

(Page No: 118) Exercise: 7.1

1. In quadrilateral ACBD, AC = AD and AB bisect $\angle A$ (see Fig. 7.16). Show that $\triangle ABC \cong \triangle ABD$. What can you say about BC and BD?

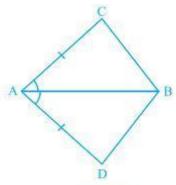


Fig. 7.16

Solution:

It is given that AC and AD are equal i.e. AC=AD and the line segment AB bisects \angle A. We will have to now prove that the two triangles ABC and ABD are similar i.e. \triangle ABC \cong \triangle ABD **Proof:**

Consider the triangles ΔABC and ΔABD,

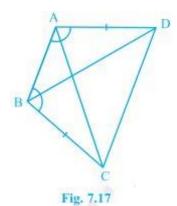
- (i) AC = AD (It is given in the question)
- (ii) AB = AB (Common)
- (iii) \angle CAB = \angle DAB (Since AB is the bisector of angle A)

So, by **SAS congruency criterion**, $\triangle ABC \cong \triangle ABD$.

For the 2nd part of the question, BC and BD are of equal lengths.

(Page No: 119)

- 2. ABCD is a quadrilateral in which AD = BC and ∠DAB = ∠CBA (see Fig. 7.17). Prove that
- (i) $\triangle ABD \cong \triangle BAC$
- (ii) BD = AC
- (iii) ∠ABD = ∠BAC.



Solution:

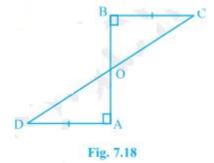
The given parameters from the questions are $\angle DAB = \angle CBA$ and AD = BC.

(i) ΔABD and ΔBAC are similar by SAS congruency as
AB = BA (It is the common arm)
∠DAB = ∠CBA and AD = BC (These are given in the question)
So, triangles ABD and BAC are similar i.e. ΔABD ≅ΔBAC. (Hence proved).

(ii) It is now known that $\triangle ABD \cong \triangle BAC$ so, BD = AC (by the rule of CPCT).

(iii) Since $\triangle ABD \cong \triangle BAC$ so, Angles $\angle ABD = \angle BAC$ (by the rule of CPCT).

3. AD and BC are equal perpendiculars to a line segment AB (see Fig. 7.18). Show that CD bisects AB.



Solution:

It is given that AD and BC are two equal perpendiculars to AB.

We will have to prove that CD is the bisector of AB

Proof:

Triangles $\triangle AOD$ and $\triangle BOC$ are similar by AAS congruency since:



- (i) $\angle A = \angle B$ (They are perpendiculars)
- (ii) AD = BC (As given in the question)
- (iii) ∠AOD = ∠BOC (They are vertically opposite angles)
- ∴ ΔAOD ≅ΔBOC.

So, AO = OB (by the rule of CPCT).

Thus, CD bisects AB (Hence proved).

4. I and m are two parallel lines intersected by another pair of parallel lines p and q (see Fig. 7.19). Show that \triangle ABC \cong \triangle CDA.

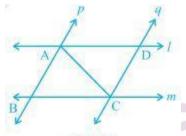


Fig. 7.19

Solution:

It is given that p || q and I || m

To prove:

Triangles ABC and CDA are similar i.e. ΔABC ≅ΔCDA

Proof:

Consider the ΔABC and ΔCDA,

- (i) \angle BCA = \angle DAC and \angle BAC = \angle DCA Since they are alternate interior angles
- (ii) AC = CA as it is the common arm

So, by **ASA congruency criterion** $\triangle ABC \cong \triangle CDA$.

5. Line I is the bisector of an angle $\angle A$ and B is any point on I. BP and BQ are perpendiculars from B to the arms of $\angle A$ (see Fig. 7.20). Show that:

- (i) ΔAPB ≅ΔAQB
- (ii) BP = BQ or B is equidistant from the arms of $\angle A$.

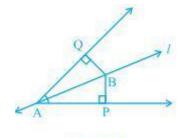


Fig. 7.20



Solution:

It is given that the line "I" is the bisector of angle ∠A and the line segments BP and BQ are perpendiculars drawn from I.

