\text{en})_2]\text{Cl}$
- $[\text{Co}(\text{NH}_3)_5(\text{CO}_3)]\text{Cl}$
- $\text{Hg}[\text{Co}(\text{SCN})_4]$

Solution

- Diamminechloridonitrito-N-platinum(II)
- Potassium trioxalatochromate(III)
- Dichloridobis(ethane-1,2-diamine)cobalt(III) chloride
- Pentaamminecarbonatocobalt(III) chloride
- Mercury (I) tetrathiocyanatocobaltate(III)

Inte t Questions

9.1 Write the formulas for the following coordination compounds:

- Tetraamminediaquacobalt(III) chloride
- Potassium tetracyanonickelate(II)
- Tris(ethane-1,2-diamine) chromium(III) chloride
- Amminebromidochloridonitrito-N-platinate(II)
- Dichloridobis(ethane-1,2-diamine)platinum(IV) nitrate
- Iron(III) hexacyanidoferrate(II)

9.2 Write the IUPAC names of the following coordination compounds:

- $[\text{Co}(\text{NH}_3)_6]\text{Cl}_3$
- $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$
- $\text{K}_3[\text{Fe}(\text{CN})_6]$
- $\text{K}_3[\text{Fe}(\text{C}_2\text{O}_4)_3]$
- $\text{K}_2[\text{PdCl}_4]$
- $[\text{Pt}(\text{NH}_3)_2\text{Cl}(\text{NH}_2\text{CH}_3)]\text{Cl}$

9. Isomerism in Coordination Compounds

Isomers are two or more compounds that have the same chemical formula but a different arrangement of atoms. Because of the different arrangement of atoms, they differ in one or more physical or chemical properties. Two principal types of isomerism are known among coordination compounds. Each of which can be further subdivided.

(a) Stereoisomerism

- Geometrical isomerism
- Optical isomerism

(b) Structural isomerism

- Linkage isomerism
- Coordination isomerism
- Ionisation isomerism
- Solvate isomerism

Stereoisomers have the same chemical formula and chemical bonds but they have different spatial arrangement. Structural isomers have different bonds. A detailed account of these isomers are given below.

9.4.1 Geometric Isomerism

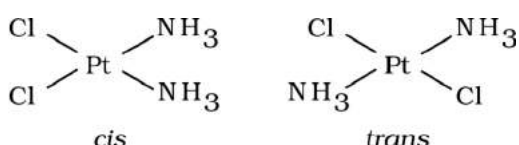


Fig. 9.2: Geometrical isomers (*cis* and *trans*) of $\text{Pt}(\text{NH}_3)_2\text{Cl}_2$

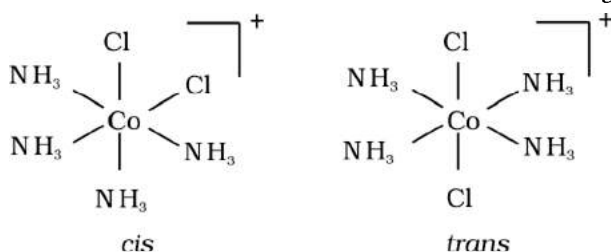


Fig. 9.3: Geometrical isomers (*cis* and *trans*) of $[\text{Co}(\text{NH}_3)_4\text{Cl}_2]^+$

This type of isomerism arises in heteroleptic complexes due to different possible geometric arrangements of the ligands. Important examples of this behaviour are found with coordination numbers 4 and 6. In a square planar complex of formula $[\text{MX}_2\text{L}_2]$ (X and L are unidentate), the two ligands X may be arranged adjacent to each other in a **cis** isomer, or opposite to each other in a **trans** isomer as depicted in Fig. 9.2.

Other square planar complex of the type MABXL (where A, B, X, L are unidentates) shows three isomers—two *cis* and one *trans*. You may attempt to draw these structures. Such isomerism is not possible for a tetrahedral geometry but similar behaviour is possible in octahedral complexes of formula $[\text{MX}_2\text{L}_4]$ in which the two ligands X may be oriented **cis** or **trans** to each other (Fig. 9.3).

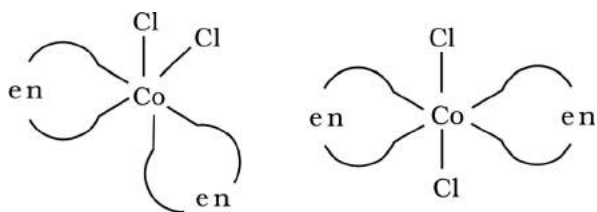
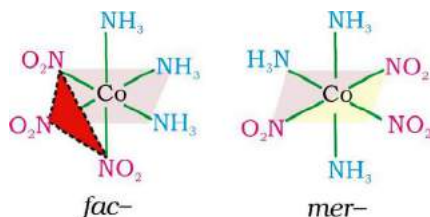


Fig. 9.4: Geometrical isomers (cis and trans) of $[\text{CoCl}_2(\text{en})_2]$

Fig. 9.5
The facial (fac) and meridional (mer) isomers of $[\text{Co}(\text{NH}_3)_3(\text{NO}_2)_3]$



This type of isomerism also arises when didentate ligands $\text{L}-\text{L}$ [e.g., $\text{NH}_2\text{CH}_2\text{CH}_2\text{NH}_2$ (en)] are present in complexes of formula $[\text{MX}_2(\text{L}-\text{L})_2]$ (Fig. 9.4).

Another type of geometrical isomerism occurs in octahedral coordination entities of the type $[\text{Ma}_3\text{b}_3]$ like $[\text{Co}(\text{NH}_3)_3(\text{NO}_2)_3]$. If three donor atoms of the same ligands occupy adjacent positions at the corners of an octahedral face, we have the **facial (fac) isomer**. When the positions are around the meridian of the octahedron, we get the **meridional (mer) isomer** (Fig. 9.5).

Why is geometrical isomerism not possible in tetrahedral complexes having two different types of unidentate ligands coordinated with the central metal ion ?

Tetrahedral complexes do not show geometrical isomerism because the relative positions of the unidentate ligands attached to the central metal atom are the same with respect to each other.

[Example 9.1](#)

[Solution](#)

9.4.2 Optical Isomerism

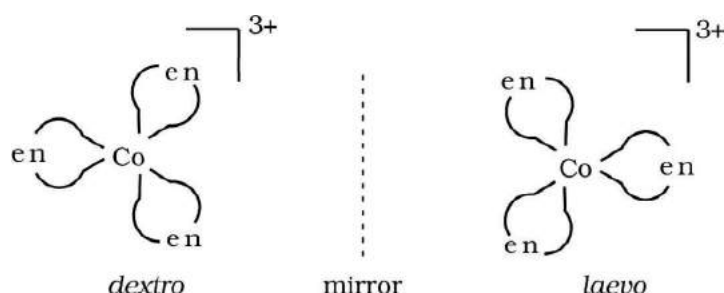
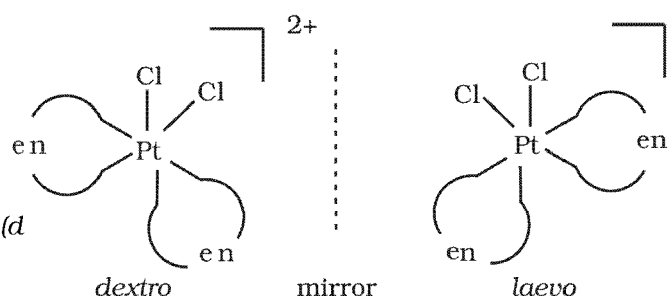


Fig.9.6: Optical isomers (d and l) of $[\text{Co}(\text{en})_3]^{3+}$

Optical isomers are mirror images that cannot be superimposed on one another. These are called as *enantiomers*. The molecules or ions that cannot be superimposed are called *chiral*. The two forms are called *dextro* (*d*) and *laevo* (*l*) depending upon the direction they rotate the plane of polarised light in a polarimeter (*d* rotates to the right, *l* to the left). Optical isomerism is common in octahedral complexes involving didentate ligands (Fig. 9.6).

In a coordination entity of the type $[\text{PtCl}_2(\text{en})_2]^{2+}$, only the **cis**-isomer shows optical activity (Fig. 9.7).

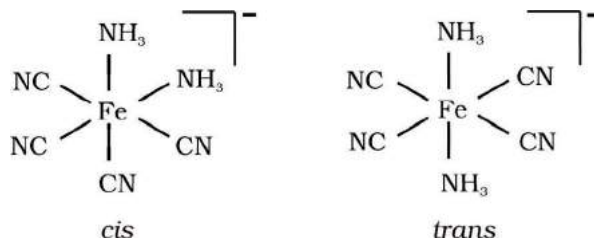
Fig.9.7
Optical isomers (*d* and *l*) of **cis**- $[\text{PtCl}_2(\text{en})_2]^{2+}$



Example 9.1

Draw structures of geometrical isomers of $[\text{Fe}(\text{NH}_3)_2(\text{CN})_4]^-$

Solution



Example 9.2

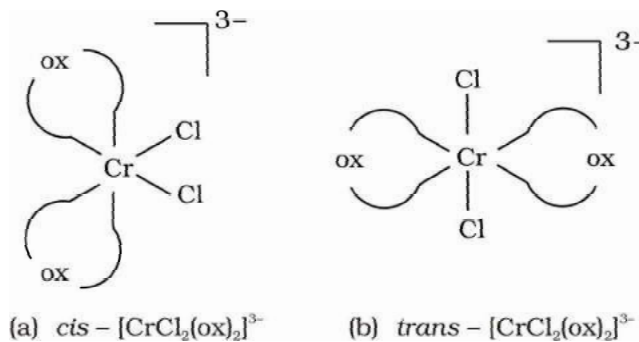
Out of the following two coordination entities which is chiral (optically active)?

(a) $\text{cis}-[\text{CrCl}_2(\text{ox})_2]^{3-}$

(b) $\text{trans}-[\text{CrCl}_2(\text{ox})_2]^{3-}$

Solution

The two entities are represented as



Out of the two, (a) $\text{cis}-[\text{CrCl}_2(\text{ox})_2]^{3-}$ is chiral (optically active).

9.4.3 Linkage Isomerism

Linkage isomerism arises in a coordination compound containing ambidentate ligand. A simple example is provided by complexes containing the thiocyanate ligand, NCS^- , which may bind through the nitrogen to give $\text{M}-\text{NCS}$ or through sulphur to give $\text{M}-\text{SCN}$. Jørgensen discovered such behaviour in the complex $[\text{Co}(\text{NH}_3)_5(\text{NO}_2)]\text{Cl}_2$, which is obtained as the red form, in which the nitrite ligand is bound through oxygen ($-\text{ONO}$), and as the yellow form, in which the nitrite ligand is bound through nitrogen ($-\text{NO}_2$).

9.4.4 Coordination Isomerism

This type of isomerism arises from the interchange of ligands between cationic and anionic entities of different metal ions present in a complex. An example is provided by $[\text{Co}(\text{NH}_3)_6][\text{Cr}(\text{CN})_6]$, in which the NH_3 ligands are bound to Co^{3+} and the CN^- ligands to Cr^{3+} . In its coordination isomer $[\text{Cr}(\text{NH}_3)_6][\text{Co}(\text{CN})_6]$, the NH_3 ligands are bound to Cr^{3+} and the CN^- ligands to Co^{3+} .

9.4.5 Ionisation Isomerism

This form of isomerism arises when the counter ion in a complex salt is itself a potential ligand and can displace a ligand which can then become the counter ion. An example is provided by the ionisation isomers $[\text{Co}(\text{NH}_3)_5(\text{SO}_4)]\text{Br}$ and $[\text{Co}(\text{NH}_3)_5\text{Br}]\text{SO}_4$.

9.4.6 Solvate Isomerism

This form of isomerism is known as ‘hydrate isomerism’ in case where water is involved as a solvent. This is similar to ionisation isomerism. Solvate isomers differ by whether or not a solvent molecule is directly bonded to the metal ion or merely present as free solvent molecules in the crystal lattice. An example is provided by the aqua complex $[\text{Cr}(\text{H}_2\text{O})_6]\text{Cl}_3$ (violet) and its solvate isomer $[\text{Cr}(\text{H}_2\text{O})_5\text{Cl}]\text{Cl}_2\cdot\text{H}_2\text{O}$ (grey-green).

Inte t Questions

- 9.3 Indicate the types of isomerism exhibited by the following complexes and draw the structures for these isomers:
- (i) $\text{K}[\text{Cr}(\text{H}_2\text{O})_2(\text{C}_2\text{O}_4)_2]$

(ii) $[\text{Co}(\text{en})_3]\text{Cl}_3$

(iii) $[\text{Co}(\text{NH}_3)_5(\text{NO}_2)](\text{NO}_3)_2$

(iv) $[\text{Pt}(\text{NH}_3)(\text{H}_2\text{O})\text{Cl}_2]$
- 9.4 Give evidence that $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{SO}_4$ and $[\text{Co}(\text{NH}_3)_5(\text{SO}_4)]\text{Cl}$ are ionisation isomers.

9. Coordination in Coordination Compounds

Werner was the first to describe the bonding features in coordination compounds. But his theory could not answer basic questions like:

(i) Why only certain elements possess the remarkable property of forming coordination compounds?

(ii) Why the bonds in coordination compounds have directional properties?

(iii) Why coordination compounds have characteristic magnetic and optical properties?

Many approaches have been put forth to explain the nature of bonding in coordination compounds viz. Valence Bond Theory (VBT), Crystal Field Theory (CFT), Ligand Field Theory (LFT) and Molecular Orbital Theory (MOT). We shall focus our attention on elementary treatment of the application of VBT and CFT to coordination compounds.

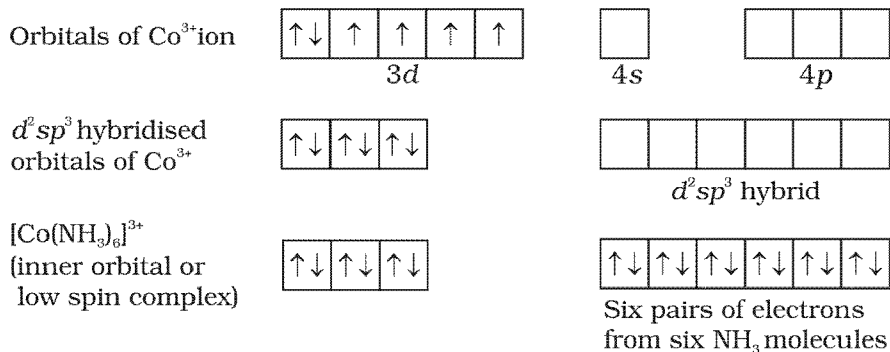
9.5.1 Valence Bond Theory

According to this theory, the metal atom or ion under the influence of ligands can use its $(n-1)d$, ns , np or ns , np , nd orbitals for hybridisation to yield a set of equivalent orbitals of definite geometry such as octahedral, tetrahedral, square planar and so on (Table 9.2). These hybridised orbitals are allowed to overlap with ligand orbitals that can donate electron pairs for bonding. This is illustrated by the following examples.

Table 9.2: Number of Orbitals and Types of Hybridisations

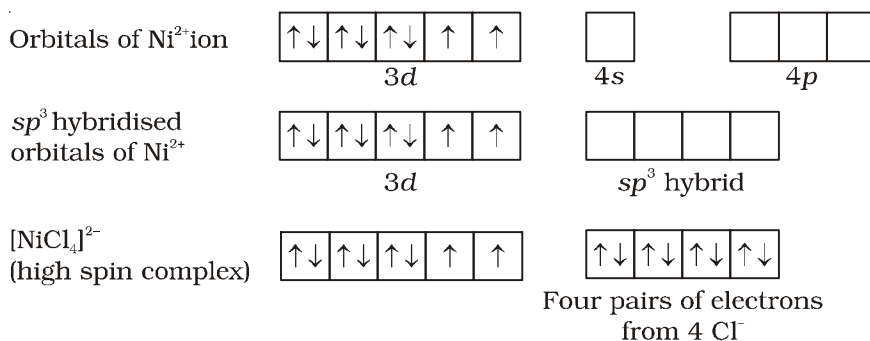
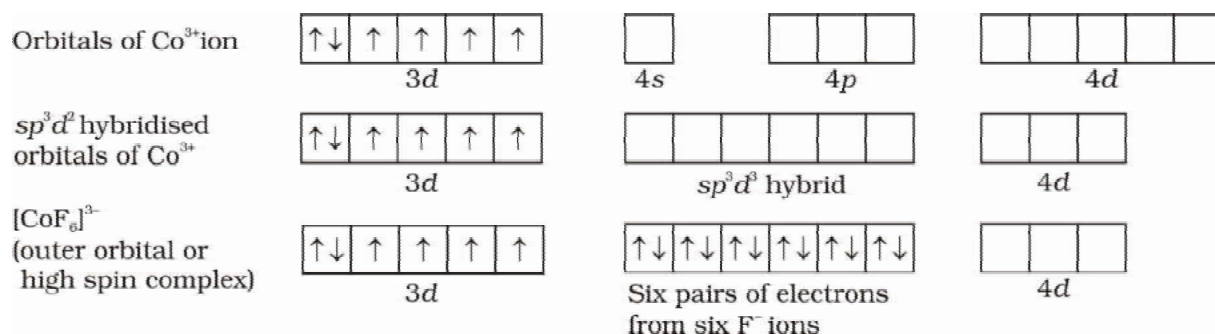
| Coordination number | Type of hybridisation | Distribution of hybrid orbitals in space |
|---------------------|-----------------------|--|
| 4 | sp^3 | Tetrahedral |
| 4 | dsp^2 | Square planar |
| 5 | sp^3d | Trigonal bipyramidal |
| 6 | sp^3d^2 | Octahedral |
| 6 | d^2sp^3 | Octahedral |

It is usually possible to predict the geometry of a complex from the knowledge of its magnetic behaviour on the basis of the valence bond theory.



