

Exercise 13.3

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1. Diameter of the base of a cone is 10.5 cm and its slant height is 10 cm. Find its curved surface area (Assume $\pi = 22/7$)

Solution:

Radius of the base of cone = diameter / 2 = $(10.5/2)$ cm = 5.25 cm
Slant height of cone, say $l = 10$ cm
CSA of cone is = $\pi r l$
= $(22/7 \times 5.25 \times 10) = 165$
Therefore, the curved surface area of the cone is 165 cm².

2. Find the total surface area of a cone, if its slant height is 21 m and diameter of its base is 24 m. (Assume $\pi = 22/7$)

Solution:

Radius of cone, $r = 24/2$ m = 12m

Slant height, $l = 21$ m

Formula: Total Surface area of the cone = $\pi r(l + r)$

Total Surface area of the cone = $22/7 \times 12 \times (21 + 12)$ m²
= 1244.57m²

3. Curved surface area of a cone is 308 cm² and its slant height is 14 cm. Find (i) radius of the base and (ii) total surface area of the cone. (Assume $\pi=22/7$)

Solution:

Slant height of cone, $l = 14$ cm

Let the radius of the cone be r .

(i) We know, CSA of cone = $\pi r l$

Given: Curved surface area of a cone is 308 cm²

$$(308) = (22/7 \times r \times 14)$$

$$308 = 44 r$$

$$r = 308/44 = 7$$

Radius of a cone base is 7 cm.

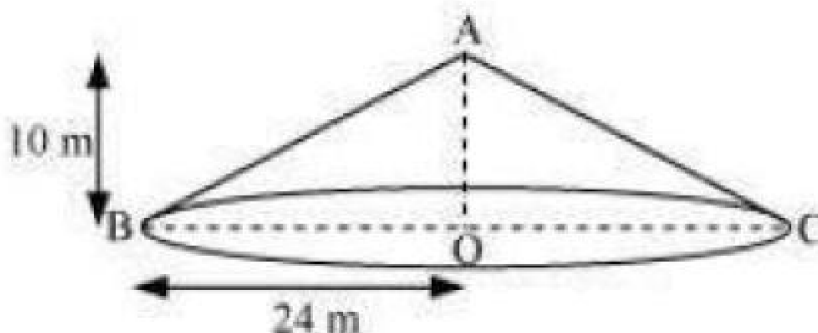
(ii) Total surface area of cone = CSA of cone + Area of base (πr^2)

$$\text{Total surface area of cone} = 308 + 22/7 \times 7^2 = 308 + 154$$

Therefore, the total surface area of the cone is 462 cm².

4. A conical tent is 10 m high and the radius of its base is 24 m. Find (i) slant height of the tent. (ii) cost of the canvas required to make the tent, if the cost of 1 m² canvas is Rs 70. (Assume $\pi=22/7$)

Solution:



Let ABC be a conical tent

Height of conical tent, $h = 10$ m

Radius of conical

tent, $r = 24$ m

Let the slant height of the tent be l .

(i) In right triangle, ABO,

$$AB^2 = AO^2 + BO^2 \text{ (using Pythagoras theorem)}$$

$$l^2 = h^2 + r^2$$

$$= (10)^2 + (24)^2$$

$$= 676$$

$$l = 26$$

Therefore, the slant height of the tent is 26 m.

(ii) CSA of tent = πrl

$$= (22/7 \times 24 \times 26) \text{ m}^2$$

Cost of 1 m^2 canvas = Rs 70

Cost of $(13728/7) \text{m}^2$ canvas is equal to Rs $(13728/7) \times 70 = \text{Rs } 137280$

Therefore, the cost of the canvas required to make such a tent is Rs 137280.

