CHAPTER 9 – SIMPLE AND COMPOUND INTEREST

Question 1.

Find the interest and the amount on:

(i) ₹ 750 in 3 years 4 months at 10% per annum.

Solution:

Given P = ₹ 750

Time (T) = $3\frac{4}{12} = 3\frac{1}{3} = \frac{10}{3}$ years

Rate (R)=10%

Interest
$$(I) = \frac{PRT}{100} = \frac{750 \times 10 \times \frac{10}{8}}{100}$$

$$\frac{250 \times 10 \times 10}{100} = 250$$

(ii) ₹ 5000 at 8% per year from 23rd December 2011 to 29th July 2012.

Solution:

Principal (P) = ₹ 5000

Rate (R) = 8% p.a

Time (T) = 23 December 2011 to 29 July 2012

Dec. Jan. Feb. March April May June July

8 31 29 31 30 31 30 29

Total 219 days = $\frac{219}{365}$ Years

$$\therefore \text{ Interest} = \frac{PRT}{100} = \frac{5000 \times 8 \times 219}{100 \times 365}$$

$$=10 \times 8 \times 3 = 240$$

∴Amount = P + I = ₹ 5000 + 240 = ₹ 5240

(iii) ₹ 2,600 in 2 years 3months at 1% per month.

Solution:

Here p = ₹ 2600

Time (T) = 2 Years 3 month = 27 months

Rate (R) = 1 per month

 $\therefore \text{ Interest} = \frac{P \times T \times R}{100} = \frac{2600 \times 27 \times 1}{100}$

 $=26 \times 27 = Rs.702$

: Amount = (2600+702) = Rs.3302

(iv) ₹ 4,000 in $1\frac{1}{3}$ years at 2 paise per rupee per month.

Solution:

Here P = Rs. 4.000, Time (T) = $1\frac{1}{3}$ year

= 1 year $+\frac{12}{3}$ months = 16 months

Rate (R) = 2 paise per rupee per month = 2% per month

: Interest (I) = $\frac{P \times T \times R}{100} = \frac{4,000 \times 2 \times 16}{100} = 40 \times 32 = \text{Rs.} 1280$

∴ Amount (A) =P + 1 = Rs. 4000 + Rs. 1280 = Rs. 5280

Question 2

Rohit borrowed Rs. 24,000 at 7.5percent per year. How much money will he pay at the end of 4th years to clear his debt?

Solution:

Principal (P) = Rs.24000

Rate (R) = 7.5% P.A.

Time (T) = 4 Years

S.I. =
$$\frac{P \times T \times R}{100}$$

= Rs. $\frac{24,000 \times 4 \times 7.5}{100}$

= Rs. 240 × 4 × 7.5

$= 240 \times 30 =$ Rs. 7200

Amount needed to clear the debt at the end of $4^{\mbox{\tiny th}}$ year

= Rs.24000 + Rs.7200 = Rs.3,1200

Question 3.

The interest on a certain sum of money is Rs. 1,480 in 2 years and at 10 per cent per year. Find the sum of money.

Solution:

Let P = Rs. X Time (T) = 2 Years Rate (R) = 0% \therefore Interest = $\frac{P \times T \times R}{100} = \frac{x \times 10 \times 2}{100} = \frac{x}{5}$ $\frac{x}{5} = Rs. 1480$ (Given) $\therefore x = 1480 \times 5 = Rs. 7400$ Hence the money Rs.7400

Question 4.

On what principal will the simple interest be Rs. 7,008 in 6 years 3 months at 5% per year?

Solution:

Let principal = Rs.P

Time (T) = 6 Years 3 month = 6 Year $\frac{3}{12}$

Year
$$=\frac{75}{12}=\frac{25}{4}$$
 year $=6\frac{1}{4}$ years

Rate (R) = 5%

Simple interest = Rs. 7,008

We know that

Simple interest = $\frac{P \times T \times R}{100}$

$$7,008 = \frac{P \times \frac{25}{4} \times 5}{100} \Rightarrow P = \frac{7008 \times 100 \times 4}{25 \times 5}$$
$$= \frac{7008 \times 16}{5} = \frac{112128}{5} = \text{Rs. } 22425.60$$

Question 5.

Find the principal which will amount to Rs. 4,000 in 4 years at 6.25% per annum.

Solution:

Let Principal = Rs P, Time (T) = 4 Years Rate = $6\frac{1}{4} = \frac{25}{4}\%$ Simple Interest = $\frac{P \times T \times R}{100} = \frac{P \times \frac{25}{4} \times 4}{100} = \frac{P}{4}$ \therefore Amount = $P + \frac{P}{4} = \frac{5P}{4}$ $\frac{5P}{4} = 4000$ $\Rightarrow 5P = 4 \times 4000$ $\Rightarrow P = Rs. 3200$

Hence Principal = Rs.3200

Question 6.