In the diamagnetic octahedral complex, $[\text{Co}(\text{NH}_3)_6]^{3+}$, the cobalt ion is in +3 oxidation state and has the electronic configuration $3d^6$. The hybridisation scheme is as shown in diagram.

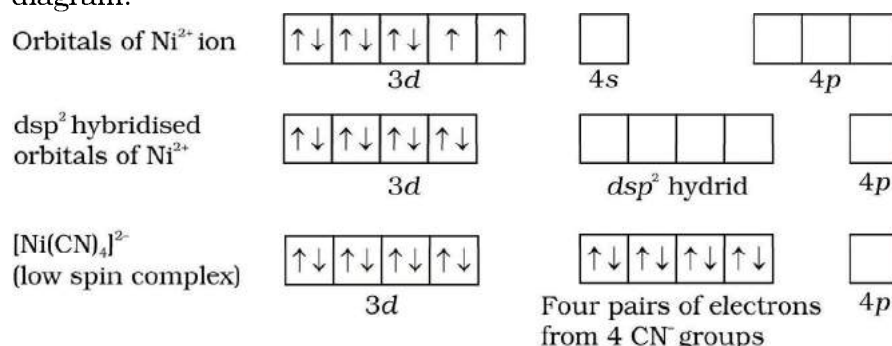
Six pairs of electrons, one from each NH_3 molecule, occupy the six hybrid orbitals. Thus, the complex has octahedral geometry and is diamagnetic because of the absence of unpaired electron. In the formation of this complex, since the inner d orbital ($3d$) is used in hybridisation, the complex, $[\text{Co}(\text{NH}_3)_6]^{3+}$ is called an **inner orbital** or **low spin** or **spin paired complex**. The paramagnetic octahedral complex, $[\text{CoF}_6]^{3-}$ uses outer orbital ($4d$) in hybridisation (sp^3d^2). It is thus called **outer orbital** or **high spin** or **spin free complex**. Thus:



In tetrahedral complexes one s and three p orbitals are hybridised to form four equivalent orbitals oriented tetrahedrally. This is illustrated below for $[\text{NiCl}_4]^{2-}$. Here nickel is in +2 oxidation state and the ion has the electronic configuration $3d^8$. The hybridisation scheme is as shown in diagram.

Each Cl^- ion donates a pair of electrons. The compound is paramagnetic since it contains two unpaired electrons. Similarly, $[\text{Ni}(\text{CO})_4]$ has tetrahedral geometry but is diamagnetic since nickel is in zero oxidation state and contains no unpaired electron.

In the square planar complexes, the hybridisation involved is dsp^2 . An example is $[\text{Ni}(\text{CN})_4]^{2-}$. Here nickel is in +2 oxidation state and has the electronic configuration $3d^8$. The hybridisation scheme is as shown in diagram:



Each of the hybridised orbitals receives a pair of electrons from a cyanide ion. The compound is diamagnetic as evident from the absence of unpaired electron.

It is important to note that the hybrid orbitals do not actually exist. In fact, hybridisation is a mathematical manipulation of wave equation for the atomic orbitals involved.

9.5.2 Magnetic Properties of Coordination Compounds

The magnetic moment of coordination compounds can be measured by the magnetic susceptibility experiments. The results can be used to obtain information about the structures adopted by metal complexes.

A critical study of the magnetic data of coordination compounds of metals of the first transition series reveals some complications. For metal ions with upto three electrons in the d orbitals, like Ti^{3+} (d^1); V^{3+} (d^2); Cr^{3+} (d^3); two vacant d orbitals are available for octahedral hybridisation with $4s$ and $4p$ orbitals. The magnetic behaviour of these free ions and their coordination entities is similar. When more than three $3d$ electrons are present, the required pair of $3d$ orbitals for octahedral hybridisation is not directly available (as a consequence of Hund's rule). Thus, for d^4 (Cr^{2+} , Mn^{3+}), d^5 (Mn^{2+} , Fe^{3+}), d^6 (Fe^{2+} , Co^{3+}) cases, a vacant pair of d orbitals results only by pairing of $3d$ electrons which leaves two, one and zero unpaired electrons, respectively.

The magnetic data agree with maximum spin pairing in many cases, especially with coordination compounds containing d^6 ions. However, with species containing d^4 and d^5 ions there are complications. $[\text{Mn}(\text{CN})_6]^{3-}$ has magnetic moment of two unpaired electrons while $[\text{MnCl}_6]^{3-}$ has a paramagnetic moment of four unpaired electrons. $[\text{Fe}(\text{CN})_6]^{3-}$ has magnetic moment of a single unpaired electron while $[\text{FeF}_6]^{3-}$ has a paramagnetic moment of five unpaired electrons. $[\text{CoF}_6]^{3-}$ is paramagnetic with four unpaired electrons while $[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$ is diamagnetic. This apparent anomaly is explained by valence bond theory in terms of formation of inner orbital and outer orbital coordination entities. $[\text{Mn}(\text{CN})_6]^{3-}$, $[\text{Fe}(\text{CN})_6]^{3-}$ and $[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$ are inner orbital complexes involving d^2sp^3 hybridisation, the former two complexes are paramagnetic and the latter diamagnetic. On the other hand, $[\text{MnCl}_6]^{3-}$, $[\text{FeF}_6]^{3-}$ and $[\text{CoF}_6]^{3-}$ are outer orbital complexes involving sp^3d^2 hybridisation and are paramagnetic corresponding to four, five and four unpaired electrons.

Example 9.

The spin only magnetic moment of $[\text{MnBr}_4]^{2-}$ is 5.9 BM. Predict the geometry of the complex ion ?

Solution

Since the coordination number of Mn^{2+} ion in the complex ion is 4, it will be either tetrahedral (sp^3 hybridisation) or square planar (dsp^2 hybridisation). But the fact that the magnetic moment of the complex ion is 5.9 BM, it should be tetrahedral in shape rather than square planar because of the presence of five unpaired electrons in the d orbitals.

9.5.3 Limitations of Valence Bond Theory

While the VB theory, to a larger extent, explains the formation, structures and magnetic behaviour of coordination compounds, it suffers from the following shortcomings:

- It involves a number of assumptions.
- It does not give quantitative interpretation of magnetic data.
- It does not explain the colour exhibited by coordination compounds.
- It does not give a quantitative interpretation of the thermodynamic or kinetic stabilities of coordination compounds.
- It does not make exact predictions regarding the tetrahedral and square planar structures of 4-coordinate complexes.
- It does not distinguish between weak and strong ligands.

9.5.4 Crystal Field Theory

The crystal field theory (CFT) is an electrostatic model which considers the metal-ligand bond to be ionic arising purely from electrostatic interactions between the metal ion and the ligand. Ligands are treated as point charges in case of anions or dipoles in case of neutral molecules. The five d orbitals in an isolated gaseous metal atom/ion have same energy, i.e., they are degenerate. This degeneracy is maintained if a spherically symmetrical field of negative charges surrounds the metal atom/ion. However, when this negative field is due to ligands (either anions or the negative ends of dipolar molecules like NH_3 and H_2O) in a complex, it becomes asymmetrical and the degeneracy of the d orbitals is lifted. It results in splitting of the d orbitals. The pattern of splitting depends upon the nature of the crystal field. Let us explain this splitting in different crystal fields.

(a) Crystal field splitting in octahedral coordination entities

In an octahedral coordination entity with six ligands surrounding the metal atom/ion, there will be repulsion between the electrons in metal d orbitals and the electrons (or negative charges) of the ligands. Such a repulsion is more when the metal d orbital is directed towards the ligand than when it is away from the ligand. Thus, the $d_{x^2-y^2}$ and d_{z^2} orbitals which point towards the axes along the direction of the ligand will experience more repulsion and will be raised in energy; and the d_{xy} , d_{yz} and d_{zx} orbitals which are directed between the axes will be lowered in energy relative to the average energy in the spherical crystal field. Thus, the degeneracy of the d orbitals has been removed due to ligand electron-metal electron repulsions in the octahedral complex to yield three orbitals of lower energy, t_{2g} set and two orbitals of higher energy, e_g set. This splitting of the

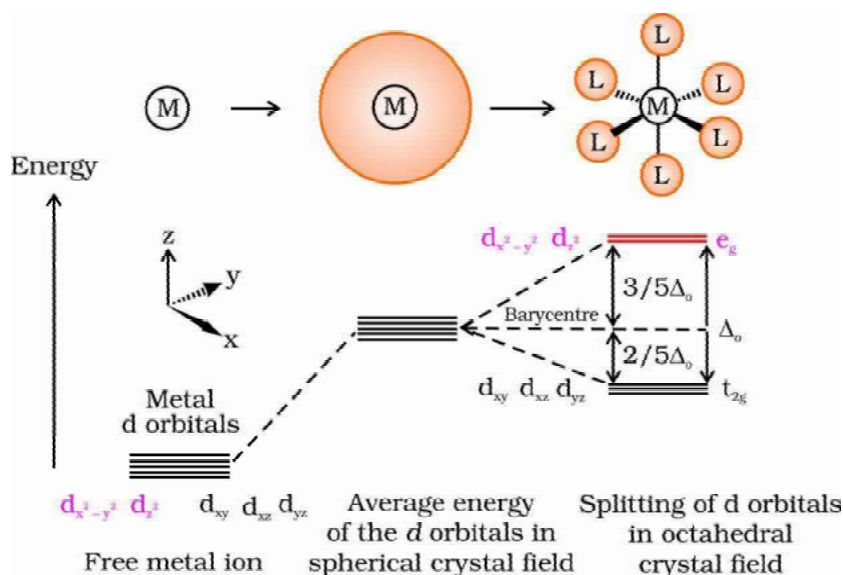
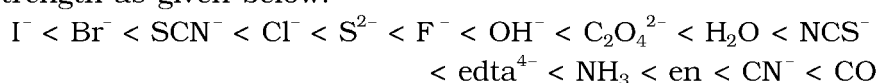


Fig.9.8: *d* orbital splitting in an octahedral crystal field

degenerate levels due to the presence of ligands in a definite geometry is termed as **crystal field splitting** and the energy separation is denoted by Δ_o (the subscript o is for octahedral) (Fig.9.8). Thus, the energy of the two e_g orbitals will increase by $(3/5) \Delta_o$ and that of the three t_{2g} will decrease by $(2/5) \Delta_o$.

The crystal field splitting, Δ_o , depends upon the field produced by the ligand and charge on the metal ion. Some ligands are able to produce strong fields in which case, the splitting will be large whereas others produce weak fields and consequently result in small splitting of *d* orbitals. In

general, ligands can be arranged in a series in the order of increasing field strength as given below:



Such a series is termed as **spectrochemical series**. It is an experimentally determined series based on the absorption of light by complexes with different ligands. Let us assign electrons in the *d* orbitals of metal ion in octahedral coordination entities. Obviously, the single *d* electron occupies one of the lower energy t_{2g} orbitals. In d^2 and d^3 coordination entities, the *d* electrons occupy the t_{2g} orbitals singly in accordance with the Hund's rule. For d^4 ions, two possible patterns of electron distribution arise: (i) the fourth electron could either enter the t_{2g} level and pair with an existing electron, or (ii) it could avoid paying the price of the pairing energy by occupying the e_g level. Which of these possibilities occurs, depends on the relative magnitude of the crystal field splitting, Δ_o and the pairing energy, *P* (*P* represents the energy required for electron pairing in a single orbital). The two options are:

- (i) If $\Delta_o < P$, the fourth electron enters one of the e_g orbitals giving the configuration $t_{2g}^3 e_g^1$. Ligands for which $\Delta_o < P$ are known as *weak field ligands* and form high spin complexes.
- (ii) If $\Delta_o > P$, it becomes more energetically favourable for the fourth electron to occupy a t_{2g} orbital with configuration $t_{2g}^4 e_g^0$. Ligands which produce this effect are known as *strong field ligands* and form low spin complexes.

Calculations show that d^4 to d^7 coordination entities are more stable for strong field as compared to weak field cases.

(b) Crystal field splitting in tetrahedral coordination entities

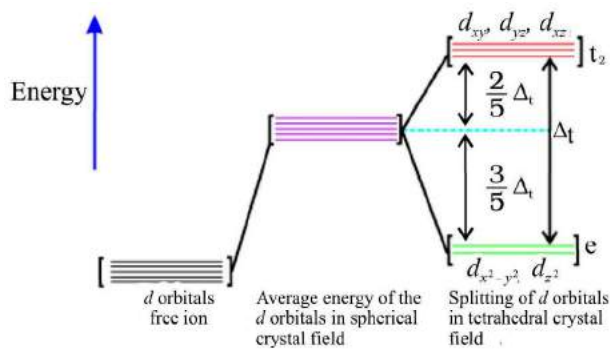


Fig.9.9: d orbital splitting in a tetrahedral crystal field.

In tetrahedral coordination entity formation, the *d* orbital splitting (Fig. 9.9) is inverted and is smaller as compared to the octahedral field splitting. For the same metal, the same ligands and metal-ligand distances, it can be shown that $\Delta_t = (4/9) \Delta_o$. Consequently, the orbital splitting energies are not sufficiently large for forcing pairing and, therefore, low spin configurations are rarely observed.

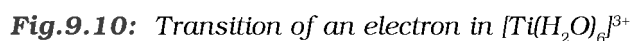
9.5.5 Colour in Coordination Compounds

In the previous Unit, we learnt that one of the most distinctive properties of transition metal complexes is their wide range of colours. This means that some of the visible spectrum is being removed from white light as it passes through the sample, so the light that emerges is no longer white. The colour of the complex is complementary to that which is absorbed. The complementary colour is the colour generated from the wavelength left over; if green light is absorbed by the complex, it appears red. Table 9.3 gives the relationship of the different wavelength absorbed and the colour observed.

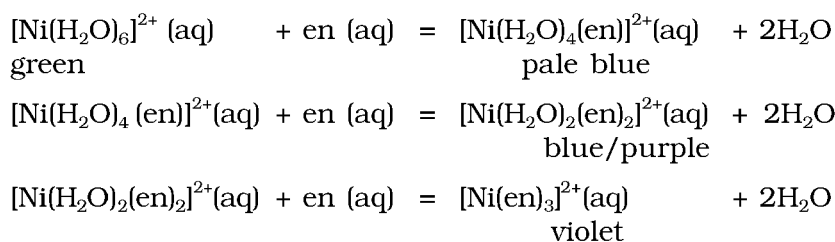
Table 9.3: Relationship between the Wavelength of Light absorbed and the Colour observed in some Coordination Entities

| Coordination entity | Wavelength of light absorbed (nm) | Colour of light absorbed | Colour of coordination entity |
|--|-----------------------------------|--------------------------|-------------------------------|
| [CoCl(NH ₃) ₅] ²⁺ | 535 | Yellow | Violet |
| [Co(NH ₃) ₅ (H ₂ O)] ³⁺ | 500 | Blue Green | Red |
| [Co(NH ₃) ₆] ³⁺ | 475 | Blue | Yellow Orange |
| [Co(CN) ₆] ³⁻ | 310 | Ultraviolet | Pale Yellow |
| [Cu(H ₂ O) ₄] ²⁺ | 600 | Red | Blue |
| [Ti(H ₂ O) ₆] ³⁺ | 498 | Blue Green | Violet |

The colour in the coordination compounds can be readily explained in terms of the crystal field theory. Consider, for example, the complex [Ti(H₂O)₆]³⁺, which is violet in colour. This is an octahedral complex where the single electron (Ti³⁺ is a 3*d*¹ system) in the metal *d* orbital is in the *t*_{2g} level in the ground state of the complex. The next higher state available for the electron is the empty *e*_g level. If light corresponding to the energy of blue-green region is absorbed by the complex, it would excite the electron from *t*_{2g} level to the *e*_g level (*t*_{2g}¹*e*_g⁰ → *t*_{2g}⁰*e*_g¹). Consequently, the complex appears violet in colour (Fig. 9.10). The crystal field theory attributes the colour of the coordination compounds to *d-d* transition of the electron.



of a complex may be illustrated by considering the $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$ complex, which forms when nickel(II) chloride is dissolved in water. If the didentate ligand, ethane-1,2-diamine(en) is progressively added in the molar ratios en:Ni, 1:1, 2:1, 3:1, the following series of reactions and their associated colour changes occur:



This sequence is shown in Fig. 9.11.

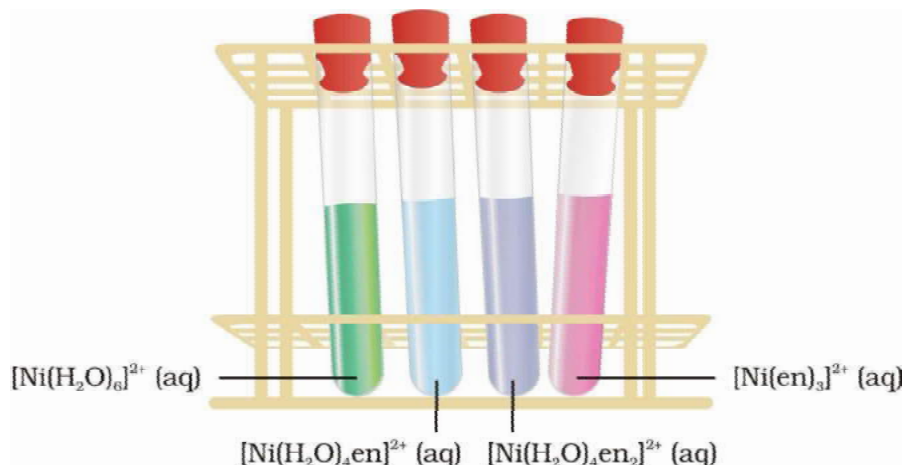


Fig.9.11
Aqueous solutions of
complexes of
nickel(II) with an
increasing number of
ethane-1,
2-diamine ligands.