- 5. What length of tarpaulin 3 m wide will be required to make conical tent of height 8 m and base radius 6m? Assume that the extra length of material that will be required for stitching margins and wastage in cutting is approximately 20 cm. [Use $\pi=3.14$]**

Solution:

Height of conical tent, $h = 8$ m

Radius of base of tent, $r = 6$ m

Slant height of tent, $l^2 = (r^2 + h^2)$

$$l^2 = (6^2 + 8^2) = (36 + 64) = (100)$$

$$\text{or } l = 10$$

Again, CSA of conical tent = πrl

$$= (3.14 \times 6 \times 10) \text{ m}^2$$

$$= 188.4 \text{ m}^2$$

Let the length of tarpaulin sheet required be L

As 20 cm will be wasted, therefore,

Effective length will be $(L - 0.2 \text{ m})$.

Breadth of tarpaulin = 3m (given)

Area of sheet = CSA of tent

$$[(L - 0.2) \times 3] = 188.4$$

$$L - 0.2 = 62.8$$

$$L = 63$$

Therefore, the length of the required tarpaulin sheet will be 63m.

6. The slant height and base diameter of conical tomb are 25 m and 14 m respectively. Find the cost of white-washing its curved surface at the rate of Rs. 210 per 100 m². (Assume $\pi = 22/7$)

Solution:

Slant height of conical tomb, $l = 25\text{m}$
 Base radius, $r = \text{diameter}/2 = 14/2 \text{ m} = 7\text{m}$
 CSA of conical tomb $= \pi r l$
 $= 22/7 \times 7 \times 25 = 550$

CSA of conical tomb $= 550\text{m}^2$
 Cost of white-washing 550 m² area, which is Rs $(210 \times 550)/100$
 $= \text{Rs. } 1155$
 Therefore, cost will be Rs. 1155 while white-washing tomb.

6. A joker's cap is in the form of right circular cone of base radius 7 cm and height 24 cm. Find the area of the sheet required to make 10 such caps. (Assume $\pi=22/7$)

Solution:

Radius of conical cap, $r = 7 \text{ cm}$
 Height of conical cap, $h = 24 \text{ cm}$
 Slant height, $l^2 = (r^2 + h^2)$
 $= (7^2 + 24^2)$
 $= (49 + 576)$
 $= (625)$
 Or $l = 25 \text{ cm}$
 CSA of 1 conical cap $= \pi r l$
 $= 22/7 \times 7 \times 24$
 $= 550$
 CSA of 10 caps $= (10 \times 550) \text{ cm}^2 = 5500 \text{ cm}^2$
 Therefore, the area of the sheet required to make 10 such caps is 5500 cm².

7. A bus stop is barricaded from the remaining part of the road, by using 50 hollow cones made of recycled cardboard. Each cone has a base diameter of 40 cm and height 1 m. If the outer side of each of the cones is to be painted and the cost of painting is Rs. 12 per m², what will be the cost of painting all these cones? (Use $\pi = 3.14$ and take $\sqrt{(1.04)} = 1.02$)

Solution:

Given:
 Radius of cone, $r = \text{diameter}/2 = 40/2 \text{ cm} = 20 \text{ cm} = 0.2 \text{ m}$
 Height of cone, $h = 1 \text{ m}$

Slant height of cone

is l , and $l^2 = (r^2 + h^2)$

Using given values, $l^2 = (0.2^2 + 1^2)$

$= (1.04)$

Or $l = 1.02$

Slant height of the cone is 1.02 m

Now,

CSA of each cone $= \pi rl$

$= (3.14 \times 0.2 \times 1.02)$

$= 0.64056$

CSA of 50 such cones $= (50 \times 0.64056) = 32.028$

CSA of 50 such cones $= 32.028 \text{ m}^2$

Again,

Cost of painting 1 m^2 area $= \text{Rs } 12$ (given)

Cost of painting 32.028 m^2 area $= \text{Rs } (32.028 \times 12)$

$= \text{Rs. } 384.336$

$= \text{Rs. } 384.34$ (approximately)

Therefore, the cost of painting all these cones is Rs. 384.34.