(i) \triangle APB and \triangle AQB are similar by AAS congruency because:

 $\angle P = \angle Q$ (They are the two right angles)

AB = AB (It is the common arm)

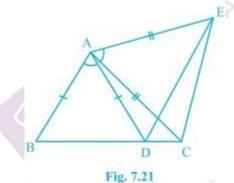
 $\angle BAP = \angle BAQ$ (As line I is the bisector of angle A)

So, $\triangle APB \cong \triangle AQB$.

(ii) By the rule of CPCT, BP = BQ. So, it can be said the point B is equidistant from the arms of $\angle A$.

(Page No: 120)

6. In Fig. 7.21, AC = AE, AB = AD and \angle BAD = \angle EAC. Show that BC = DE.



Solution:

It is given in the question that AB = AD, AC = AE, and $\angle BAD = \angle EAC$

To proof:

The line segment BC and DE are similar i.e. BC = DE

Proof:

We know that ∠BAD = ∠EAC

Now, by adding ∠DAC on both sides we get,

 $\angle BAD + \angle DAC = \angle EAC + \angle DAC$

This implies, ∠BAC = ∠EAD

Now, \triangle ABC and \triangle ADE are similar by SAS congruency since:

- (i) AC = AE (As given in the question)
- (ii) ∠BAC = ∠EAD

(iii) AB = AD (It is also given in the question)

∴ Triangles ABC and ADE are similar i.e. \triangle ABC \cong \triangle ADE.

So, by the rule of CPCT, it can be said that BC = DE.

7. AB is a line segment and P is its mid-point. D and E are points on the same side of AB such that \angle BAD = \angle ABE and \angle EPA = \angle DPB (see Fig. 7.22). Show that

- (i) ΔDAP ≅ΔEBP
- (ii) AD = BE

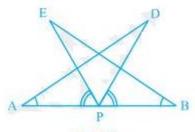


Fig. 7.22

Answer

In the question, it is given that P is the mid-point of line segment AB. Also, \angle BAD = \angle ABE and \angle EPA = \angle DPB

(i) It is given that ∠EPA = ∠DPB

Now, add ∠DPE om both sides,

∠EPA + ∠DPE = ∠DPB + ∠DPE

This implies that angles DPA and EPB are equal i.e. ∠DPA = ∠EPB

Now, consider the triangles DAP and EBP.

∠DPA = ∠EPB

AP = BP (Since P is the mid-point of the line segement AB)

 $\angle BAD = \angle ABE$ (As given in the question)

So, by **ASA congruency**, $\triangle DAP \cong \triangle EBP$.

(ii) By the rule of CPCT, AD = BE.

8. In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that DM = CM. Point D is joined to point B (see Fig. 7.23). Show that:

- (i) ΔAMC ≅ΔBMD
- (ii) ∠DBC is a right angle.

(iii) ΔDBC ≅ΔACB

(iv) CM = 1/2 AB

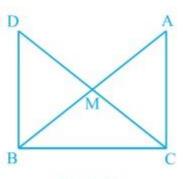


Fig. 7.23

Solution:

It is given that M is the mid-point of the line segment AB, $\angle C = 90^{\circ}$, and DM = CM

(i) Consider the triangles $\triangle AMC$ and $\triangle BMD$:

AM = BM (Since M is the mid-point)

CM = DM (Given in the question)

∠CMA = ∠DMB (They are vertically opposite angles)

So, by **SAS congruency criterion**, $\triangle AMC \cong \triangle BMD$.

(ii) $\angle ACM = \angle BDM$ (by CPCT)

∴ AC | BD as alternate interior angles are equal.

Now, $\angle ACB + \angle DBC = 180^{\circ}$ (Since they are co-interiors angles)

⇒90° + ∠B = 180°

∴ ∠DBC = 90°

(iii) In ΔDBC and ΔACB,

BC = CB (Common side)

 \angle ACB = \angle DBC (They are right angles)

DB = AC (by CPCT)

So, $\triangle DBC \cong \triangle ACB$ by **SAS congruency**.