Colour of Some Gem Stones

The colours produced by electronic transitions within the d orbitals of a transition metal ion occur frequently in everyday life. Ruby [Fig.9.12(a)] is aluminium oxide (Al_2O_3) containing about 0.5-1% Cr^{3+} ions (d^3), which are randomly distributed in positions normally occupied by Al^{3+} . We may view these chromium(III) species as octahedral chromium(III) complexes incorporated into the alumina lattice; $d-d$ transitions at these centres give rise to the colour.

In emerald [Fig.9.12(b)], Cr^{3+} ions occupy octahedral sites in the mineral beryl ($\text{Be}_3\text{Al}_2\text{Si}_6\text{O}_{18}$). The absorption bands seen in the ruby shift to longer wavelength, namely yellow-red and blue, causing emerald to transmit light in the green region.

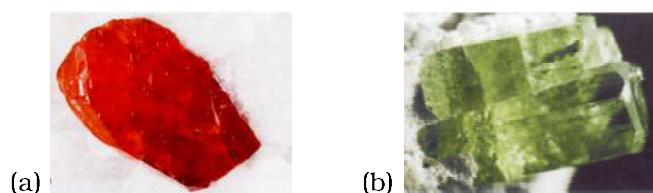


Fig.9.12: (a) Ruby: this gemstone was found in marble from Mogok, Myanmar; (b) Emerald: this gemstone was found in Muzo, Columbia.

9.5.6 Limitations of Crystal Field Theory

The crystal field model is successful in explaining the formation, structures, colour and magnetic properties of coordination compounds to a large extent. However, from the assumptions that the ligands are point charges, it follows that anionic ligands should exert the greatest splitting effect. The anionic ligands actually are found at the low end of the spectrochemical series. Further, it does not take into account the covalent character of bonding between the ligand and the central atom. These are some of the weaknesses of CFT, which are explained by ligand field theory (LFT) and molecular orbital theory which are beyond the scope of the present study.

Inte Questions

- 9.5 Explain on the basis of valence bond theory that $[\text{Ni}(\text{CN})_4]^{2-}$ ion with square planar structure is diamagnetic and the $[\text{NiCl}_4]^{2-}$ ion with tetrahedral geometry is paramagnetic.
- 9.6 $[\text{NiCl}_4]^{2-}$ is paramagnetic while $[\text{Ni}(\text{CO})_4]$ is diamagnetic though both are tetrahedral. Why?
- 9.7 $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ is strongly paramagnetic whereas $[\text{Fe}(\text{CN})_6]^{3-}$ is weakly paramagnetic. Explain.
- 9.8 Explain $[\text{Co}(\text{NH}_3)_6]^{3+}$ is an inner orbital complex whereas $[\text{Ni}(\text{NH}_3)_6]^{2+}$ is an outer orbital complex.
- 9.9 Predict the number of unpaired electrons in the square planar $[\text{Pt}(\text{CN})_4]^{2-}$ ion.
- 9.10 The hexaquo manganese(II) ion contains five unpaired electrons, while the hexacyanoion contains only one unpaired electron. Explain using Crystal Field Theory.

9. Coordination in Metal Carbonyls

The homoleptic carbonyls (compounds containing carbonyl ligands only) are formed by most of the transition metals. These carbonyls have simple, well defined structures. Tetracarbonylnickel(0) is tetrahedral, pentacarbonyliron(0) is trigonalbipyramidal while hexacarbonyl chromium(0) is octahedral.

Decacarbonyldimanganese(0) is made up of two square pyramidal $\text{Mn}(\text{CO})_5$ units joined by a Mn – Mn bond. Octacarbonyldicobalt(0) has a Co – Co bond bridged by two CO groups (Fig.9.13).

Fig. 9.13
Structures of some
representative
homoleptic metal
carbonyls.

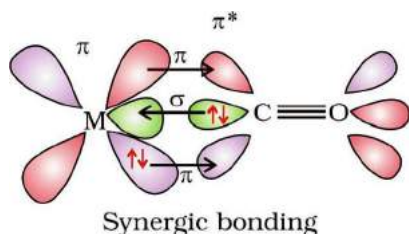
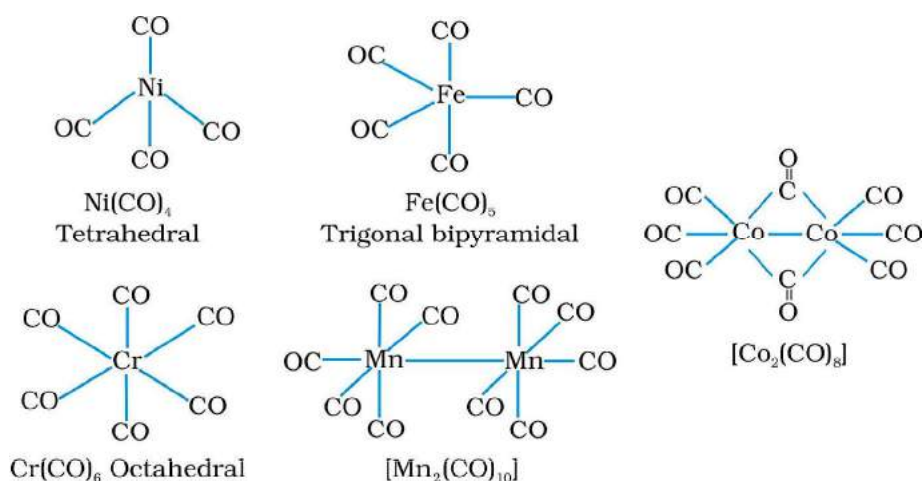
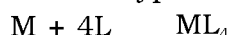


Fig. 9.14: Example of synergic bonding
interactions in a carbonyl complex.

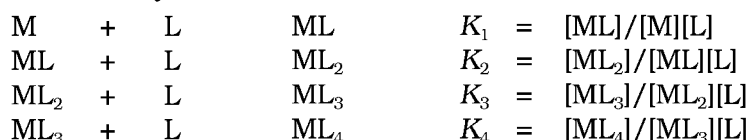
The metal-carbon bond in metal carbonyls possess both σ and π character. The M–C σ bond is formed by the donation of lone pair of electrons on the carbonyl carbon into a vacant orbital of the metal. The M–C π bond is formed by the donation of a pair of electrons from a filled d orbital of metal into the vacant antibonding π^* orbital of carbon monoxide. The metal to ligand bonding creates a synergic effect which strengthens the bond between CO and the metal (Fig.9.14).

9. Stability of Coordination Compounds

The stability of a complex in solution refers to the degree of association between the two species involved in the state of equilibrium. The magnitude of the (stability or formation) equilibrium constant for the association, quantitatively expresses the stability. Thus, if we have a reaction of the type:



then the larger the stability constant, the higher the proportion of ML_4 that exists in solution. Free metal ions rarely exist in the solution so that M will usually be surrounded by solvent molecules which will compete with the ligand molecules, L, and be successively replaced by them. For simplicity, we generally ignore these solvent molecules and write four stability constants as follows:



where K_1 , K_2 , etc., are referred to as **stepwise stability constants**. Alternatively, we can write the **overall stability constant** thus:

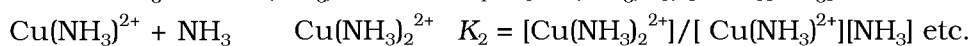


The stepwise and overall stability constant are therefore related as follows:

$$\beta_4 = K_1 \times K_2 \times K_3 \times K_4 \text{ or more generally,}$$

$$\beta_n = K_1 \times K_2 \times K_3 \times K_4 \dots\dots K_n$$

If we take as an example, the steps involved in the formation of the cuprammonium ion, we have the following:



where K_1 , K_2 are the stepwise stability constants and overall stability constant.

$$\text{Also } \beta_4 = [\text{Cu}(\text{NH}_3)_4^{2+}]/[\text{Cu}^{2+}][\text{NH}_3]^4$$

The addition of the four amine groups to copper shows a pattern found for most formation constants, in that the successive stability constants decrease. In this case, the four constants are:

$$\log K_1 = 4.0, \log K_2 = 3.2, \log K_3 = 2.7, \log K_4 = 2.0 \text{ or } \log \beta_4 = 11.9$$

The **instability constant or the dissociation constant** of coordination compounds is defined as the reciprocal of the formation constant.

Inte t Question

9.11 Calculate the overall complex dissociation equilibrium constant for the $\text{Cu}(\text{NH}_3)_4^{2+}$ ion, given that β_4 for this complex is 2.1×10^{13} .

9. Importance and Applications of Coordination Compounds

The coordination compounds are of great importance. These compounds are widely present in the mineral, plant and animal worlds and are known to play many important functions in the area of analytical chemistry, metallurgy, biological systems, industry and medicine. These are described below:

- Coordination compounds find use in many qualitative and quantitative chemical analysis. The familiar colour reactions given by metal ions with a number of ligands (especially chelating ligands), as a result of formation of coordination entities, form the basis for their detection and estimation by classical and instrumental methods of analysis. Examples of such reagents include EDTA, DMG (dimethylglyoxime), α -nitroso- β -naphthol, cupron, etc.
- Hardness of water is estimated by simple titration with Na_2EDTA . The Ca^{2+} and Mg^{2+} ions form stable complexes with EDTA. The selective estimation of these ions can be done due to difference in the stability constants of calcium and magnesium complexes.
- Some important extraction processes of metals, like those of silver and gold, make use of complex formation. Gold, for example, combines with cyanide in the presence of oxygen and water to form the coordination entity $[\text{Au}(\text{CN})_2]^-$ in aqueous solution. Gold can be separated in metallic form from this solution by the addition of zinc (Unit 6).
- Similarly, purification of metals can be achieved through formation and subsequent decomposition of their coordination compounds. For example, impure nickel is converted to $[\text{Ni}(\text{CO})_4]$, which is decomposed to yield pure nickel.

- Coordination compounds are of great importance in biological systems. The pigment responsible for photosynthesis, chlorophyll, is a coordination compound of magnesium. Haemoglobin, the red pigment of blood which acts as oxygen carrier is a coordination compound of iron. Vitamin B₁₂, cyanocobalamin, the anti-pernicious anaemia factor, is a coordination compound of cobalt. Among the other compounds of biological importance with coordinated metal ions are the enzymes like, carboxypeptidase A and carbonic anhydrase (catalysts of biological systems).
- Coordination compounds are used as catalysts for many industrial processes. Examples include rhodium complex, $[(\text{Ph}_3\text{P})_3\text{RhCl}]$, a Wilkinson catalyst, is used for the hydrogenation of alkenes.
- Articles can be electroplated with silver and gold much more smoothly and evenly from solutions of the complexes, $[\text{Ag}(\text{CN})_2]^-$ and $[\text{Au}(\text{CN})_2]^-$ than from a solution of simple metal ions.
- In black and white photography, the developed film is fixed by washing with hypo solution which dissolves the undecomposed AgBr to form a complex ion, $[\text{Ag}(\text{S}_2\text{O}_3)_2]^{3-}$.
- There is growing interest in the use of chelate therapy in medicinal chemistry. An example is the treatment of problems caused by the presence of metals in toxic proportions in plant/animal systems. Thus, excess of copper and iron are removed by the chelating ligands D-penicillamine and desferrioxime B via the formation of coordination compounds. EDTA is used in the treatment of lead poisoning. Some coordination compounds of platinum effectively inhibit the growth of tumours. Examples are: *cis-platin* and related compounds.

Summary

The **chemistry of coordination compounds** is an important and challenging area of modern inorganic chemistry. During the last fifty years, advances in this area, have provided development of new concepts and models of bonding and molecular structure, novel breakthroughs in **chemical industry** and vital insights into the functioning of critical components of **biological systems**.

The first systematic attempt at explaining the formation, reactions, structure and bonding of a coordination compound was made by **A. Werner**. His theory postulated the use of two types of **linkages (primary and secondary)** by a metal atom/ion in a coordination compound. In the modern language of chemistry these linkages are recognised as the ionisable (ionic) and non-ionisable (covalent) bonds, respectively. Using the property of isomerism, Werner predicted the geometrical shapes of a large number of coordination entities.

The Valence Bond Theory (VBT) explains with reasonable success, the formation, magnetic behaviour and geometrical shapes of coordination compounds. It, however, fails to provide a quantitative interpretation of magnetic behaviour and has nothing to say about the optical properties of these compounds.

The Crystal Field Theory (CFT) to coordination compounds is based on the effect of different crystal fields (provided by the ligands taken as point charges), on the degeneracy of *d* orbital energies of the central metal atom/ion. The splitting of the *d* orbitals provides different electronic arrangements in strong and weak crystal fields. The treatment provides for quantitative estimations of orbital separation energies, magnetic moments and spectral and stability

parameters. However, the assumption that ligands constitute point charges creates many theoretical difficulties.

The metal–carbon bond in **metal carbonyls** possesses both σ and π character. The ligand to metal is σ bond and metal to ligand is π bond. This unique synergic bonding provides stability to metal carbonyls.

The stability of coordination compounds is measured in terms of **stepwise stability (or formation) constant (K) or overall stability constant (β)**. The stabilisation of coordination compound due to chelation is called the **chelate effect**. The stability of coordination compounds is related to Gibbs energy, enthalpy and entropy terms.

Coordination compounds are of great importance. These compounds provide critical insights into the functioning and structures of vital components of biological systems. Coordination compounds also find extensive applications in **metallurgical processes, analytical and medicinal chemistry**.

Exercises

- 9.1** Explain the bonding in coordination compounds in terms of Werner's postulates.
- 9.2** FeSO_4 solution mixed with $(\text{NH}_4)_2\text{SO}_4$ solution in 1:1 molar ratio gives the test of Fe^{2+} ion but CuSO_4 solution mixed with aqueous ammonia in 1:4 molar ratio does not give the test of Cu^{2+} ion. Explain why?
- 9.3** Explain with two examples each of the following: coordination entity, ligand, coordination number, coordination polyhedron, homoleptic and heteroleptic.
- 9.4** What is meant by unidentate, didentate and ambidentate ligands? Give two examples for each.
- 9.5** Specify the oxidation numbers of the metals in the following coordination entities:
(i) $[\text{Co}(\text{H}_2\text{O})(\text{CN})(\text{en})_2]^{2+}$ (iii) $[\text{PtCl}_4]^{2-}$ (v) $[\text{Cr}(\text{NH}_3)_3\text{Cl}_3]$
(ii) $[\text{CoBr}_2(\text{en})_2]^+$ (iv) $\text{K}_3[\text{Fe}(\text{CN})_6]$
- 9.6** Using IUPAC norms write the formulas for the following:
(i) Tetrahydroxidozincate(II) (vi) Hexaamminecobalt(III) sulphate
(ii) Potassium tetrachloridopalladate(II) (vii) Potassium tri(oxalato)chromate(III)
(iii) Diamminedichloridoplatinum(II) (viii) Hexaammineplatinum(IV)
(iv) Potassium tetracyanonickelate(II) (ix) Tetrabromidocuprate(II)
(v) Pentaamminenitrito-O-cobalt(III) (x) Pentaamminenitrito-N-cobalt(III)
- 9.7** Using IUPAC norms write the systematic names of the following:
(i) $[\text{Co}(\text{NH}_3)_6]\text{Cl}_3$ (iv) $[\text{Co}(\text{NH}_3)_4\text{Cl}(\text{NO}_2)]\text{Cl}$ (vii) $[\text{Ni}(\text{NH}_3)_6]\text{Cl}_2$
(ii) $[\text{Pt}(\text{NH}_3)_2\text{Cl}(\text{NH}_2\text{CH}_3)]\text{Cl}$ (v) $[\text{Mn}(\text{H}_2\text{O})_6]^{2+}$ (viii) $[\text{Co}(\text{en})_3]^{3+}$
(iii) $[\text{Ti}(\text{H}_2\text{O})_6]^{3+}$ (vi) $[\text{NiCl}_4]^{2-}$ (ix) $[\text{Ni}(\text{CO})_4]$
- 9.8** List various types of isomerism possible for coordination compounds, giving an example of each.
- 9.9** How many geometrical isomers are possible in the following coordination entities?
(i) $[\text{Cr}(\text{C}_2\text{O}_4)_3]^{3-}$ (ii) $[\text{Co}(\text{NH}_3)_3\text{Cl}_3]$
- 9.10** Draw the structures of optical isomers of:
(i) $[\text{Cr}(\text{C}_2\text{O}_4)_3]^{3-}$ (ii) $[\text{PtCl}_2(\text{en})_2]^{2+}$ (iii) $[\text{Cr}(\text{NH}_3)_2\text{Cl}_2(\text{en})]^+$