(i) At what rate per cent per annum will Rs. 630 produce an interest of Rs. 126 in 4 years?

Solution:

P = Rs. 630, I = Rs. 126, T = 4

$$R = \frac{100 \times I}{P \times T} = \frac{100 \times 126}{630 \times 4} = \frac{100}{20} = 5\%$$

(ii) At what rate per cent per year will a sum double itself in $6\frac{1}{4}$ years?

Solution:

Let P = Rs.100

: Amount = 2 × Rs.100 = Rs.100

Interest = A-P
= Rs.200 - Rs.100 = Rs.100
T =
$$6\frac{1}{4}$$
 years = $\frac{25}{4}$ years
R = $\frac{100 \times I}{P \times T} = \frac{100 \times 100}{100 \times \frac{25}{10}}\% = \frac{100 \times 100}{100} \times \frac{4}{25} = 16\%$

Question 7.

(i) In how many years will Rs. 950 produce Rs. 399 as simple interest at 7%?

Solution:

P = Rs.950 S.I = Rs.3900 R = 7% We know that: T = $\frac{100 \times I}{P \times R} = \frac{100 \times 399}{950 \times 7}$ = $\frac{10 \times 21}{5 \times 7} = 2 \times 3 = 6$ Years

(ii) Find the time in which Rs. 1200 will amount to Rs. 1536 at 3.5% per year.

Solution:

A = Rs.1536

P = Rs.1200

I = A - P

= Rs.1536 - Rs.1200 = Rs.336

We know that

 $T = \frac{100 \times I}{P \times R}$ (Formula) = $\frac{100 \times 336}{1200 \times 3.5} = \frac{100 \times 336 \times 10}{1200 \times 35}$ [$\because \frac{1}{3.5} = \frac{10}{35}$]

$$=\frac{28\times10}{35}=8 Years$$

Question 8.

The simple interest on a certain sum of money is $\frac{3}{8}$ of the sum in 64 years. Find the rate percent charged.

Solution:

Let P = RS.8

$$S.I = Rs.\frac{3}{8} \times 8$$

= Rs.3

$$T = 6\frac{1}{4}$$
 years $= \frac{25}{4}$ Years

We know that:

$$R = \frac{100 \times 1}{P \times T}$$
$$= \frac{100 \times 3}{8 \times \frac{25}{4}} = \frac{100 \times 3}{8} \times \frac{4}{25} = 2 \times 3$$
 (Formula)

= 6%

Question 9.

What sum of money borrowed on 24th May will amount to Rs.10210.20 on 17th October of the same year at 5 percent per annum simple interest?

Solution:

A = Rs.10210.20

R = 5% P.A

T = May + June+ July + August + Sept +Oct

$$=\frac{146}{365}$$
 days $=\frac{2}{5}$ Year

We know that:

P + I = A

(Formula for finding principal)

$$\Rightarrow P + \frac{P \times R \times T}{100} = A$$

$$\Rightarrow P\left(1 + \frac{5 \times \frac{2}{5}}{100}\right) = Rs. 10210 \cdot 2$$

$$\Rightarrow P\left(1 + \frac{R \times T}{100}\right) = A$$

$$\Rightarrow P\left(1 + \frac{2}{100}\right) = Rs. 10210 \cdot 20$$

$$\Rightarrow P\left(\frac{102}{100}\right) = Rs. 10210 \cdot 20$$

$$\Rightarrow P = Rs. 10210 \cdot 20 \times \frac{100}{102}$$

$$\Rightarrow P = Rs. \frac{1021020}{102}$$

$$\Rightarrow P = Rs. \frac{1021020}{102}$$

... Money to be borrowed = Rs.10010

Question 10.

In what time will the interest on a certain sum of money at 6% be $\frac{5}{8}$ of itself?

Solution:

Let P = Rs.8

Interest = $Rs.8\frac{5}{8}$ = Rs.5 (Converting the mixed fraction into normal one)

$$R = 6\%$$

$$T = \frac{100 \times 1}{P \times R}$$

$$= \frac{100 \times 5}{8 \times 6}$$

$$= \frac{500}{48} = \frac{125}{12} \text{ Years}$$

$$= 10\frac{5}{12} \text{ Years}$$

= 10 Years 5 months

$$\left[::\frac{5}{12} \text{ year } = \frac{5}{12} \times 12 \text{ months } = 5 \text{ months}\right]$$

Time = 10 years 5 months