(iv) DC = AB (Since \triangle DBC \cong \triangle ACB)

 \Rightarrow DM = CM = AM = BM (Since M the is mid-point)

So, DM + CM = BM + AM

Hence, CM + CM = AB

⇒CM = (½) AB



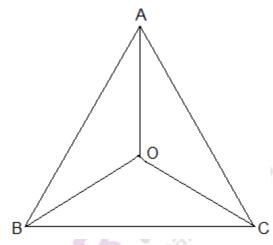
(Page No: 123)

Exercise: 7.2

1. In an isosceles triangle ABC, with AB = AC, the bisectors of \angle B and \angle C intersect each other at O. Join A to O. Show that :

(i) OB = OC

(ii) AO bisects ∠A



Solution:

Given:

-> AB = AC and

-> the bisectors of \(\mathre{L} \mathre{L} \) and \(\alpha \) intersect each other at O

(i) Since ABC is an isosceles with AB = AC,

=> ∠B = ∠C

 $\Rightarrow 1/2 \angle B = 1/2 \angle C$

⇒∠OBC = ∠OCB (Angle bisectors)

 \therefore OB = OC (Side opposite to the equal angles are equal.)

(ii) In ΔAOB and ΔAOC,

AB = AC (Given in the question)

AO = AO (Common arm)

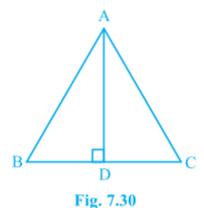
OB = OC (As Proved Already)

So, $\triangle AOB \cong \triangle AOC$ by SSS congruence condition.

 $\angle BAO = \angle CAO$ (by CPCT)

Thus, AO bisects ∠A.

2. In \triangle ABC, AD is the perpendicular bisector of BC (see Fig. 7.30). Show that \triangle ABC is an isosceles triangle in which AB = AC.



Solution:

It is given that AD is the perpendicular bisector of BC

To prove:

AB = AC

Proof:

In ΔADB and ΔADC,

AD = AD (It is the Common arm)

 $\angle ADB = \angle ADC$

BD = CD (Since AD is the perpendicular bisector)

So, \triangle ADB \cong \triangle ADC by **SAS** congruency criterion.

AB = AC (by CPCT)

(Page No: 124)

3. ABC is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see Fig. 7.31). Show that these altitudes are equal.

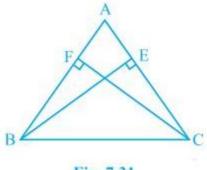


Fig. 7.31

Solution:



Given:

- (i) BE and CF are altitudes.
- (ii) AC = AB

To prove:

BE = CF

Proof:

Triangles ΔAEB and ΔAFC are similar by AAS congruency since

 $\angle A = \angle A$ (It is the common arm)

 \angle AEB = \angle AFC (They are right angles)

AB = AC (Given in the question)

∴ \triangle AEB \cong \triangle AFC and so, BE = CF (by CPCT).

4. ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (see Fig. 7.32). Show that

- (i) $\triangle ABE \cong \triangle ACF$
- (ii) AB = AC, i.e., ABC is an isosceles triangle.

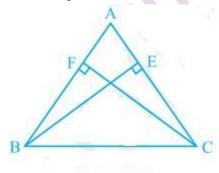


Fig. 7.32

Solution:

It is given that BE = CF

(i) In ΔABE and ΔACF,

 $\angle A = \angle A$ (It is the common angle)

 $\angle AEB = \angle AFC$ (They are right angles)

BE = CF (Given in the question)

∴ \triangle ABE \cong \triangle ACF by **AAS** congruency condition.

(ii) AB = AC by CPCT and so, ABC is an isosceles triangle.



5. ABC and DBC are two isosceles triangles on the same base BC (see Fig. 7.33). Show that $\angle ABD = \angle ACD$.

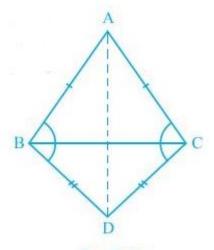


Fig. 7.33

Solution:

In the question, it is given that ABC and DBC are two isosceles triangles.

We will have to show that $\angle ABD = \angle ACD$

Proof:

Triangles ΔABD and ΔACD are similar by SSS congruency since

AD = AD (It is the common arm)

AB = AC (Since ABC is an isosceles triangle)

BD = CD (Since BCD is an isosceles triangle)

So, $\triangle ABD \cong \triangle ACD$.

 \therefore \angle ABD = \angle ACD by CPCT.

6. \triangle ABC is an isosceles triangle in which AB = AC. Side BA is produced to D such that AD = AB (see Fig. 7.34). Show that \angle BCD is a right angle.