- 9.11** Draw all the isomers (geometrical and optical) of:
 (i) $[\text{CoCl}_2(\text{en})_2]^+$ (ii) $[\text{Co}(\text{NH}_3)\text{Cl}(\text{en})_2]^{2+}$ (iii) $[\text{Co}(\text{NH}_3)_2\text{Cl}_2(\text{en})]^+$
- 9.12** Write all the geometrical isomers of $[\text{Pt}(\text{NH}_3)(\text{Br})(\text{Cl})(\text{py})]$ and how many of these will exhibit optical isomers?
- 9.13** Aqueous copper sulphate solution (blue in colour) gives:
 (i) a green precipitate with aqueous potassium fluoride and
 (ii) a bright green solution with aqueous potassium chloride. Explain these experimental results.
- 9.14** What is the coordination entity formed when excess of aqueous KCN is added to an aqueous solution of copper sulphate? Why is it that no precipitate of copper sulphide is obtained when $\text{H}_2\text{S}(\text{g})$ is passed through this solution?
- 9.15** Discuss the nature of bonding in the following coordination entities on the basis of valence bond theory:
 (i) $[\text{Fe}(\text{CN})_6]^{4-}$ (ii) $[\text{FeF}_6]^{3-}$ (iii) $[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$ (iv) $[\text{CoF}_6]^{3-}$
- 9.16** Draw figure to show the splitting of d orbitals in an octahedral crystal field.
- 9.17** What is spectrochemical series? Explain the difference between a weak field ligand and a strong field ligand.
- 9.18** What is crystal field splitting energy? How does the magnitude of Δ_o decide the actual configuration of d orbitals in a coordination entity?
- 9.19** $[\text{Cr}(\text{NH}_3)_6]^{3+}$ is paramagnetic while $[\text{Ni}(\text{CN})_4]^{2-}$ is diamagnetic. Explain why?
- 9.20** A solution of $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$ is green but a solution of $[\text{Ni}(\text{CN})_4]^{2-}$ is colourless. Explain.
- 9.21** $[\text{Fe}(\text{CN})_6]^{4-}$ and $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$ are of different colours in dilute solutions. Why?
- 9.22** Discuss the nature of bonding in metal carbonyls.
- 9.23** Give the oxidation state, d orbital occupation and coordination number of the central metal ion in the following complexes:
 (i) $\text{K}_3[\text{Co}(\text{C}_2\text{O}_4)_3]$ (iii) $(\text{NH}_4)_2[\text{CoF}_4]$
 (ii) $\text{cis-}[\text{CrCl}_2(\text{en})_2]\text{Cl}$ (iv) $[\text{Mn}(\text{H}_2\text{O})_6]\text{SO}_4$
- 9.24** Write down the IUPAC name for each of the following complexes and indicate the oxidation state, electronic configuration and coordination number. Also give stereochemistry and magnetic moment of the complex:
 (i) $\text{K}[\text{Cr}(\text{H}_2\text{O})_2(\text{C}_2\text{O}_4)_2] \cdot 3\text{H}_2\text{O}$ (iii) $[\text{CrCl}_3(\text{py})_3]$ (v) $\text{K}_4[\text{Mn}(\text{CN})_6]$
 (ii) $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$ (iv) $\text{Cs}[\text{FeCl}_4]$
- 9.25** What is meant by stability of a coordination compound in solution? State the factors which govern stability of complexes.
- 9.26** What is meant by the *chelate effect*? Give an example.
- 9.27** Discuss briefly giving an example in each case the role of coordination compounds in:
 (i) biological systems (iii) analytical chemistry
 (ii) medicinal chemistry and (iv) extraction/metallurgy of metals.
- 9.28** How many ions are produced from the complex $\text{Co}(\text{NH}_3)_6\text{Cl}_2$ in solution?
 (i) 6 (ii) 4 (iii) 3 (iv) 2
- 9.29** Amongst the following ions which one has the highest magnetic moment value?
 (i) $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$ (ii) $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$ (iii) $[\text{Zn}(\text{H}_2\text{O})_6]^{2+}$
- 9.30** The oxidation number of cobalt in $\text{K}[\text{Co}(\text{CO})_4]$ is
 (i) +1 (ii) +3 (iii) -1 (iv) -3

- 9.31** Amongst the following, the most stable complex is
 (i) $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ (ii) $[\text{Fe}(\text{NH}_3)_6]^{3+}$ (iii) $[\text{Fe}(\text{C}_2\text{O}_4)_3]^{3-}$ (iv) $[\text{FeCl}_6]^{3-}$
- 9.32** What will be the correct order for the wavelengths of absorption in the visible region for the following:
 $[\text{Ni}(\text{NO}_2)_6]^{4-}$, $[\text{Ni}(\text{NH}_3)_6]^{2+}$, $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$?

Answers to Some Intext Questions

- 9.1** (i) $[\text{Co}(\text{NH}_3)_4(\text{H}_2\text{O})_2]\text{Cl}_3$ (iv) $[\text{Pt}(\text{NH}_3)\text{BrCl}(\text{NO}_2)]^-$
 (ii) $\text{K}_2[\text{Ni}(\text{CN})_4]$ (v) $[\text{PtCl}_2(\text{en})_2](\text{NO}_3)_2$
 (iii) $[\text{Cr}(\text{en})_3]\text{Cl}_3$ (vi) $\text{Fe}_4[\text{Fe}(\text{CN})_6]_3$
- 9.2** (i) Hexaamminecobalt(III) chloride
 (ii) Pentaamminechloridocobalt(III) chloride
 (iii) Potassium hexacyanidoferrate(III)
 (iv) Potassium trioxalatoferrate(III)
 (v) Potassium tetrachloridopalladate(II)
 (vi) Diamminechlorido(methanamine)platinum(II) chloride
- 9.3** (i) Both geometrical (*cis*-, *trans*-) and optical isomers for *cis* can exist.
 (ii) Two optical isomers can exist.
 (iii) There are 10 possible isomers. (Hint: There are geometrical, ionisation and linkage isomers possible).
 (iv) Geometrical (*cis*-, *trans*-) isomers can exist.
- 9.4** The ionisation isomers dissolve in water to yield different ions and thus react differently to various reagents:
 $[\text{Co}(\text{NH}_3)_5\text{Br}]\text{SO}_4 + \text{Ba}^{2+} \rightarrow \text{BaSO}_4 (\text{s})$
 $[\text{Co}(\text{NH}_3)_5\text{SO}_4]\text{Br} + \text{Ba}^{2+} \rightarrow \text{No reaction}$
 $[\text{Co}(\text{NH}_3)_5\text{Br}]\text{SO}_4 + \text{Ag}^+ \rightarrow \text{No reaction}$
 $[\text{Co}(\text{NH}_3)_5\text{SO}_4]\text{Br} + \text{Ag}^+ \rightarrow \text{AgBr} (\text{s})$
- 9.6** In $\text{Ni}(\text{CO})_4$, Ni is in zero oxidation state whereas in NiCl_4^{2-} , it is in +2 oxidation state. In the presence of CO ligand, the unpaired *d* electrons of Ni pair up but Cl⁻ being a weak ligand is unable to pair up the unpaired electrons.
- 9.7** In presence of CN⁻, (a strong ligand) the 3*d* electrons pair up leaving only one unpaired electron. The hybridisation is d^2sp^3 forming inner orbital complex. In the presence of H₂O, (a weak ligand), 3*d* electrons do not pair up. The hybridisation is sp^3d^2 forming an outer orbital complex containing five unpaired electrons, it is strongly paramagnetic.
- 9.8** In the presence of NH₃, the 3*d* electrons pair up leaving two *d* orbitals empty to be involved in d^2sp^3 hybridisation forming inner orbital complex in case of $[\text{Co}(\text{NH}_3)_6]^{3+}$.
 In $[\text{Ni}(\text{NH}_3)_6]^{2+}$, Ni is in +2 oxidation state and has d^8 configuration, the hybridisation involved is sp^3d^2 forming outer orbital complex.
- 9.9** For square planar shape, the hybridisation is dsp^2 . Hence the unpaired electrons in 5*d* orbital pair up to make one *d* orbital empty for dsp^2 hybridisation. Thus there is no unpaired electron.
- 9.11** The overall dissociation constant is the reciprocal of overall stability constant i.e. $1/\beta_4 = 4.7 \times 10^{-14}$

Answers to Some Questions in Exercises

UNIT 1

- 1.11** 106.57 u
1.13 143.1 pm
1.15 8.97 g cm^{-3}
1.16 $\text{Ni}^{2+} = 96\%$ and $\text{Ni}^{3+} = 4\%$
1.24 (i) 354 pm (ii) 2.26×10^{22} unit cells
1.25 6.02×10^{18} cation vacancies mol^{-1}

UNIT 2

- | | |
|---|--|
| 2.4 16.23 M | 2.5 0.617 m, 0.01 and 0.99, 0.67 |
| 2.6 157.8 mL | 2.7 33.5% |
| 2.8 17.95 m and 9.10 M | 2.9 $1.5 \times 10^{-3}\%$, 1.25×10^{-4} m |
| 2.15 $40.907 \text{ g mol}^{-1}$ | 2.16 73.58 kPa |
| 2.17 12.08 kPa | 2.18 10 g |
| 2.19 23 g mol^{-1} , 3.53 kPa | 2.20 269.07 K |
| 2.21 A = 25.58 u and B = 42.64 u | 2.22 0.061 M |
| 2.24 KCl, CH_3OH , CH_3CN , Cyclohexane | |
| 2.25 Toluene, chloroform; Phenol, Pentanol; Formic acid, ethylene glycol | |
| 2.26 5 m | 2.27 2.45×10^{-8} M |
| 2.28 1.424% | 2.29 3.2 g of water |
| 2.30 4.575 g | 2.32 0.65^0 |
| 2.33 $i = 1.0753$, $K_a = 3.07 \times 10^{-3}$ | 2.34 17.44 mm Hg |
| 2.35 178×10^{-5} | 2.36 280.7 torr, 32 torr |
| 2.38 0.6 and 0.4 | 2.39 $x(\text{O}_2) 4.6 \times 10^{-5}$, $x(\text{N}_2) 9.22 \times 10^{-5}$ |
| 2.40 0.03 mol of CaCl_2 | 2.41 5.27×10^{-3} atm. |

UNIT 3

- 3.4** (i) $E^\circ = 0.34\text{V}$, $\Delta_r G^\circ = -196.86 \text{ kJ mol}^{-1}$, $K = 3.124 \times 10^{34}$
(ii) $E^\circ = 0.03\text{V}$, $\Delta_r G^\circ = -2.895 \text{ kJ mol}^{-1}$, $K = 3.2$
3.5 (i) 2.68 V, (ii) 0.53 V, (iii) 0.08 V, (iv) -1.298 V
3.6 1.56 V
3.8 $124.0 \text{ S cm}^2 \text{ mol}^{-1}$
3.9 0.219 cm^{-1}
3.11 1.85×10^{-5}
3.12 3F, 2F, 5F
3.13 1F, 4.44F
3.14 2F, 1F
3.15 1.8258g
3.16 14.40 min, Copper 0.427g, Zinc 0.437 g

UNIT 4

- 4.2 (i) $8.0 \times 10^{-9} \text{ mol L}^{-1} \text{ s}^{-1}$; $3.89 \times 10^{-9} \text{ mol L}^{-1} \text{ s}^{-1}$
- 4.4 $\text{bar}^{-1/2} \text{ s}^{-1}$
- 4.6 (i) 4 times (ii) $\frac{1}{4}$ times
- 4.8 (i) $4.67 \times 10^{-3} \text{ mol L}^{-1} \text{ s}^{-1}$ (ii) $1.98 \times 10^{-2} \text{ s}^{-1}$
- 4.9 (i) $\text{rate} = k[A][B]^2$ (ii) 9 times
- 4.10 Orders with respect to A is 1.5 and order with respect to B is zero.
- 4.11 $\text{rate law} = k[A][B]^2$; $\text{rate constant} = 6.0 \text{ M}^{-2} \text{ min}^{-1}$
- 4.13 (i) $3.47 \times 10^{-3} \text{ seconds}$ (ii) 0.35 minutes (iii) 0.173 years
- 4.14 1845 years 4.16 $4.6 \times 10^{-2} \text{ s}$
- 4.17 $0.7814 \mu\text{g}$ and $0.227 \mu\text{g}$. 4.19 77.7 minutes
- 4.20 $2.20 \times 10^{-3} \text{ s}^{-1}$ 4.21 $2.23 \times 10^{-3} \text{ s}^{-1}$, $7.8 \times 10^{-4} \text{ atm s}^{-1}$
- 4.23 $3.9 \times 10^{12} \text{ s}^{-1}$ 4.24 0.135 M
- 4.25 0.158 M 4.26 $232.79 \text{ kJ mol}^{-1}$
- 4.27 $239.339 \text{ kJ mol}^{-1}$ 4.28 24°C
- 4.29 $E_a = 76.750 \text{ kJ mol}^{-1}$, $k = 0.9965 \times 10^{-2} \text{ s}^{-1}$
- 4.30 52.8 kJ mol^{-1}

UNIT 6

- 6.1 Zinc is highly reactive metal, it may not be possible to replace it from a solution of ZnSO_4 so easily.
- 6.2 It prevents one of the components from forming the froth by complexation.
- 6.3 The Gibbs energies of formation of most sulphides are greater than that for CS_2 . In fact, CS_2 is an endothermic compound. Hence it is common practice to roast sulphide ores to corresponding oxides prior to reduction.
- 6.5 CO
- 6.6 Selenium, tellurium, silver, gold are the metals present in anode mud. This is because these are less reactive than copper.
- 6.9 Silica removes Fe_2O_3 remaining in the matte by forming silicate, FeSiO_3 .
- 6.15 Cast iron is made from pig iron by melting pig iron with scrap iron and coke. It has slightly lower carbon content ($\approx 3\%$) than pig iron ($\approx 4\% \text{ C}$)
- 6.17 To remove basic impurities, like Fe_2O_3
- 6.18 To lower the melting point of the mixture.
- 6.20 The reduction may require very high temperature if CO is used as a reducing agent in this case.
- 6.21 Yes, $2\text{Al} + \frac{3}{2}\text{O}_2 \rightarrow \text{Al}_2\text{O}_3 \quad \Delta_r G^\circ = -827 \text{ kJ mol}^{-1}$
- $2\text{Cr} + \frac{3}{2}\text{O}_2 \rightarrow \text{Cr}_2\text{O}_3 \quad \Delta_r G^\circ = -540 \text{ kJ mol}^{-1}$
- Hence $\text{Cr}_2\text{O}_3 + 2\text{Al} \rightarrow \text{Al}_2\text{O}_3 + 2\text{Cr} \quad -827 - (-540) = -287 \text{ kJ mol}^{-1}$
- 6.22 Carbon is better reducing agent.
- 6.25 Graphite rods act as anode and get burnt away as CO and CO_2 during the process of electrolysis.
- 6.28 Above 1600K Al can reduce MgO .

UNIT 7

- 7.10** Because of inability of nitrogen to expand its covalency beyond 4.
- 7.20** Freons
- 7.22** It dissolves in rain water and produces acid rain.
- 7.23** Due to strong tendency to accept electrons, halogens act as strong oxidising agent.
- 7.24** Due to high electronegativity and small size, it cannot act as central atom in higher oxoacids.
- 7.25** Nitrogen has smaller size than chlorine. Smaller size favours hydrogen bonding.
- 7.30** Synthesis of O_2PtF_6 inspired Bartlett to prepare XePtF_6 as Xe and oxygen have nearly same ionisation enthalpies.
- 7.31** (i) +3 (ii) +3 (iii) -3 (iv) +5 (v) +5
- 7.34** ClF, Yes.
- 7.36** (i) $\text{I}_2 < \text{F}_2 < \text{Br}_2 < \text{Cl}_2$
(ii) $\text{HF} < \text{HCl} < \text{HBr} < \text{HI}$
(iii) $\text{BiH}_3 \leq \text{SbH}_3 < \text{AsH}_3 < \text{PH}_3 < \text{NH}_3$
- 7.37** (ii) NeF_2
- 7.38** (i) XeF_4
(ii) XeF_2
(iii) XeO_3

UNIT 8

- 8.2** It is because Mn^{2+} has $3d^5$ configuration which has extra stability.
- 8.5** Stable oxidation states.
 $3d^3$ (Vanadium): +2, +3, +4, and +5
 $3d^5$ (Chromium): +3, +4, +6
 $3d^5$ (Manganese): +2, +4, +6, +7
 $3d^8$ (Nickel): +2, +3 (in complexes)
 $3d^4$ There is no d^4 configuration in the ground state.
- 8.6** Vanadate VO_3^- , chromate CrO_4^{2-} , permanganate MnO_4^-
- 8.10** +3 is the common oxidation state of the lanthanoids
In addition to +3, oxidation states +2 and +4 are also exhibited by some of the lanthanoids.
- 8.13** In transition elements the oxidation states vary from +1 to any highest oxidation state by one
For example, for manganese it may vary as +2, +3, +4, +5, +6, +7. In the nontransition elements the variation is selective, always differing by 2, e.g. +2, +4, or +3, +5 or +4, +6 etc.
- 8.18** Except Sc^{3+} , all others will be coloured in aqueous solution because of incompletely filled $3d$ -orbitals, will give rise to $d-d$ transitions.
- 8.21** (i) Cr^{2+} is reducing as it involves change from d^4 to d^3 , the latter is more stable configuration
(t_{2g}^3) Mn(III) to Mn(II) is from $3d^4$ to $3d^5$ again $3d^5$ is an extra stable configuration.
(ii) Due to CFSE, which more than compensates the 3rd IE.
(iii) The hydration or lattice energy more than compensates the ionisation enthalpy involved in removing electron from d^1 .
- 8.23** Copper, because with +1 oxidation state an extra stable configuration, $3d^{10}$ results.
- 8.24** Unpaired electrons $\text{Mn}^{3+} = 4$, $\text{Cr}^{3+} = 3$, $\text{V}^{3+} = 2$, $\text{Ti}^{3+} = 1$. Most stable Cr^{3+}
- 8.28** Second part 59, 95, 102.
- 8.30** Lawrencium, 103, +3

8.36 $Ti^{2+} = 2$, $V^{2+} = 3$, $Cr^{3+} = 3$, $Mn^{2+} = 5$, $Fe^{2+} = 6$, $Fe^{3+} = 5$, $Co^{2+} = 7$, $Ni^{2+} = 8$, $Cu^{2+} = 9$

8.38 $M\sqrt{n(n+2)} = 2.2$, $n \approx 1$, d^2 sp^3 , CN^- strong ligand
= 5.3, $n \approx 4$, sp^3 , d^2 , H_2O weak ligand
= 5.9, $n \approx 5$, sp^3 , Cl^- weak ligand.

