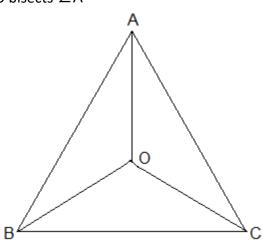


Exercise: 7.2

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1. In an isosceles triangle ABC, with AB = AC, the bisectors of $\angle B$ and \triangle intersect each other at O. Join A to O. Show that :

(i) OB = OC (ii) AO bisects $\angle A$



Solution:

Given:

-> AB = AC and

-> the bisectors of $\angle B$ and $\triangle C$ intersect each other at O

- (i) Since ABC is an isosceles with AB = AC,
- =>∠B= ∠C

 $\Rightarrow 1/2 \Delta B = 1/2 \Delta C$

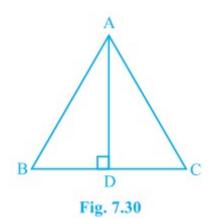
- $\Rightarrow \angle OBC = \angle OCB$ (Angle bisectors)
- \therefore OB = OC(Side opposite to the equal angles are equal.)

(ii) In $\triangle AOB$ and $\triangle AOC$, AB = AC (Given in the question) AO = AO (Common arm) OB = OC (As Proved Already) So, $\triangle AOB \cong \triangle AOC$ by SSS congruence condition. $\angle BAO = \angle CAO$ (by CPCT) Thus, AO bisects $\angle A$.

2. In \triangle ABC, AD is the perpendicular bisector of BC (see Fig. 7.30). Show that \triangle ABC is an isosceles triangle in which AB = AC.



NCERT Solutions For Class 9 Maths Chapter 7- Triangles



Solution:

It is given that AD is the perpendicular bisector of BC **To prove:** AB = AC **Proof:** In \triangle ADB and \triangle ADC, AD = AD (It is the Common arm) \angle ADB = \angle ADC BD = CD (Since AD is the perpendicular bisector) So, \triangle ADB $\cong \triangle$ ADC bySAS congruency criterion. AB = AC (by CPCT)

3. ABC is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see Fig. 7.31). Show that these altitudes are equal.

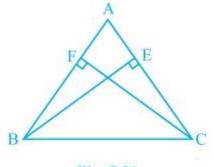


Fig. 7.31

Solution:

Given: (i) BE and CF are altitudes.

(ii) AC = AB

To prove:



BE = CF

Proof:

Triangles ΔAEB and ΔAFC are similar by AAS congruency since

 $\angle A = \angle A$ (It is the common arm)

 $\angle AEB = \angle AFC$ (They are right angles)

AB = AC (Given in the question)

 \therefore $\triangle AEB \cong \triangle AFC and so, BE = CF (by CPCT).$

4. ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (see Fig. 7.32). Show that

(i) $\triangle ABE \cong \triangle ACF$

(ii) AB = AC, i.e., ABC is an isosceles triangle.

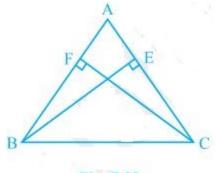


Fig. 7.32

Solution:

It is given that BE = CF

(i) In \triangle ABE and \triangle ACF,

 $\angle A = \angle A$ (It is the common angle)

 $\angle AEB = \angle AFC$ (They are right angles)

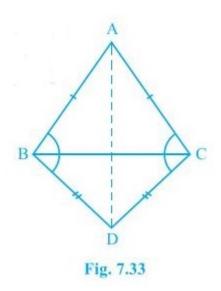
BE = CF (Given in the question)

 \therefore $\triangle ABE \cong \triangle ACF b AAS congruency condition.$

(ii) AB = AC by CPCT and so, ABC is an isosceles triangle.

5. ABC and DBC are two isosceles triangles on the same base BC (see Fig. 7.33). Show that $\angle ABD = \angle ACD$.





Solution:

In the question, it is given that ABC and DBC are two isosceles triangles.

We will have to show that $\angle ABD = \angle ACD$

Proof:

Triangles $\triangle ABD$ and $\triangle ACD$ are similar by SSS congruency since

AD = AD (It is the common arm)

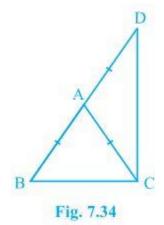
AB = AC (Since ABC is an isosceles triangle)

BD = CD (Since BCD is an isosceles triangle)

So, $\triangle ABD \cong \triangle ACD$.

 \therefore \triangle BD = \triangle CD by CPCT.

6. \triangle ABC is an isosceles triangle in which AB = AC. Side BA is produced to D such that AD = AB (see Fig. 7.34). Show that \angle BCD is a right angle.



Solution:



It is given that AB = AC and AD = AB We will have to now prove $\angle BCD$ is a right angle. Proof: Consider ∆ABC, AB = AC (It is given in the question) Also, $\angle ACB = \angle ABC$ (They are angles opposite to the equal sides and so, they are equal) Now, consider $\triangle ACD$, AD = ABAlso, $\angle ADC = \angle ACD$ (They are angles opposite to the equal sides and so, they are equal) Now, In ∆ABC, $\angle CAB + \angle ACB + \angle ABC = 180^{\circ}$ So. $\angle CAB + 2 \angle ACB = 180^{\circ}$ $\Rightarrow \angle CAB = 180^{\circ} 2 \angle ACB$ -- (i) Similarly in ∆ADC, \angle CAD = 180[°] 2 \angle ACD-- (ii) also, $\angle CAB + \angle CAD = 180^{\circ}$ (BD is a straight line.) Adding (i) and (ii) we get, $\angle CAB + \angle CAD = 180^{\circ} 2 \angle ACB + 180^{\circ} 2 \angle ACD$ \Rightarrow 180° = 360° - 2 \angle ACB 2 \angle ACD $\Rightarrow 2(ACB + ACD) = 180^{\circ}$ $\Rightarrow \angle BCD = 90^{\circ}$

7. ABC is a right-angled triangle in which $\angle A = 90^{\circ}$ and AB = AC. Find $\angle B$ and $\angle C$.

Solution:

In the question, it si given that $\angle A = 90^{\circ}$ and AB = AC

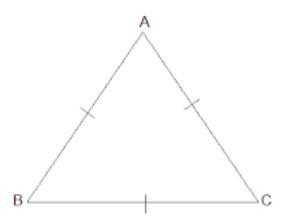


AB = AC ⇒ \pounds = \pounds (They are angles opposite to the equal sides and so, they are equal) Now, $\angle A + \pounds + \pounds = 180^{\circ}$ (Since the sum of the interior angles of the triangle) $\therefore 90^{\circ} + 2\pounds = 180^{\circ}$ ⇒ $2\pounds = 90^{\circ}$ ⇒ $\pounds = 45^{\circ}$ So, $\angle B = \pounds = 45^{\circ}$

8. Show that the angles of an equilateral triangle are 60° each.

Solution:

Let ABC be an equilateral triangle as shown below:



Here, BC = AC = AB (Since the length of all sides is same) $\Rightarrow A = A = A = A (Sides opposite to the equal angles are equal.)$ Also, we know that $\angle A + A + A = 180^{\circ}$ $\Rightarrow 3A = 180^{\circ}$ $\Rightarrow A = 60^{\circ}$ $\therefore A = A = A = A = 60^{\circ}$ So, the angles of an equilateral triangle are always 60° each.