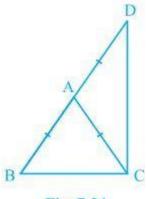


Fig. 7.34

Solution:

It is given that AB = AC and AD = AB

We will have to now prove ∠BCD is a right angle.

Proof:

Consider AABC,

AB = AC (It is given in the question)

Also, $\angle ACB = \angle ABC$ (They are angles opposite to the equal sides and so, they are equal)

Now, consider ΔACD,

AD = AB

Also, $\angle ADC = \angle ACD$ (They are angles opposite to the equal sides and so, they are equal)

Now,

In ΔABC,

 \angle CAB + \angle ACB + \angle ABC = 180°

So, $\angle CAB + 2\angle ACB = 180^{\circ}$

⇒∠CAB = 180° - 2∠ACB --- (i)

Similarly in ΔADC,

∠CAD = 180° - 2∠ACD --- (ii)

also,

 $\angle CAB + \angle CAD = 180^{\circ}$ (BD is a straight line.)

Adding (i) and (ii) we get,

 \angle CAB + \angle CAD = 180° - 2 \angle ACB + 180° - 2 \angle ACD

⇒180° = 360° - 2∠ACB - 2∠ACD

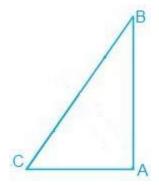
 \Rightarrow 2(\angle ACB + \angle ACD) = 180°

⇒∠BCD = 90°

7. ABC is a right-angled triangle in which $\angle A = 90^{\circ}$ and AB = AC. Find $\angle B$ and $\angle C$.

Solution:





In the question, it si given that

$$\angle A = 90^{\circ}$$
 and $AB = AC$

AB = AC

 $\Rightarrow \angle B = \angle C$ (They are angles opposite to the equal sides and so, they are equal)

Now,

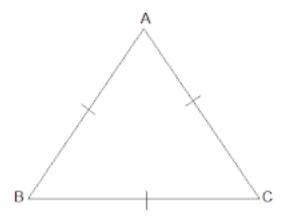
 $\angle A + \angle B + \angle C = 180^{\circ}$ (Since the sum of the interior angles of the triangle)

So,
$$\angle B = \angle C = 45^{\circ}$$

8. Show that the angles of an equilateral triangle are 60° each.

Solution:

Let ABC be an equilateral triangle as shown below:



Here, BC = AC = AB (Since the length of all sides is same)

 $\Rightarrow \angle A = \angle B = \angle C$ (Sides opposite to the equal angles are equal.)

Also, we know that

$$\angle A + \angle B + \angle C = 180^{\circ}$$



⇒3∠A = 180°

⇒∠A = 60°

 $\therefore \angle A = \angle B = \angle C = 60^{\circ}$

So, the angles of an equilateral triangle are always 60° each.

(Page No: 128)

Exercise: 7.3

- 1. \triangle ABC and \triangle DBC are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC (see Fig. 7.39). If AD is extended to intersect BC at P, show that
- (i) ΔABD ≅ΔACD
- (ii) $\triangle ABP \cong \triangle ACP$
- (iii) AP bisects ∠A as well as ∠D.
- (iv) AP is the perpendicular bisector of BC.

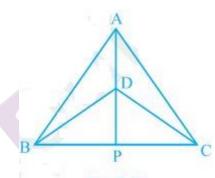


Fig. 7.39

Solution:

In the above question, it is given that \triangle ABC and \triangle DBC are two isosceles triangles.

(i) \triangle ABD and \triangle ACD are similar by SSS congruency because:

AD = AD (It is the common arm)

AB = AC (Since $\triangle ABC$ is isosceles)

BD = CD (Since \triangle DBC is isosceles)

∴ \triangle ABD \cong \triangle ACD.

(ii) ΔABP and ΔACP are similar as:

AP = AP (It is the common side)

 $\angle PAB = \angle PAC$ (by CPCT since $\triangle ABD \cong \triangle ACD$)



AB = AC (Since $\triangle ABC$ is isosceles)

So, $\triangle ABP \cong \triangle ACP$ by SAS congruency condition.

(iii) $\angle PAB = \angle PAC$ by CPCT as $\triangle ABD \cong \triangle ACD$.

AP bisects ∠A. --- (i)

Also, \triangle BPD and \triangle CPD are similar by SSS congruency as

PD = PD (It is the common side)

BD = CD (Since \triangle DBC is isosceles.)