UNIT 9

9.5 (i) +3 (ii) +3 (iii) +2 (iv) +3 (v) +3

9.6 (i) $[Zn(OH)_4]^{2-}$ (ii) $K_2[PdCl_4]$ (iii) $[Pt(NH_3)_2Cl_2]$ (iv) $K_2[Ni(CN)_4]$

(v) $[Co(NH_3)_5(ONO)]^{2+}$ (vi) $[Co(NH_3)_6]_2(SO_4)_3$ (vii) $K_3[Cr(C_2O_4)_3]$ (viii) $[Pt(NH_3)_6]^{4+}$

(ix) $[CuBr_4]^{2-}$ (x) $[Co(NH_3)_5(NO_2)]^{2+}$

9.9 (i) $[Cr(C_2O_4)_3]^{3-}$ Nil

(ii) $[Co(NH_3)_3Cl_3]^-$ Two (*fac*- and *mer*-)

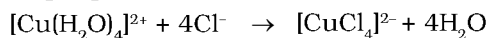
9.12 Three (two *cis* and one *trans*)

9.13 Aqueous $CuSO_4$ solution exists as $[Cu(H_2O)_4]SO_4$ which has blue colour due to $[Cu(H_2O)_4]^{2+}$ ions.

(i) When KF is added, the weak H_2O ligands are replaced by F^- ligands, forming $[CuF_4]^{2-}$ ions which is a green precipitate.



(ii) When KCl is added, Cl^- ligands replace the weak H_2O ligands forming $[CuCl_4]^{2-}$ ions which has bright green colour.



9.14 $[Cu(H_2O)_4]^{2+} + 4CN^- \rightarrow [Cu(CN)_4]^{2-} + 4H_2O$

As CN^- is a strong ligand, it forms a highly stable complex with Cu^{2+} ion. On passing H_2S , free Cu^{2+} ions are not available to form the precipitate of CuS .

9.23 (i) OS = +3, CN = 6, d-orbital occupation is $t_{2g}^6 e_g^0$.

(ii) OS = +3, CN = 6, d^3 (t_{2g}^3),

(iii) OS = +2, CN = 4, d^7 ($t_{2g}^5 e_g^2$),

(iv) OS = +2, CN = 6, d^5 ($t_{2g}^3 e_g^2$).

9.28 (iii)

9.29 (ii)

9.30 (iii)

9.31 (iii)

9.32 (i) The order of the ligand in the spectrochemical series :



Hence the energy of the observed light will be in the order :



Thus, wavelengths absorbed ($E = hc/\lambda$) will be in the opposite order.

Elements, their Atomic Number and Molar Mass

| Element | Symbol | Atomic Number | Molar mass/ (g mol ⁻¹) |
|-------------|--------|---------------|---------------------------------------|
| Actinium | Ac | 89 | 227.03 |
| Aluminium | Al | 13 | 26.98 |
| Americium | Am | 95 | (243) |
| Antimony | Sb | 51 | 121.75 |
| Argon | Ar | 18 | 39.95 |
| Arsenic | As | 33 | 74.92 |
| Astatine | At | 85 | 210 |
| Barium | Ba | 56 | 137.34 |
| Berkelium | Bk | 97 | (247) |
| Beryllium | Be | 4 | 9.01 |
| Bismuth | Bi | 83 | 208.98 |
| Bohrium | Bh | 107 | (264) |
| Boron | B | 5 | 10.81 |
| Bromine | Br | 35 | 79.91 |
| Cadmium | Cd | 48 | 112.40 |
| Caesium | Cs | 55 | 132.91 |
| Calcium | Ca | 20 | 40.08 |
| Californium | Cf | 98 | 251.08 |
| Carbon | C | 6 | 12.01 |
| Cerium | Ce | 58 | 140.12 |
| Chlorine | Cl | 17 | 35.45 |
| Chromium | Cr | 24 | 52.00 |
| Cobalt | Co | 27 | 58.93 |
| Copper | Cu | 29 | 63.54 |
| Curium | Cm | 96 | 247.07 |
| Dubnium | Db | 105 | (263) |
| Dysprosium | Dy | 66 | 162.50 |
| Einsteinium | Es | 99 | (252) |
| Erbium | Er | 68 | 167.26 |
| Europium | Eu | 63 | 151.96 |
| Fermium | Fm | 100 | (257.10) |
| Fluorine | F | 9 | 19.00 |
| Francium | Fr | 87 | (223) |
| Gadolinium | Gd | 64 | 157.25 |
| Gallium | Ga | 31 | 69.72 |
| Germanium | Ge | 32 | 72.61 |
| Gold | Au | 79 | 196.97 |
| Hafnium | Hf | 72 | 178.49 |
| Hassium | Hs | 108 | (269) |
| Helium | He | 2 | 4.00 |
| Holmium | Ho | 67 | 164.93 |
| Hydrogen | H | 1 | 1.0079 |
| Indium | In | 49 | 114.82 |
| Iodine | I | 53 | 126.90 |
| Iridium | Ir | 77 | 192.2 |
| Iron | Fe | 26 | 55.85 |
| Krypton | Kr | 36 | 83.80 |
| Lanthanum | La | 57 | 138.91 |
| Lawrencium | Lr | 103 | (262.1) |
| Lead | Pb | 82 | 207.19 |
| Lithium | Li | 3 | 6.94 |
| Lutetium | Lu | 71 | 174.96 |
| Magnesium | Mg | 12 | 24.31 |
| Manganese | Mn | 25 | 54.94 |
| Meitneium | Mt | 109 | (268) |
| Mendelevium | Md | 101 | 258.10 |

| Element | Symbol | Atomic Number | Molar mass/ (g mol ⁻¹) |
|---------------|--------|---------------|---------------------------------------|
| Mercury | Hg | 80 | 200.59 |
| Molybdenum | Mo | 42 | 95.94 |
| Neodymium | Nd | 60 | 144.24 |
| Neon | Ne | 10 | 20.18 |
| Neptunium | Np | 93 | (237.05) |
| Nickel | Ni | 28 | 58.71 |
| Niobium | Nb | 41 | 92.91 |
| Nitrogen | N | 7 | 14.0067 |
| Nobelium | No | 102 | (259) |
| Osmium | Os | 76 | 190.2 |
| Oxygen | O | 8 | 16.00 |
| Palladium | Pd | 46 | 106.4 |
| Phosphorus | P | 15 | 30.97 |
| Platinum | Pt | 78 | 195.09 |
| Plutonium | Pu | 94 | (244) |
| Polonium | Po | 84 | 210 |
| Potassium | K | 19 | 39.10 |
| Praseodymium | Pr | 59 | 140.91 |
| Promethium | Pm | 61 | (145) |
| Protactinium | Pa | 91 | 231.04 |
| Radium | Ra | 88 | (226) |
| Radon | Rn | 86 | (222) |
| Rhenium | Re | 75 | 186.2 |
| Rhodium | Rh | 45 | 102.91 |
| Rubidium | Rb | 37 | 85.47 |
| Ruthenium | Ru | 44 | 101.07 |
| Rutherfordium | Rf | 104 | (261) |
| Samarium | Sm | 62 | 150.35 |
| Scandium | Sc | 21 | 44.96 |
| Seaborgium | Sg | 106 | (266) |
| Selenium | Se | 34 | 78.96 |
| Silicon | Si | 14 | 28.08 |
| Silver | Ag | 47 | 107.87 |
| Sodium | Na | 11 | 22.99 |
| Strontium | Sr | 38 | 87.62 |
| Sulphur | S | 16 | 32.06 |
| Tantalum | Ta | 73 | 180.95 |
| Technetium | Tc | 43 | (98.91) |
| Tellurium | Te | 52 | 127.60 |
| Terbium | Tb | 65 | 158.92 |
| Thallium | Tl | 81 | 204.37 |
| Thorium | Th | 90 | 232.04 |
| Thulium | Tm | 69 | 168.93 |
| Tin | Sn | 50 | 118.69 |
| Titanium | Ti | 22 | 47.88 |
| Tungsten | W | 74 | 183.85 |
| Ununbium | Uub | 112 | (277) |
| Ununnilium | Uun | 110 | (269) |
| Unununium | Uuu | 111 | (272) |
| Uranium | U | 92 | 238.03 |
| Vanadium | V | 23 | 50.94 |
| Xenon | Xe | 54 | 131.30 |
| Ytterbium | Yb | 70 | 173.04 |
| Yttrium | Y | 39 | 88.91 |
| Zinc | Zn | 30 | 65.37 |
| Zirconium | Zr | 40 | 91.22 |

The value given in parenthesis is the molar mass of the isotope of largest known half-life.

Some Useful Conversion Factors

Common Unit of Mass and Weight

1 pound = 453.59 grams

1 pound = 453.59 grams = 0.45359 kilogram
1 kilogram = 1000 grams = 2.205 pounds
1 gram = 10 decigrams = 100 centigrams
 = 1000 milligrams
1 gram = 6.022 × 10²³ atomic mass units or u
1 atomic mass unit = 1.6606 × 10⁻²⁴ gram
1 metric tonne = 1000 kilograms
 = 2205 pounds

Common Unit of Volume

1 quart = 0.9463 litre

1 litre = 1.056 quarts

1 litre = 1 cubic decimetre = 1000 cubic
centimetres = 0.001 cubic metre
1 millilitre = 1 cubic centimetre = 0.001 litre
 = 1.056 × 10⁻³ quart
1 cubic foot = 28.316 litres = 29.902 quarts
 = 7.475 gallons

Common Units of Energy

1 joule = 1 × 10⁷ ergs

1 thermochemical calorie**
 = 4.184 joules
 = 4.184 × 10⁷ ergs
= 4.129 × 10⁻² litre-atmospheres
= 2.612 × 10¹⁹ electron volts
1 ergs = 1 × 10⁻⁷ joule = 2.3901 × 10⁻⁸ calorie
1 electron volt = 1.6022 × 10⁻¹⁹ joule
 = 1.6022 × 10⁻¹² erg
 = 96.487 kJ/mol†
1 litre-atmosphere = 24.217 calories
 = 101.32 joules
 = 1.0132 × 10⁹ ergs
1 British thermal unit = 1055.06 joules
 = 1.05506 × 10¹⁰ ergs
 = 252.2 calories

Common Units of Length

1 inch = 2.54 centimetres (exactly)

1 mile = 5280 feet = 1.609 kilometres
1 yard = 36 inches = 0.9144 metre
1 metre = 100 centimetres = 39.37 inches
 = 3.281 feet
 = 1.094 yards
1 kilometre = 1000 metres = 1094 yards
 = 0.6215 mile
1 Angstrom = 1.0 × 10⁻⁸ centimetre
 = 0.10 nanometre
 = 1.0 × 10⁻¹⁰ metre
 = 3.937 × 10⁻⁹ inch

Common Units of Force* and Pressure

1 atmosphere = 760 millimetres of mercury
 = 1.013 × 10⁵ pascals
 = 14.70 pounds per square inch
1 bar = 10⁵ pascals
1 torr = 1 millimetre of mercury
1 pascal = 1 kg/ms² = 1 N/m²

Temperature

SI Base Unit: Kelvin (K)

K = -273.15°C
K = °C + 273.15
°F = 1.8(°C) + 32

°C = $\frac{^{\circ}\text{F} - 32}{1.8}$

* Force: 1 newton (N) = 1 kg m/s², i.e., the force that, when applied for 1 second, gives a 1-kilogram mass a velocity of 1 metre per second.
** The amount of heat required to raise the temperature of one gram of water from 14.5°C to 15.5°C.
† Note that the other units are per particle and must be multiplied by 6.022 × 10²³ to be strictly comparable.

Standard potentials at 298 K in electrochemical order

| Reduction half-reaction | E° / V | Reduction half-reaction | E° / V |
|---|----------------------|---|----------------------|
| $\text{H}_4\text{XeO}_6 + 2\text{H}^+ + 2\text{e}^- \longrightarrow \text{XeO}_3 + 3\text{H}_2\text{O}$ | +3.0 | $\text{Cu}^+ + \text{e}^- \longrightarrow \text{Cu}$ | +0.52 |
| $\text{F}_2 + 2\text{e}^- \longrightarrow 2\text{F}^-$ | +2.87 | $\text{NiOOH} + \text{H}_2\text{O} + \text{e}^- \longrightarrow \text{Ni}(\text{OH})_2 + \text{OH}^-$ | +0.49 |
| $\text{O}_3 + 2\text{H}^+ + 2\text{e}^- \longrightarrow \text{O}_2 + \text{H}_2\text{O}$ | +2.07 | $\text{Ag}_2\text{CrO}_4 + 2\text{e}^- \longrightarrow 2\text{Ag} + \text{CrO}_4^{2-}$ | +0.45 |
| $\text{S}_2\text{O}_8^{2-} + 2\text{e}^- \longrightarrow 2\text{SO}_4^{2-}$ | +2.05 | $\text{O}_2 + 2\text{H}_2\text{O} + 4\text{e}^- \longrightarrow 4\text{OH}^-$ | +0.40 |
| $\text{Ag}^+ + \text{e}^- \longrightarrow \text{Ag}^+$ | +1.98 | $\text{ClO}_4^- + \text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{ClO}_3^- + 2\text{OH}^-$ | +0.36 |
| $\text{Co}^{3+} + \text{e}^- \longrightarrow \text{Co}^{2+}$ | +1.81 | $[\text{Fe}(\text{CN})_6]^{3-} + \text{e}^- \longrightarrow [\text{Fe}(\text{CN})_6]^{4-}$ | +0.36 |
| $\text{H}_2\text{O}_2 + 2\text{H}^+ + 2\text{e}^- \longrightarrow 2\text{H}_2\text{O}$ | +1.78 | $\text{Cu}^{2+} + 2\text{e}^- \longrightarrow \text{Cu}$ | +0.34 |
| $\text{Au}^+ + \text{e}^- \longrightarrow \text{Au}$ | +1.69 | $\text{Hg}_2\text{Cl}_2 + 2\text{e}^- \longrightarrow 2\text{Hg} + 2\text{Cl}^-$ | +0.27 |
| $\text{Pb}^{4+} + 2\text{e}^- \longrightarrow \text{Pb}^{2+}$ | +1.67 | $\text{AgCl} + \text{e}^- \longrightarrow \text{Ag} + \text{Cl}^-$ | +0.27 |
| $2\text{HClO} + 2\text{H}^+ + 2\text{e}^- \longrightarrow \text{Cl}_2 + 2\text{H}_2\text{O}$ | +1.63 | $\text{Bi}^{3+} + 3\text{e}^- \longrightarrow \text{Bi}$ | +0.20 |
| $\text{Ce}^{4+} + \text{e}^- \longrightarrow \text{Ce}^{3+}$ | +1.61 | $\text{SO}_4^{2-} + 4\text{H}^+ + 2\text{e}^- \longrightarrow \text{H}_2\text{SO}_3 + \text{H}_2\text{O}$ | +0.17 |
| $2\text{HBrO} + 2\text{H}^+ + 2\text{e}^- \longrightarrow \text{Br}_2 + 2\text{H}_2\text{O}$ | +1.60 | $\text{Cu}^{2+} + \text{e}^- \longrightarrow \text{Cu}^+$ | +0.16 |
| $\text{MnO}_4^- + 8\text{H}^+ + 5\text{e}^- \longrightarrow \text{Mn}^{2+} + 4\text{H}_2\text{O}$ | +1.51 | $\text{Sn}^{4+} + 2\text{e}^- \longrightarrow \text{Sn}^{2+}$ | +0.15 |
| $\text{Mn}^{3+} + \text{e}^- \longrightarrow \text{Mn}^{2+}$ | +1.51 | $\text{AgBr} + \text{e}^- \longrightarrow \text{Ag} + \text{Br}^-$ | +0.07 |
| $\text{Au}^{3+} + 3\text{e}^- \longrightarrow \text{Au}$ | +1.40 | $\text{Ti}^{4+} + \text{e}^- \longrightarrow \text{Ti}^{3+}$ | 0.00 |
| $\text{Cl}_2 + 2\text{e}^- \longrightarrow 2\text{Cl}^-$ | +1.36 | $2\text{H}^+ + 2\text{e}^- \longrightarrow \text{H}_2$ | 0.0 by definition |
| $\text{Cr}_2\text{O}_7^{2-} + 14\text{H}^+ + 6\text{e}^- \longrightarrow 2\text{Cr}^{3+} + 7\text{H}_2\text{O}$ | +1.33 | $\text{Fe}^{3+} + 3\text{e}^- \longrightarrow \text{Fe}$ | -0.04 |
| $\text{O}_3 + \text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{O}_2 + 2\text{OH}^-$ | +1.24 | $\text{O}_2 + \text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{HO}_2^- + \text{OH}^-$ | -0.08 |
| $\text{O}_2 + 4\text{H}^+ + 4\text{e}^- \longrightarrow 2\text{H}_2\text{O}$ | +1.23 | $\text{Pb}^{2+} + 2\text{e}^- \longrightarrow \text{Pb}$ | -0.13 |
| $\text{ClO}_4^- + 2\text{H}^+ + 2\text{e}^- \longrightarrow \text{ClO}_3^- + 2\text{H}_2\text{O}$ | +1.23 | $\text{In}^+ + \text{e}^- \longrightarrow \text{In}$ | -0.14 |
| $\text{MnO}_2 + 4\text{H}^+ + 2\text{e}^- \longrightarrow \text{Mn}^{2+} + 2\text{H}_2\text{O}$ | +1.23 | $\text{Sn}^{2+} + 2\text{e}^- \longrightarrow \text{Sn}$ | -0.14 |
| $\text{Pt}^{2+} + 2\text{e}^- \longrightarrow \text{Pt}$ | +1.20 | $\text{AgI} + \text{e}^- \longrightarrow \text{Ag} + \text{I}^-$ | -0.15 |
| $\text{Br}_2 + 2\text{e}^- \longrightarrow 2\text{Br}^-$ | +1.09 | $\text{Ni}^{2+} + 2\text{e}^- \longrightarrow \text{Ni}$ | -0.23 |
| $\text{Pu}^{4+} + \text{e}^- \longrightarrow \text{Pu}^{3+}$ | +0.97 | $\text{V}^{3+} + \text{e}^- \longrightarrow \text{V}^{2+}$ | -0.26 |
| $\text{NO}_3^- + 4\text{H}^+ + 3\text{e}^- \longrightarrow \text{NO} + 2\text{H}_2\text{O}$ | +0.96 | $\text{Co}^{2+} + 2\text{e}^- \longrightarrow \text{Co}$ | -0.28 |
| $2\text{Hg}^{2+} + 2\text{e}^- \longrightarrow \text{Hg}_2^{2+}$ | +0.92 | $\text{In}^{3+} + 3\text{e}^- \longrightarrow \text{In}$ | -0.34 |
| $\text{ClO}^- + \text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{Cl}^- + 2\text{OH}^-$ | +0.89 | $\text{Tl}^+ + \text{e}^- \longrightarrow \text{Tl}$ | -0.34 |
| $\text{Hg}_2^{2+} + 2\text{e}^- \longrightarrow \text{Hg}$ | +0.86 | $\text{PbSO}_4 + 2\text{e}^- \longrightarrow \text{Pb} + \text{SO}_4^{2-}$ | -0.36 |
| $\text{NO}_3^- + 2\text{H}^+ + \text{e}^- \longrightarrow \text{NO}_2 + \text{H}_2\text{O}$ | +0.80 | $\text{Ti}^{3+} + \text{e}^- \longrightarrow \text{Ti}^{2+}$ | -0.37 |
| $\text{Ag}^+ + \text{e}^- \longrightarrow \text{Ag}$ | +0.80 | $\text{Cd}^{2+} + 2\text{e}^- \longrightarrow \text{Cd}$ | -0.40 |
| $\text{Hg}_2^{2+} + 2\text{e}^- \longrightarrow 2\text{Hg}$ | +0.79 | $\text{In}^{2+} + \text{e}^- \longrightarrow \text{In}^+$ | -0.40 |
| $\text{Fe}^{3+} + \text{e}^- \longrightarrow \text{Fe}^{2+}$ | +0.77 | $\text{Cr}^{3+} + \text{e}^- \longrightarrow \text{Cr}^{2+}$ | -0.41 |
| $\text{BrO}^- + \text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{Br}^- + 2\text{OH}^-$ | +0.76 | $\text{Fe}^{2+} + 2\text{e}^- \longrightarrow \text{Fe}$ | -0.44 |
| $\text{Hg}_2\text{SO}_4 + 2\text{e}^- \longrightarrow 2\text{Hg} + \text{SO}_4^{2-}$ | +0.62 | $\text{In}^{3+} + 2\text{e}^- \longrightarrow \text{In}^+$ | -0.44 |
| $\text{MnO}_4^{2-} + 2\text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{MnO}_2 + 4\text{OH}^-$ | +0.60 | $\text{S} + 2\text{e}^- \longrightarrow \text{S}^{2-}$ | -0.48 |
| $\text{MnO}_4^- + \text{e}^- \longrightarrow \text{MnO}_4^{2-}$ | +0.56 | $\text{In}^{3+} + \text{e}^- \longrightarrow \text{In}^{2+}$ | -0.49 |
| $\text{I}_2 + 2\text{e}^- \longrightarrow 2\text{I}^-$ | +0.54 | $\text{U}^{4+} + \text{e}^- \longrightarrow \text{U}^{3+}$ | -0.61 |
| $\text{I}_3 + 2\text{e}^- \longrightarrow 3\text{I}^-$ | +0.53 | $\text{Cr}^{3+} + 3\text{e}^- \longrightarrow \text{Cr}$ | -0.74 |
| | | $\text{Zn}^{2+} + 2\text{e}^- \longrightarrow \text{Zn}$ | -0.76 |

(continued)

| Reduction half-reaction | E°/V | Reduction half-reaction | E°/V |
|---|--------------------|--|--------------------|
| $\text{Cd}(\text{OH})_2 + 2\text{e}^- \longrightarrow \text{Cd} + 2\text{OH}^-$ | -0.81 | $\text{La}^{3+} + 3\text{e}^- \longrightarrow \text{La}$ | -2.52 |
| $2\text{H}_2\text{O} + 2\text{e}^- \longrightarrow \text{H}_2 + 2\text{OH}^-$ | -0.83 | $\text{Na}^+ + \text{e}^- \longrightarrow \text{Na}$ | -2.71 |
| $\text{Cr}^{2+} + 2\text{e}^- \longrightarrow \text{Cr}$ | -0.91 | $\text{Ca}^{2+} + 2\text{e}^- \longrightarrow \text{Ca}$ | -2.87 |
| $\text{Mn}^{2+} + 2\text{e}^- \longrightarrow \text{Mn}$ | -1.18 | $\text{Sr}^{2+} + 2\text{e}^- \longrightarrow \text{Sr}$ | -2.89 |
| $\text{V}^{2+} + 2\text{e}^- \longrightarrow \text{V}$ | -1.19 | $\text{Ba}^{2+} + 2\text{e}^- \longrightarrow \text{Ba}$ | -2.91 |
| $\text{Ti}^{2+} + 2\text{e}^- \longrightarrow \text{Ti}$ | -1.63 | $\text{Ra}^{2+} + 2\text{e}^- \longrightarrow \text{Ra}$ | -2.92 |
| $\text{Al}^{3+} + 3\text{e}^- \longrightarrow \text{Al}$ | -1.66 | $\text{Cs}^+ + \text{e}^- \longrightarrow \text{Cs}$ | -2.92 |
| $\text{U}^{3+} + 3\text{e}^- \longrightarrow \text{U}$ | -1.79 | $\text{Rb}^+ + \text{e}^- \longrightarrow \text{Rb}$ | -2.93 |
| $\text{Sc}^{3+} + 3\text{e}^- \longrightarrow \text{Sc}$ | -2.09 | $\text{K}^+ + \text{e}^- \longrightarrow \text{K}$ | -2.93 |
| $\text{Mg}^{2+} + 2\text{e}^- \longrightarrow \text{Mg}$ | -2.36 | $\text{Li}^+ + \text{e}^- \longrightarrow \text{Li}$ | -3.05 |
| $\text{Ce}^{3+} + 3\text{e}^- \longrightarrow \text{Ce}$ | -2.48 | | |

Logarithms

Sometimes, a numerical expression may involve multiplication, division or rational powers of large numbers. For such calculations, logarithms are very useful. They help us in making difficult calculations easy. In Chemistry, logarithm values are required in solving problems of chemical kinetics, thermodynamics, electrochemistry, etc. We shall first introduce this concept, and discuss the laws, which will have to be followed in working with logarithms, and then apply this technique to a number of problems to show how it makes difficult calculations simple.

We know that

$$2^3 = 8, 3^2 = 9, 5^3 = 125, 7^0 = 1$$

In general, for a positive real number a , and a rational number m , let $a^m = b$,

where b is a real number. In other words

the m^{th} power of base a is b .

Another way of stating the same fact is

logarithm of b to base a is m .

If for a positive real number a , $a \neq 1$

$$a^m = b,$$

we say that m is the logarithm of b to the base a .

We write this as $\log_a b = m$,

“log” being the abbreviation of the word “logarithm”.

Thus, we have

$$\log_2 8 = 3, \quad \text{Since } 2^3 = 8$$

$$\log_3 9 = 2, \quad \text{Since } 3^2 = 9$$

$$\log \frac{125}{5} = 3, \quad \text{Since } 5^3 = 125$$

$$\log_7 1 = 0, \quad \text{Since } 7^0 = 1$$

Laws of Logarithms

In the following discussion, we shall take logarithms to any base a , ($a > 0$ and $a \neq 1$)

First Law: $\log_a (mn) = \log_a m + \log_a n$

Proof: Suppose that $\log_a m = x$ and $\log_a n = y$

Then $a^x = m$, $a^y = n$

$$\text{Hence } mn = a^x \cdot a^y = a^{x+y}$$

It now follows from the definition of logarithms that

$$\log_a (mn) = x + y = \log_a m + \log_a n$$

Second Law: $\log_a \left(\frac{m}{n} \right) = \log_a m - \log_a n$

Proof: Let $\log_a m = x$, $\log_a n = y$

Then $a^x = m$, $a^y = n$

$$\text{Hence } \frac{m}{n} = \frac{a^x}{a^y} = a^{x-y}$$

Therefore

$$\log_a \left(\frac{m}{n} \right) = x - y = \log_a m - \log_a n$$

Third Law : $\log_a(m^n) = n \log_a m$

Proof : As before, if $\log_a m = x$, then $a^x = m$

$$\text{Then } m^n = (a^x)^n = a^{nx}$$

giving $\log_a(m^n) = nx = n \log_a m$

Thus according to First Law: “the log of the product of two numbers is equal to the sum of their logs. Similarly, the Second Law says: the log of the ratio of two numbers is the difference of their logs. Thus, the use of these laws converts a problem of multiplication / division into a problem of addition/ subtraction, which are far easier to perform than multiplication/division. That is why logarithms are so useful in all numerical computations.

Logarithms to Base 10

Because number 10 is the base of writing numbers, it is very convenient to use logarithms to the base 10. Some examples are:

$$\begin{array}{ll} \log_{10} 10 = 1, & \text{since } 10^1 = 10 \\ \log_{10} 100 = 2, & \text{since } 10^2 = 100 \\ \log_{10} 10000 = 4, & \text{since } 10^4 = 10000 \\ \log_{10} 0.01 = -2, & \text{since } 10^{-2} = 0.01 \\ \log_{10} 0.001 = -3, & \text{since } 10^{-3} = 0.001 \\ \text{and } \log_{10} 1 = 0 & \text{since } 10^0 = 1 \end{array}$$

The above results indicate that if n is an integral power of 10, i.e., 1 followed by several zeros or 1 preceded by several zeros immediately to the right of the decimal point, then $\log n$ can be easily found.

If n is not an integral power of 10, then it is not easy to calculate $\log n$. But mathematicians have made tables from which we can read off approximate value of the logarithm of any positive number between 1 and 10. And these are sufficient for us to calculate the logarithm of any number expressed in decimal form. For this purpose, we always express the given decimal as the product of an integral power of 10 and a number between 1 and 10.

Standard Form of Decimal

We can express any number in decimal form, as the product of (i) an integral power of 10, and (ii) a number between 1 and 10. Here are some examples:

(i) 25.2 lies between 10 and 100

$$25.2 = \frac{25.2}{10} \times 10 = 2.52 \times 10^1$$

(ii) 1038.4 lies between 1000 and 10000.

$$\therefore 1038.4 = \frac{1038.4}{1000} \times 10^3 = 1.0384 \times 10^3$$

(iii) 0.005 lies between 0.001 and 0.01

$$\therefore 0.005 = (0.005 \times 1000) \times 10^{-3} = 5.0 \times 10^{-3}$$

(iv) 0.00025 lies between 0.0001 and 0.001

$$\therefore 0.00025 = (0.00025 \times 10000) \times 10^{-4} = 2.5 \times 10^{-4}$$

In each case, we divide or multiply the decimal by a power of 10, to bring one non-zero digit to the left of the decimal point, and do the reverse operation by the same power of 10, indicated separately.

Thus, any positive decimal can be written in the form
 $n = m \times 10^p$
where p is an integer (positive, zero or negative) and $1 \leq m < 10$. This is called the “standard form of n .”

Working Rule

1. Move the decimal point to the left, or to the right, as may be necessary, to bring one non-zero digit to the left of decimal point.
2. (i) If you move p places to the left, multiply by 10^p .
(ii) If you move p places to the right, multiply by 10^{-p} .
(iii) If you do not move the decimal point at all, multiply by 10^0 .
(iv) Write the new decimal obtained by the power of 10 (of step 2) to obtain the standard form of the given decimal.

Characteristic and Mantissa

Consider the standard form of n
 $n = m \times 10^p$, where $1 \leq m < 10$
Taking logarithms to the base 10 and using the laws of logarithms
 $\log n = \log m + \log 10^p$
 $= \log m + p \log 10$
 $= p + \log m$

Here p is an integer and as $1 \leq m < 10$, so $0 \leq \log m < 1$, i.e., m lies between 0 and 1. When $\log n$ has been expressed as $p + \log m$, where p is an integer and $0 \leq \log m < 1$, we say that p is the “characteristic” of $\log n$ and that $\log m$ is the “mantissa of $\log n$.” Note that characteristic is always an integer – positive, negative or zero, and mantissa is never negative and is always less than 1. If we can find the characteristics and the mantissa of $\log n$, we have to just add them to get $\log n$.

- Thus to find $\log n$, all we have to do is as follows:
1. Put n in the standard form, say
 $n = m \times 10^p$, $1 \leq m < 10$
 2. Read off the characteristic p of $\log n$ from this expression (exponent of 10).
 3. Look up $\log m$ from tables, which is being explained below.
 4. Write $\log n = p + \log m$

If the characteristic p of a number n is say, 2 and the mantissa is .4133, then we have $\log n = 2 + .4133$ which we can write as 2.4133. If, however, the characteristic p of a number m is say -2 and the mantissa is .4123, then we have $\log m = -2 + .4123$. We cannot write this as -2.4123. (Why?) In order to avoid this confusion we write $\bar{2}$ for -2 and thus we write $\log m = \bar{2}.4123$.

Now let us explain how to use the table of logarithms to find mantissas. A table is appended at the end of this Appendix.
Observe that in the table, every row starts with a two digit number, 10, 11, 12,... 97, 98, 99. Every column is headed by a one-digit number, 0, 1, 2, ...9. On the right, we have the section called “Mean differences” which has 9 columns headed by 1, 2...9.

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|------|------|------|------|------|------|------|------|------|------|----|----|----|----|----|----|----|----|----|----|
| .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. | .. |
| 61 | 7853 | 7860 | 7868 | 7875 | 7882 | 7889 | 7896 | 7803 | 7810 | 7817 | | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 62 | 7924 | 7931 | 7935 | 7945 | 7954 | 7959 | 7966 | 7973 | 7980 | 7987 | | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |
| 63 | 7993 | 8000 | 8007 | 8014 | 8021 | 8028 | 8035 | 8041 | 8048 | 8055 | | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |

Now suppose we wish to find $\log (6.234)$. Then look into the row starting with 62. In this row, look

at the number in the column headed by 3. The number is 7945. This means that

$$\log (6.230) = 0.7945^*$$

But we want $\log (6.234)$. So our answer will be a little more than 0.7945. How much more? We look this up in the section on Mean differences. Since our fourth digit is 4, look under the column headed by 4 in the Mean difference section (in the row 62). We see the number 3 there. So add 3 to 7945. We get 7948. So we finally have

$$\log (6.234) = 0.7948.$$

Take another example. To find $\log (8.127)$, we look in the row 81 under column 2, and we find 9096. We continue in the same row and see that the mean difference under 7 is 4. Adding this to 9096, and we get 9100. So, $\log (8.127) = 0.9100$.

Finding N when $\log N$ is given

We have so far discussed the procedure for finding $\log n$ when a positive number n is given. We now turn to its converse i.e., to find n when $\log n$ is given and give a method for this purpose. If $\log n = t$, we sometimes say $n = \text{antilog } t$. Therefore our task is given t , find its antilog. For this, we use the ready-made antilog tables.

Suppose $\log n = 2.5372$.

To find n , first take just the mantissa of $\log n$. In this case it is .5372. (Make sure it is positive.) Now take up antilog of this number in the antilog table which is to be used exactly like the log table. In the antilog table, the entry under column 7 in the row .53 is 3443 and the mean difference for the last digit 2 in that row is 2, so the table gives 3445. Hence,

$$\text{antilog } (.5372) = 3.445$$

Now since $\log n = 2.5372$, the characteristic of $\log n$ is 2. So the standard form of n is given by

$$n = 3.445 \times 10^2$$

$$\text{or } n = 344.5$$

Illustration 1:

If $\log x = 1.0712$, find x .