BP = CP (by CPCT as \triangle ABP \cong \triangle ACP)

So, $\triangle BPD \cong \triangle CPD$.

Thus, $\angle BDP = \angle CDP$ by CPCT. --- (ii)

Now by comparing (i) and (ii) it can be said that AP bisects $\angle A$ as well as $\angle D$.

(iv) $\angle BPD = \angle CPD$ (by CPCT as $\triangle BPD \cong \triangle CPD$)

and BP = CP --- (i)

also,

∠BPD + ∠CPD = 180° (Since BC is a straight line.)

⇒2∠BPD = 180°

⇒∠BPD = 90° ---(ii)

Now, from equations (i) and (ii), it can be said that

AP is the perpendicular bisector of BC.

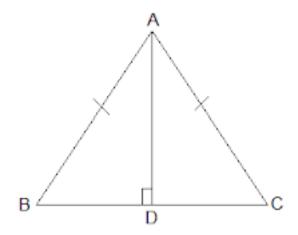
2. AD is an altitude of an isosceles triangle ABC in which AB = AC. Show that

(i) AD bisects BC

(ii) AD bisects ∠A.

Solution:

It is given that AD is an altitude and AB = AC. The diagram is as follows:



(i) In ΔABD and ΔACD,

 $\angle ADB = \angle ADC = 90^{\circ}$

AB = AC (It is given in the question)

AD = AD (Common arm)

∴ \triangle ABD \cong \triangle ACD by RHS congruence condition.

Now, by the rule of CPCT,

BD = CD.

So, AD bisects BC

(ii) Again by the rule of CPCT, \angle BAD = \angle CAD

Hence, AD bisects ∠A.

- 3. Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of Δ PQR (see Fig. 7.40). Show that:
- (i) $\triangle ABM \cong \triangle PQN$
- (ii) $\triangle ABC \cong \triangle PQR$

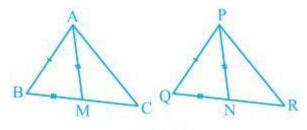


Fig. 7.40

Solution:

Given parameters are:

AB = PQ,

BC = QR and



AM = PN

(i) 1/2 BC = BM and 1/2QR = QN (Since AM and PN are medians)

Also, BC = QR

So, 1/2 BC = 1/2QR

⇒BM = QN

In \triangle ABM and \triangle PQN,

AM = PN and AB = PQ (As given in the question)

BM = QN (Already proved)

∴ \triangle ABM \cong \triangle PQN by SSS congruency.

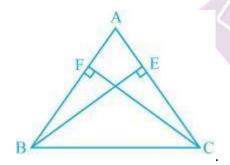
(ii) In ΔABC and ΔPQR,

AB = PQ and BC = QR (As given in the question)

 $\angle ABC = \angle PQR$ (by CPCT)

So, $\triangle ABC \cong \triangle PQR$ by SAS congruency.

4. BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.



Solution:

It is known that BE and CF are two equal altitudes.

Now, in \triangle BEC and \triangle CFB,

 \angle BEC = \angle CFB = 90° (Same Altitudes)

BC = CB (Common side)

BE = CF (Common side)

So, $\triangle BEC \cong \triangle CFB$ by RHS congruence criterion.

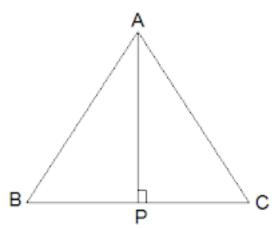
Also, $\angle C = \angle B$ (by CPCT)

Therefore, AB = AC as sides opposite to the equal angles is always equal.



5. ABC is an isosceles triangle with AB = AC. Draw AP \perp BC to show that \angle B = \angle C.

Solution:



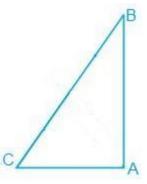
In the question, it is given that AB = ACNow, $\triangle ABP$ and $\triangle ACP$ are similar by RHS congruency as $\angle APB = \angle APC = 90^\circ$ (AP is altitude) AB = AC (Given in the question) AP = AP (Common side) So, $\triangle ABP \cong \triangle ACP$.

∴ ∠B = ∠C (by CPCT)

(Page No: 132)

Exercise: 7.4

1. Show that in a right angled triangle, the hypotenuse is the longest side.



Solution:

It is known that ABC is a triangle right angled at B.