Solution: We find that the number corresponding to 0712 is 1179. Since characteristic of $\log x$ is 1, we have

$$\begin{aligned} x &= 1.179 \times 10^1 \\ &= 11.79 \end{aligned}$$

Illustration 2:

If $\log x = \bar{2}.1352$, find x .

Solution: From antilog tables, we find that the number corresponding to 1352 is 1366. Since the characteristic is $\bar{2}$ i.e., -2, so

$$x = 1.366 \times 10^{-2} = 0.01366$$

Use of Logarithms in Numerical Calculations

Illustration 1:

Find 6.3×1.29

Solution: Let $x = 6.3 \times 1.29$

$$\text{Then } \log x = \log (6.3 \times 1.29) = \log 6.3 + \log 1.29$$

Now,

$$\log 6.3 = 0.7993$$

$$\log 1.29 = 0.1106$$

$$\therefore \log x = 0.9099,$$

Taking antilog

* It should, however, be noted that the values given in the table are not exact. They are only approximate values, although we use the sign of equality which may give the impression that they are exact values. The same convention will be followed in respect of antilogarithm of a number.

$$x = 8.127$$

Illustration 2:

$$\text{Find } \frac{(1.23)^{1.5}}{11.2 \times 23.5}$$

$$\textbf{Solution:} \text{ Let } x = \frac{(1.23)^{\frac{3}{2}}}{11.2 \times 23.5}$$

$$\text{Then } \log x = \log \frac{(1.23)^{\frac{3}{2}}}{11.2 \times 23.5}$$

$$= \frac{3}{2} \log 1.23 - \log (11.2 \times 23.5)$$

$$= \frac{3}{2} \log 1.23 - \log 11.2 - \log 23.5$$

Now,

$$\log 1.23 = 0.0899$$

$$\frac{3}{2} \log 1.23 = 0.13485$$

$$\log 11.2 = 1.0492$$

$$\log 23.5 = 1.3711$$

$$\log x = 0.13485 - 1.0492 - 1.3711$$

$$= \overline{3.71455}$$

$$\therefore x = 0.005183$$

Illustration 3:

$$\text{Find } \sqrt{\frac{(71.24)^5 \times \sqrt{56}}{(2.3)^7 \times \sqrt{21}}}$$

$$\textbf{Solution:} \text{ Let } x = \sqrt{\frac{(71.24)^5 \times \sqrt{56}}{(2.3)^7 \times \sqrt{21}}}$$

$$\text{Then } \log x = \frac{1}{2} \log \left[\frac{(71.24)^5 \times \sqrt{56}}{(2.3)^7 \times \sqrt{21}} \right]$$

$$= \frac{1}{2} [\log (71.24)^5 + \log \sqrt{56} - \log (2.3)^7 - \log \sqrt{21}]$$

$$= \frac{5}{2} \log 71.24 + \frac{1}{4} \log 56 - \frac{7}{2} \log 2.3 - \frac{1}{4} \log 21$$

Now, using log tables

$$\log 71.24 = 1.8527$$

$$\log 56 = 1.7482$$

$$\log 2.3 = 0.3617$$

$$\log 21 = 1.3222$$

$$\therefore \log x = \frac{5}{2} \log (1.8527) + \frac{1}{4} (1.7482) - \frac{7}{2} (0.3617) - \frac{1}{4} (1.3222)$$

$$= 3.4723$$

$$\therefore x = 2967$$

LOGARITHMS

TABLE I

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|------|------|------|------|------|------|------|------|------|------|---|---|----|----|----|----|----|----|----|
| 10 | 0000 | 0043 | 0086 | 0128 | 0170 | 0212 | 0253 | 0294 | 0334 | 0374 | 5 | 9 | 13 | 17 | 21 | 26 | 30 | 34 | 38 |
| | | | | | | | | | | | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 |
| 11 | 0414 | 0453 | 0492 | 0531 | 0569 | 0607 | 0645 | 0682 | 0719 | 0755 | 4 | 8 | 12 | 16 | 20 | 23 | 27 | 31 | 35 |
| | | | | | | | | | | | 4 | 7 | 11 | 15 | 18 | 22 | 26 | 29 | 33 |
| 12 | 0792 | 0828 | 0864 | 0899 | 0934 | 0969 | 1004 | 1038 | 1072 | 1106 | 3 | 7 | 11 | 14 | 18 | 21 | 25 | 28 | 32 |
| | | | | | | | | | | | 3 | 7 | 10 | 14 | 17 | 20 | 24 | 27 | 31 |
| 13 | 1139 | 1173 | 1206 | 1239 | 1271 | 1303 | 1335 | 1367 | 1399 | 1430 | 3 | 6 | 10 | 13 | 16 | 19 | 23 | 26 | 29 |
| | | | | | | | | | | | 3 | 7 | 10 | 13 | 16 | 19 | 22 | 25 | 29 |
| 14 | 1461 | 1492 | 1523 | 1553 | 1584 | 1614 | 1644 | 1673 | 1703 | 1732 | 3 | 6 | 9 | 12 | 15 | 19 | 22 | 25 | 28 |
| | | | | | | | | | | | 3 | 6 | 9 | 12 | 14 | 17 | 20 | 23 | 26 |
| 15 | 1761 | 1790 | 1818 | 1847 | 1875 | 1903 | 1931 | 1959 | 1987 | 2014 | 3 | 6 | 9 | 11 | 14 | 17 | 20 | 23 | 26 |
| | | | | | | | | | | | 3 | 6 | 8 | 11 | 14 | 17 | 19 | 22 | 25 |
| 16 | 2041 | 2068 | 2095 | 2122 | 2148 | 2175 | 2201 | 2227 | 2253 | 2279 | 3 | 6 | 8 | 11 | 14 | 16 | 19 | 22 | 24 |
| | | | | | | | | | | | 3 | 5 | 8 | 10 | 13 | 16 | 18 | 21 | 23 |
| 17 | 2304 | 2330 | 2355 | 2380 | 2405 | 2430 | 2455 | 2480 | 2504 | 2529 | 3 | 5 | 8 | 10 | 13 | 15 | 18 | 20 | 23 |
| | | | | | | | | | | | 3 | 5 | 8 | 10 | 12 | 15 | 17 | 20 | 22 |
| 18 | 2553 | 2577 | 2601 | 2625 | 2648 | 2672 | 2695 | 2718 | 2742 | 2765 | 2 | 5 | 7 | 9 | 12 | 14 | 17 | 19 | 21 |
| | | | | | | | | | | | 2 | 4 | 7 | 9 | 11 | 14 | 16 | 18 | 21 |
| 19 | 2788 | 2810 | 2833 | 2856 | 2878 | 2900 | 2923 | 2945 | 2967 | 2989 | 2 | 4 | 7 | 9 | 11 | 13 | 16 | 18 | 20 |
| | | | | | | | | | | | 2 | 4 | 6 | 8 | 11 | 13 | 15 | 17 | 19 |
| 20 | 3010 | 3032 | 3054 | 3075 | 3096 | 3118 | 3139 | 3160 | 3181 | 3201 | 2 | 4 | 6 | 8 | 11 | 13 | 15 | 17 | 19 |
| 21 | 3222 | 3243 | 3263 | 3284 | 3304 | 3324 | 3345 | 3365 | 3385 | 3404 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| 22 | 3424 | 3444 | 3464 | 3483 | 3502 | 3522 | 3541 | 3560 | 3579 | 3598 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 15 | 17 |
| 23 | 3617 | 3636 | 3655 | 3674 | 3692 | 3711 | 3729 | 3747 | 3766 | 3784 | 2 | 4 | 6 | 7 | 9 | 11 | 13 | 15 | 17 |
| 24 | 3802 | 3820 | 3838 | 3856 | 3874 | 3892 | 3909 | 3927 | 3945 | 3962 | 2 | 4 | 5 | 7 | 9 | 11 | 12 | 14 | 16 |
| 25 | 3979 | 3997 | 4014 | 4031 | 4048 | 4065 | 4082 | 4099 | 4116 | 4133 | 2 | 3 | 5 | 7 | 9 | 10 | 12 | 14 | 15 |
| 26 | 4150 | 4166 | 4183 | 4200 | 4216 | 4232 | 4249 | 4265 | 4281 | 4298 | 2 | 3 | 5 | 7 | 8 | 10 | 11 | 13 | 15 |
| 27 | 4314 | 4330 | 4346 | 4362 | 4378 | 4393 | 4409 | 4425 | 4440 | 4456 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 13 | 14 |
| 28 | 4472 | 4487 | 4502 | 4518 | 4533 | 4548 | 4564 | 4579 | 4594 | 4609 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 12 | 14 |
| 29 | 4624 | 4639 | 4654 | 4669 | 4683 | 4698 | 4713 | 4728 | 4742 | 4757 | 1 | 3 | 4 | 6 | 7 | 9 | 10 | 12 | 13 |
| 30 | 4771 | 4786 | 4800 | 4814 | 4829 | 4843 | 4857 | 4871 | 4886 | 4900 | 1 | 3 | 4 | 6 | 7 | 9 | 10 | 11 | 13 |
| 31 | 4914 | 4928 | 4942 | 4955 | 4969 | 4983 | 4997 | 5011 | 5024 | 5038 | 1 | 3 | 4 | 6 | 7 | 8 | 10 | 11 | 12 |
| 32 | 5051 | 5065 | 5079 | 5092 | 5105 | 5119 | 5132 | 5145 | 5159 | 5172 | 1 | 3 | 4 | 5 | 7 | 8 | 9 | 11 | 12 |
| 33 | 5185 | 5198 | 5211 | 5224 | 5237 | 5250 | 5263 | 5276 | 5289 | 5302 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 12 |
| 34 | 5315 | 5328 | 5340 | 5353 | 5366 | 5378 | 5391 | 5403 | 5416 | 5428 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 11 |
| 35 | 5441 | 5453 | 5465 | 5478 | 5490 | 5502 | 5514 | 5527 | 5539 | 5551 | 1 | 2 | 4 | 5 | 6 | 7 | 9 | 10 | 11 |
| 36 | 5563 | 5575 | 5587 | 5599 | 5611 | 5623 | 5635 | 5647 | 5658 | 5670 | 1 | 2 | 4 | 5 | 6 | 7 | 8 | 10 | 11 |
| 37 | 5682 | 5694 | 5705 | 5717 | 5729 | 5740 | 5752 | 5763 | 5775 | 5786 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9 | 10 |
| 38 | 5798 | 5809 | 5821 | 5832 | 5843 | 5855 | 5866 | 5877 | 5888 | 5899 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9 | 10 |
| 39 | 5911 | 5922 | 5933 | 5944 | 5955 | 5966 | 5977 | 5988 | 5999 | 6010 | 1 | 2 | 3 | 4 | 5 | 7 | 8 | 9 | 10 |
| 40 | 6021 | 6031 | 6042 | 6053 | 6064 | 6075 | 6085 | 6096 | 6107 | 6117 | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 9 | 10 |
| 41 | 6128 | 6138 | 6149 | 6160 | 6170 | 6180 | 6191 | 6201 | 6212 | 6222 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 42 | 6232 | 6243 | 6253 | 6263 | 6274 | 6284 | 6294 | 6304 | 6314 | 6325 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 43 | 6335 | 6345 | 6355 | 6365 | 6375 | 6385 | 6395 | 6405 | 6415 | 6425 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 44 | 6435 | 6444 | 6454 | 6464 | 6474 | 6484 | 6493 | 6503 | 6513 | 6522 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 45 | 6532 | 6542 | 6551 | 6561 | 6471 | 6580 | 6590 | 6599 | 6609 | 6618 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 46 | 6628 | 6637 | 6646 | 6656 | 6665 | 6675 | 6684 | 6693 | 6702 | 6712 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 7 | 8 |
| 47 | 6721 | 6730 | 6739 | 6749 | 6758 | 6767 | 6776 | 6785 | 6794 | 6803 | 1 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 8 |
| 48 | 6812 | 6821 | 6830 | 6839 | 6848 | 6857 | 6866 | 6875 | 6884 | 6893 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 8 |
| 49 | 6902 | 6911 | 6920 | 6928 | 6937 | 6946 | 6955 | 6964 | 6972 | 6981 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 8 |

LOGARITHMS

TABLE 1 (Continued)

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| 50 | 6990 | 6998 | 7007 | 7016 | 7024 | 7033 | 7042 | 7050 | 7059 | 7067 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 51 | 7076 | 7084 | 7093 | 7101 | 7110 | 7118 | 7126 | 7135 | 7143 | 7152 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 52 | 7160 | 7168 | 7177 | 7185 | 7193 | 7202 | 7210 | 7218 | 7226 | 7235 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 7 | 7 |
| 53 | 7243 | 7251 | 7259 | 7267 | 7275 | 7284 | 7292 | 7300 | 7308 | 7316 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 54 | 7324 | 7332 | 7340 | 7348 | 7356 | 7364 | 7372 | 7380 | 7388 | 7396 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 55 | 7404 | 7412 | 7419 | 7427 | 7435 | 7443 | 7451 | 7459 | 7466 | 7474 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 56 | 7482 | 7490 | 7497 | 7505 | 7513 | 7520 | 7528 | 7536 | 7543 | 7551 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 57 | 7559 | 7566 | 7574 | 7582 | 7589 | 7597 | 7604 | 7612 | 7619 | 7627 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 58 | 7634 | 7642 | 7649 | 7657 | 7664 | 7672 | 7679 | 7686 | 7694 | 7701 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 59 | 7709 | 7716 | 7723 | 7731 | 7738 | 7745 | 7752 | 7760 | 7767 | 7774 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 60 | 7782 | 7789 | 7796 | 7803 | 7810 | 7818 | 7825 | 7832 | 7839 | 7846 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 61 | 7853 | 7860 | 7768 | 7875 | 7882 | 7889 | 7896 | 7903 | 7910 | 7917 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 62 | 7924 | 7931 | 7938 | 7945 | 7952 | 7959 | 7966 | 7973 | 7980 | 7987 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |
| 63 | 7993 | 8000 | 8007 | 8014 | 8021 | 8028 | 8035 | 8041 | 8048 | 8055 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 64 | 8062 | 8069 | 8075 | 8082 | 8089 | 8096 | 8102 | 8109 | 8116 | 8122 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 65 | 8129 | 8136 | 8142 | 8149 | 8156 | 8162 | 8169 | 8176 | 8182 | 8189 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 66 | 8195 | 8202 | 8209 | 8215 | 8222 | 8228 | 8235 | 8241 | 8248 | 8254 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 67 | 8261 | 8267 | 8274 | 8280 | 8287 | 8293 | 8299 | 8306 | 8312 | 8319 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 68 | 8325 | 8331 | 8338 | 8344 | 8351 | 8357 | 8363 | 8370 | 8376 | 8382 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 69 | 8388 | 8395 | 8401 | 8407 | 8414 | 8420 | 8426 | 8432 | 8439 | 8445 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 70 | 8451 | 8457 | 8463 | 8470 | 8476 | 8482 | 8488 | 8494 | 8500 | 8506 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 71 | 8513 | 8519 | 8525 | 8531 | 8537 | 8543 | 8549 | 8555 | 8561 | 8567 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 72 | 8573 | 8579 | 8585 | 8591 | 8597 | 8603 | 8609 | 8615 | 8621 | 8627 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 73 | 8633 | 8639 | 8645 | 8651 | 8657 | 8663 | 8669 | 8675 | 8681 | 8686 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 74 | 8692 | 8698 | 8704 | 8710 | 8716 | 8722 | 8727 | 8733 | 8739 | 8745 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 75 | 8751 | 8756 | 8762 | 8768 | 8774 | 8779 | 8785 | 8791 | 8797 | 8802 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 76 | 8808 | 8814 | 8820 | 8825 | 8831 | 8837 | 8842 | 8848 | 8854 | 8859 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 77 | 8865 | 8871 | 8876 | 8882 | 8887 | 8893 | 8899 | 8904 | 8910 | 8915 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 78 | 8921 | 8927 | 8932 | 8938 | 8943 | 8949 | 8954 | 8960 | 8965 | 8971 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 79 | 8976 | 8982 | 8987 | 8993 | 8998 | 9004 | 9009 | 9015 | 9020 | 9025 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 80 | 9031 | 9036 | 9042 | 9047 | 9053 | 9058 | 9063 | 9069 | 9074 | 9079 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 81 | 9085 | 9090 | 9096 | 9101 | 9106 | 9112 | 9117 | 9122 | 9128 | 9133 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 82 | 9138 | 9143 | 9149 | 9154 | 9159 | 9165 | 9170 | 9175 | 9180 | 9186 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 83 | 9191 | 9196 | 9201 | 9206 | 9212 | 9217 | 9222 | 9227 | 9232 | 9238 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 84 | 9243 | 9248 | 9253 | 9258 | 9263 | 9269 | 9274 | 9279 | 9284 | 9289 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 85 | 9294 | 9299 | 9304 | 9309 | 9315 | 9320 | 9325 | 9330 | 9335 | 9340 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 86 | 9345 | 9350 | 9355 | 9360 | 9365 | 9370 | 9375 | 9380 | 9385 | 9390 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 87 | 9395 | 9400 | 9405 | 9410 | 9415 | 9420 | 9425 | 9430 | 9435 | 9440 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 88 | 9445 | 9450 | 9455 | 9460 | 9465 | 9469 | 9474 | 9479 | 9484 | 9489 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 89 | 9494 | 9499 | 9504 | 9509 | 9513 | 9518 | 9523 | 9528 | 9533 | 9538 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 90 | 9542 | 9547 | 9552 | 9557 | 9562 | 9566 | 9571 | 9576 | 9581 | 9586 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 91 | 9590 | 9595 | 9600 | 9605 | 9609 | 9614 | 9619 | 9624 | 9628 | 9633 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 92 | 9638 | 9643 | 9647 | 9652 | 9657 | 9661 | 9666 | 9671 | 9675 | 9680 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 93 | 9685 | 9689 | 9694 | 9699 | 9703 | 9708 | 9713 | 9717 | 9722 | 9727 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 94 | 9731 | 9736 | 9741 | 9745 | 9750 | 9754 | 9759 | 9763 | 9768 | 9773 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 95 | 9777 | 9782 | 9786 | 9791 | 9795 | 9800 | 9805 | 9809 | 9814 | 9818 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 96 | 9823 | 9827 | 9832 | 9836 | 9841 | 9845 | 9850 | 9854 | 9859 | 9863 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 97 | 9868 | 9872 | 9877 | 9881 | 9886 | 9890 | 9894 | 9899 | 9903 | 9908 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 98 | 9912 | 9917 | 9921 | 9926 | 9930 | 9934 | 9939 | 9943 | 9948 | 9952 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 99 | 9956 | 9961 | 9965 | 9969 | 9974 | 9978 | 9983 | 9987 | 9997 | 9996 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |

ANTILOGARITHMS

TABLE II

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|-----|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| .00 | 1000 | 1002 | 1005 | 1007 | 1009 | 1012 | 1014 | 1016 | 1019 | 1021 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| .01 | 1023 | 1026 | 1028 | 1030 | 1033 | 1035 | 1038 | 1040 | 1042 | 1045 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| .02 | 1047 | 1050 | 1052 | 1054 | 1057 | 1059 | 1062 | 1064 | 1067 | 1069 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| .03 | 1072 | 1074 | 1076 | 1079 | 1081 | 1084 | 1086 | 1089 | 1091 | 1094 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| .04 | 1096 | 1099 | 1102 | 1104 | 1107 | 1109 | 1112 | 1114 | 1117 | 1119 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| .05 | 1122 | 1125 | 1127 | 1130 | 1132 | 1135 | 1138 | 1140 | 1143 | 1146 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| .06 | 1148 | 1151 | 1153 | 1156 | 1159 | 1161 | 1164 | 1167 | 1169 | 1172 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| .07 | 1175 | 1178 | 1180 | 1183 | 1186 | 1189 | 1191 | 1194 | 1197 | 1199 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| .08 | 1202 | 1205 | 1208 | 1211 | 1213 | 1216 | 1219 | 1222 | 1225 | 1227 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .09 | 1230 | 1233 | 1236 | 1239 | 1242 | 1245 | 1247 | 1250 | 1253 | 1256 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .10 | 1259 | 1262 | 1265 | 1268 | 1271 | 1274 | 1276 | 1279 | 1282 | 1285 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .11 | 1288 | 1291 | 1294 | 1297 | 1300 | 1303 | 1306 | 1309 | 1312 | 1315 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .12 | 1318 | 1321 | 1324 | 1327 | 1330 | 1334 | 1337 | 1340 | 1343 | 1346 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .13 | 1349 | 1352 | 1355 | 1358 | 1361 | 1365 | 1368 | 1371 | 1374 | 1377 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .14 | 1380 | 1384 | 1387 | 1390 | 1393 | 1396 | 1400 | 1403 | 1406 | 1409 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .15 | 1413 | 1416 | 1419 | 1422 | 1426 | 1429 | 1432 | 1435 | 1439 | 1442 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .16 | 1445 | 1449 | 1452 | 1455 | 1459 | 1462 | 1466 | 1469 | 1472 | 1476 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .17 | 1479 | 1483 | 1486 | 1489 | 1493 | 1496 | 1500 | 1503 | 1507 | 1510 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .18 | 1514 | 1517 | 1521 | 1524 | 1528 | 1531 | 1535 | 1538 | 1542 | 1545 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| .19 | 1549 | 1552 | 1556 | 1560 | 1563 | 1567 | 1570 | 1574 | 1578 | 1581 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 3 |
| .20 | 1585 | 1589 | 1592 | 1596 | 1600 | 1603 | 1607 | 1611 | 1614 | 1618 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 3 |
| .21 | 1622 | 1626 | 1629 | 1633 | 1637 | 1641 | 1644 | 1648 | 1652 | 1656 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 3 |
| .22 | 1660 | 1663 | 1667 | 1671 | 1675 | 1679 | 1683 | 1687 | 1690 | 1694 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 3 |
| .23 | 1698 | 1702 | 1706 | 1710 | 1714 | 1718 | 1722 | 1726 | 1730 | 1734 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .24 | 1738 | 1742 | 1746 | 1750 | 1754 | 1758 | 1762 | 1766 | 1770 | 1774 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .25 | 1778 | 1782 | 1786 | 1791 | 1795 | 1799 | 1803 | 1807 | 1811 | 1816 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .26 | 1820 | 1824 | 1828 | 1832 | 1837 | 1841 | 1845 | 1849 | 1854 | 1858 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .27 | 1862 | 1866 | 1871 | 1875 | 1879 | 1884 | 1888 | 1892 | 1897 | 1901 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .28 | 1905 | 1910 | 1914 | 1919 | 1923 | 1928 | 1932 | 1936 | 1941 | 1945 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .29 | 1950 | 1954 | 1959 | 1963 | 1968 | 1972 | 1977 | 1982 | 1986 | 1991 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .30 | 1995 | 2000 | 2004 | 2009 | 2014 | 2018 | 2023 | 2028 | 2032 | 2037 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .31 | 2042 | 2046 | 2051 | 2056 | 2061 | 2065 | 2070 | 2075 | 2080 | 2084 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .32 | 2089 | 2094 | 2099 | 2104 | 2109 | 2113 | 2118 | 2123 | 2128 | 2133 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .33 | 2138 | 2143 | 2148 | 2153 | 2158 | 2163 | 2168 | 2173 | 2178 | 2183 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 4 |
| .34 | 2188 | 2193 | 2198 | 2203 | 2208 | 2213 | 2218 | 2223 | 2228 | 2234 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| .35 | 2239 | 2244 | 2249 | 2254 | 2259 | 2265 | 2270 | 2275 | 2280 | 2286 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| .36 | 2291 | 2296 | 2301 | 2307 | 2312 | 2317 | 2323 | 2328 | 2333 | 2339 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| .37 | 2344 | 2350 | 2355 | 2360 | 2366 | 2371 | 2377 | 2382 | 2388 | 2393 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| .38 | 2399 | 2404 | 2410 | 2415 | 2421 | 2427 | 2432 | 2438 | 2443 | 2449 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| .39 | 2455 | 2460 | 2466 | 2472 | 2477 | 2483 | 2489 | 2495 | 2500 | 2506 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| .40 | 2512 | 2518 | 2523 | 2529 | 2535 | 2541 | 2547 | 2553 | 2559 | 2564 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| .41 | 2570 | 2576 | 2582 | 2588 | 2594 | 2600 | 2606 | 2612 | 2618 | 2624 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| .42 | 2630 | 2636 | 2642 | 2649 | 2655 | 2661 | 2667 | 2673 | 2679 | 2685 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| .43 | 2692 | 2698 | 2704 | 2710 | 2716 | 2723 | 2729 | 2735 | 2742 | 2748 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| .44 | 2754 | 2761 | 2767 | 2773 | 2780 | 2786 | 2793 | 2799 | 2805 | 2812 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| .45 | 2818 | 2825 | 2831 | 2838 | 2844 | 2851 | 2858 | 2864 | 2871 | 2877 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| .46 | 2884 | 2891 | 2897 | 2904 | 2911 | 2917 | 2924 | 2931 | 2938 | 2944 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| .47 | 2951 | 2958 | 2965 | 2972 | 2979 | 2985 | 2992 | 2999 | 3006 | 3013 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| .48 | 3020 | 3027 | 3034 | 3041 | 3048 | 3055 | 3062 | 3069 | 3076 | 3083 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |
| .49 | 3090 | 3097 | 3105 | 3112 | 3119 | 3126 | 3133 | 3141 | 3148 | 3155 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |

ANTILOGARITHMS

TABLE II (Continued)

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|-----|------|------|------|------|------|------|------|------|------|------|---|---|---|---|----|----|----|----|----|
| .50 | 3162 | 3170 | 3177 | 3184 | 3192 | 3199 | 3206 | 3214 | 3221 | 3228 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| .51 | 3236 | 3243 | 3251 | 3258 | 3266 | 3273 | 3281 | 3289 | 3296 | 3304 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| .52 | 3311 | 3319 | 3327 | 3334 | 3342 | 3350 | 3357 | 3365 | 3373 | 3381 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| .53 | 3388 | 3396 | 3404 | 3412 | 3420 | 3428 | 3436 | 3443 | 3451 | 3459 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| .54 | 3467 | 3475 | 3483 | 3491 | 3499 | 3508 | 3516 | 3524 | 3532 | 3540 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| .55 | 3548 | 3556 | 3565 | 3573 | 3581 | 3589 | 3597 | 3606 | 3614 | 3622 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 7 | 7 |
| .56 | 3631 | 3639 | 3648 | 3656 | 3664 | 3673 | 3681 | 3690 | 3698 | 3707 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| .57 | 3715 | 3724 | 3733 | 3741 | 3750 | 3758 | 3767 | 3776 | 3784 | 3793 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| .58 | 3802 | 3811 | 3819 | 3828 | 3837 | 3846 | 3855 | 3864 | 3873 | 3882 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 8 |
| .59 | 3890 | 3899 | 3908 | 3917 | 3926 | 3936 | 3945 | 3954 | 3963 | 3972 | 1 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 8 |
| .60 | 3981 | 3990 | 3999 | 4009 | 4018 | 4027 | 4036 | 4046 | 4055 | 4064 | 1 | 2 | 3 | 4 | 5 | 6 | 6 | 7 | 8 |
| .61 | 4074 | 4083 | 4093 | 4102 | 4111 | 4121 | 4130 | 4140 | 4150 | 4159 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| .62 | 4169 | 4178 | 4188 | 4198 | 4207 | 4217 | 4227 | 4236 | 4246 | 4256 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| .63 | 4266 | 4276 | 4285 | 4295 | 4305 | 4315 | 4325 | 4335 | 4345 | 4355 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| .64 | 4365 | 4375 | 4385 | 4395 | 4406 | 4416 | 4426 | 4436 | 4446 | 4457 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| .65 | 4467 | 4477 | 4487 | 4498 | 4508 | 4519 | 4529 | 4539 | 4550 | 4560 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| .66 | 4571 | 4581 | 4592 | 4603 | 4613 | 4624 | 4634 | 4645 | 4656 | 4667 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 9 | 10 |
| .67 | 4677 | 4688 | 4699 | 4710 | 4721 | 4732 | 4742 | 4753 | 4764 | 4775 | 1 | 2 | 3 | 4 | 5 | 7 | 8 | 9 | 10 |
| .68 | 4786 | 4797 | 4808 | 4819 | 4831 | 4842 | 4853 | 4864 | 4875 | 4887 | 1 | 2 | 3 | 4 | 6 | 7 | 8 | 9 | 10 |
| .69 | 4898 | 4909 | 4920 | 4932 | 4943 | 4955 | 4966 | 4977 | 4989 | 5000 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9 | 10 |
| .70 | 5012 | 5023 | 5035 | 5047 | 5058 | 5070 | 5082 | 5093 | 5105 | 5117 | 1 | 2 | 4 | 5 | 6 | 7 | 8 | 9 | 11 |
| .71 | 5129 | 5140 | 5152 | 5164 | 5176 | 5188 | 5200 | 5212 | 5224 | 5236 | 1 | 2 | 4 | 5 | 6 | 7 | 8 | 10 | 11 |
| .72 | 5248 | 5260 | 5272 | 5284 | 5297 | 5309 | 5321 | 5333 | 5346 | 5358 | 1 | 2 | 4 | 5 | 6 | 7 | 9 | 10 | 11 |
| .73 | 5370 | 5383 | 5395 | 5408 | 5420 | 5433 | 5445 | 5458 | 5470 | 5483 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 11 |
| .74 | 5495 | 5508 | 5521 | 5534 | 5546 | 5559 | 5572 | 5585 | 5598 | 5610 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 12 |
| .75 | 5623 | 5636 | 5649 | 5662 | 5675 | 5689 | 5702 | 5715 | 5728 | 5741 | 1 | 3 | 4 | 5 | 7 | 8 | 9 | 10 | 12 |
| .76 | 5754 | 5768 | 5781 | 5794 | 5808 | 5821 | 5834 | 5848 | 5861 | 5875 | 1 | 3 | 4 | 5 | 7 | 8 | 9 | 11 | 12 |
| .77 | 5888 | 5902 | 5916 | 5929 | 5943 | 5957 | 5970 | 5984 | 5998 | 6012 | 1 | 3 | 4 | 5 | 7 | 8 | 10 | 11 | 12 |
| .78 | 6026 | 6039 | 6053 | 6067 | 6081 | 6095 | 6109 | 6124 | 6138 | 6152 | 1 | 3 | 4 | 6 | 7 | 8 | 10 | 11 | 13 |
| .79 | 6166 | 6180 | 6194 | 6209 | 6223 | 6237 | 6252 | 6266 | 6281 | 6295 | 1 | 3 | 4 | 6 | 7 | 9 | 10 | 11 | 13 |
| .80 | 6310 | 6324 | 6339 | 6353 | 6368 | 6383 | 6397 | 6412 | 6427 | 6442 | 1 | 3 | 4 | 6 | 7 | 9 | 10 | 12 | 13 |
| .81 | 6457 | 6471 | 6486 | 6501 | 6516 | 6531 | 6546 | 6561 | 6577 | 6592 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 12 | 14 |
| .82 | 6607 | 6622 | 6637 | 6653 | 6668 | 6683 | 6699 | 6714 | 6730 | 6745 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 12 | 14 |
| .83 | 6761 | 6776 | 6792 | 6808 | 6823 | 6839 | 6855 | 6871 | 6887 | 6902 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 13 | 14 |
| .84 | 6918 | 6934 | 6950 | 6966 | 6982 | 6998 | 7015 | 7031 | 7047 | 7063 | 2 | 3 | 5 | 6 | 8 | 10 | 11 | 13 | 15 |
| .85 | 7079 | 7096 | 7112 | 7129 | 7145 | 7161 | 7178 | 7194 | 7211 | 7228 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 13 | 15 |
| .86 | 7244 | 7261 | 7278 | 7295 | 7311 | 7328 | 7345 | 7362 | 7379 | 7396 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 13 | 15 |
| .87 | 7413 | 7430 | 7447 | 7464 | 7482 | 7499 | 7516 | 7534 | 7551 | 7568 | 2 | 3 | 5 | 7 | 9 | 10 | 12 | 14 | 16 |
| .88 | 7586 | 7603 | 7621 | 7638 | 7656 | 7674 | 7691 | 7709 | 7727 | 7745 | 2 | 4 | 5 | 7 | 9 | 11 | 12 | 14 | 16 |
| .89 | 7762 | 7780 | 7798 | 7816 | 7834 | 7852 | 7870 | 7889 | 7907 | 7925 | 2 | 4 | 5 | 7 | 9 | 11 | 13 | 14 | 16 |
| .90 | 7943 | 7962 | 7980 | 7998 | 8017 | 8035 | 8054 | 8072 | 8091 | 8110 | 2 | 4 | 6 | 7 | 9 | 11 | 13 | 15 | 17 |
| .91 | 8128 | 8147 | 8166 | 8185 | 8204 | 8222 | 8241 | 8260 | 8279 | 8299 | 2 | 4 | 6 | 8 | 9 | 11 | 13 | 15 | 17 |
| .92 | 8318 | 8337 | 8356 | 8375 | 8395 | 8414 | 8433 | 8453 | 8472 | 8492 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 15 | 17 |
| .93 | 8511 | 8531 | 8551 | 8570 | 8590 | 8610 | 8630 | 8650 | 8670 | 8690 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| .94 | 8710 | 8730 | 8750 | 8770 | 8790 | 8810 | 8831 | 8851 | 8872 | 8892 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| .95 | 8913 | 8933 | 8954 | 8974 | 8995 | 9016 | 9036 | 9057 | 9078 | 9099 | 2 | 4 | 6 | 8 | 10 | 12 | 15 | 17 | 19 |
| .96 | 9120 | 9141 | 9162 | 9183 | 9204 | 9226 | 9247 | 9268 | 9290 | 9311 | 2 | 4 | 6 | 8 | 11 | 13 | 15 | 17 | 19 |
| .97 | 9333 | 9354 | 9376 | 9397 | 9419 | 9441 | 9462 | 9484 | 9506 | 9528 | 2 | 4 | 7 | 9 | 11 | 13 | 15 | 17 | 20 |
| .98 | 9550 | 9572 | 9594 | 9616 | 9638 | 9661 | 9683 | 9705 | 9727 | 9750 | 2 | 4 | 7 | 9 | 11 | 13 | 16 | 18 | 20 |
| .99 | 9772 | 9795 | 9817 | 9840 | 9863 | 9886 | 9908 | 9931 | 9954 | 9977 | 2 | 5 | 7 | 9 | 11 | 14 | 16 | 18 | 20 |