We know that,

 $\angle A + \angle B + \angle C = 180^{\circ}$

Now, if $\angle B + \angle C = 90^{\circ}$ then $\angle A$ has to be 90°.

Since A is the largest angle of the triangle, the side opposite to it must be the largest.

So, AB is the hypotenuse which will be the largest side of the above right-angled triangle i.e. ΔABC .

2. In Fig. 7.48, sides AB and AC of \triangle ABC are extended to points P and Q respectively. Also, \angle PBC < \angle QCB. Show that AC > AB.

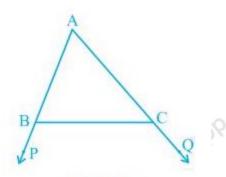


Fig. 7.48

Solution:

It is given that ∠PBC < ∠QCB

We know that $\angle ABC + \angle PBC = 180^{\circ}$

So, ∠ABC = 180° - ∠PBC

Also,

 $\angle ACB + \angle QCB = 180^{\circ}$

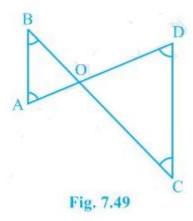
Therefore ∠ACB = 180° - ∠QCB

Now, since ∠PBC < ∠QCB,

∴ ∠ABC > ∠ACB

Hence, AC > AB as sides opposite to the larger angle is always larger.

3. In Fig. 7.49, $\angle B < \angle A$ and $\angle C < \angle D$. Show that AD < BC.



Solution:

In the question, it is mentioned that angles B and angle C is smaller than angles A and D respectively i.e. \angle B < \angle A and \angle C < \angle D

Now,

Since the side opposite to the smaller angle is always smaller

AO < BO --- (i)

And OD < OC ---(ii)

By adding equation (i) and equation (ii) we get

AO + OD < BO + OC

So, AD < BC

4. AB and CD are respectively the smallest and longest sides of a quadrilateral ABCD (see Fig. 7.50).

Show that $\angle A > \angle C$ and $\angle B > \angle D$.

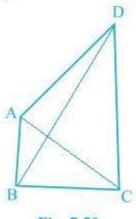


Fig. 7.50



Solution:

In ΔABD,

AB < AD < BD

So, ∠ADB < ∠ABD --- (i) (Since angle opposite to longer side is always larger)

Now, in $\triangle BCD$,

BC < DC < BD

Hence, it can be concluded that

∠BDC < ∠CBD --- (ii)

Now, by adding equation (i) and equation (ii) we get,

∠ADB + ∠BDC < ∠ABD + ∠CBD

=> \(\alpha DC < \(\alpha BC \)

=> ∠B > ∠D

Similarly, In triangle ABC,

∠ACB < ∠BAC --- (iii) (Since the angle opposite to the longer side is always larger)

Now, In ΔADC,

 $\angle DCA < \angle DAC --- (iv)$

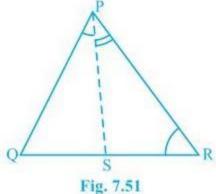
By adding equation (iii) and equation (iv) we get,

∠ACB + ∠DCA < ∠BAC + ∠DAC

⇒∠BCD < ∠BAD

 $\therefore \angle A > \angle C$

5. In Fig 7.51, PR > PQ and PS bisect ∠QPR. Prove that ∠PSR > ∠PSQ.



Solution:

It is given that PR > PQ and PS bisects ∠QPR

Now we will have to prove that angle PSR is smaller than PSQ i.e. ∠PSR > ∠PSQ

Proof:

 $\angle QPS = \angle RPS ---$ (ii) (As PS bisects $\angle QPR$)

∠PQR > ∠PRQ --- (i) (Since PR > PQ as angle opposite to the larger side is always larger)



 \angle PSR = \angle PQR + \angle QPS --- (iii) (Since the exterior angle of a triangle equals to the sum of opposite interior angles)

 \angle PSQ = \angle PRQ + \angle RPS --- (iv) (As the exterior angle of a triangle equals to the sum of opposite interior angles)

By adding (i) and (ii)

∠PQR + ∠QPS > ∠PRQ + ∠RPS

Now, from (i), (ii), (iii) and (iv), we get

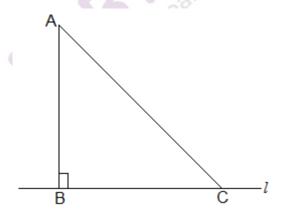
∠PSR > ∠PSQ

(Page No: 133)

6. Show that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.

Solution:

First, let "I" be a line segment and "B" be a point lying on it. A line AB perpendicular to I is now drawn. Also, let C be any other point on I. The diagram will be as follows:



To prove:

AB < AC

Proof:

In $\triangle ABC$, $\angle B = 90^{\circ}$

Now, we know that

$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\therefore \angle A + \angle C = 90^{\circ}$$

Hence, $\angle C$ must be an acute angle which implies $\angle C < \angle B$

So, AB < AC (As the side opposite to the larger angle is always larger)



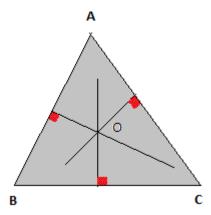
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Exercise 7.5 (Optional)

1. ABC is a triangle. Locate a point in the interior of \triangle ABC which is equidistant from all the vertices of \triangle ABC.

Solution:

Consider a triangle ABC. A point in the interior of \triangle ABC which is equidistant from all the vertices of \triangle ABC is the "circumcenter".

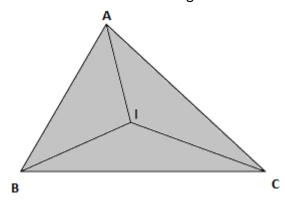


Now, the circumcenter is the point where the three perpendicular bisectors to the three sides of the triangle intersect each other. So, draw the three perpendicular bisector to AB, BC and CA and mark their intersecting points as O which is the required point.

2. In a triangle, locate a point in its interior which is equidistant from all the sides of the triangle.

Solution:

Again consider a triangle ABC. Now, a point in the interior of the triangle which is equidistant from all the sides of the triangle will be its "incenter".



(Here, $\angle BAI = \angle CAI$, $\angle ABI = \angle CBI$ and $\angle BCI = \angle ACI$)



The incenter of a triangle is the intersection point where all the interior angle bisectors of the triangle meets. So, to locate incenter, draw three interior angle bisectors and mark the intersection point as O which is the required point.

3. In a huge park, people are concentrated at three points (see Fig. 7.52).

A: where there are different slides and swings for children,

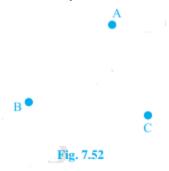
B: near which a man-made lake is situated,

C: which is near to a large parking and exit.

Where should an icecream parlour be set up so that maximum number of persons can approach

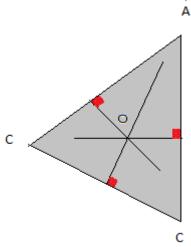
it?

(Hint: The parlour should be equidistant from A, B and C)



Solution:

The parlor should be at a point where it is equidistant from ABC. If points ABC are considered as a triangle, the parlor will have to be at the circumcenter as it is equidistant from the three vertices of the triangle. Thus, join ABC and construct three perpendicular bisectors to AB, BC and CA. Mark the intersection point as O which will be the circumcenter.



4. Complete the hexagonal and star shaped Rangolies [see Fig. (i) and (ii)] by filling them with as many equilateral triangles of side 1 cm as you can. Count the number of triangles in each case. Which has more triangles?



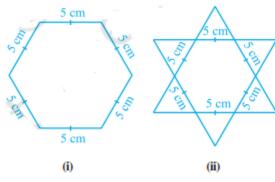


Fig. 7.53

Solution:

First calculate the area of hexagon i.e. fig (i).

$$Hexagon\ Area = 6 \times \frac{25\sqrt{3}}{4}$$

Now, the area of equilateral triangles with side 1 cm = $(\sqrt{3}/4) \times a^2 = (\sqrt{3}/4)$ cm²

So, No. of equilateral triangles in fig (i) will be = (hexagon area/area of equilateral triangle) = 150

Now, in fig (ii), the star shaped rangoli will have an area as:

Area of star shape rangoli =
$$12 \times \frac{\sqrt{3}}{4} \times 5^2$$

Now, the area of equilateral triangles with side 1 cm = (area of star shaped rangoli/area of equilateral triangle) = 300

Thus, fig (ii) has more triangles.