

Exercise 4.1

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1. Check whether the following are quadratic equations:

(i) $(x + 1)^2 = 2(x - 3)$

(ii) $x^2 - 2x = (-2)(3 - x)$

(iii) $(x - 2)(x + 1) = (x - 1)(x + 3)$

(iv) $(x - 3)(2x + 1) = x(x + 5)$

(v) $(2x - 1)(x - 3) = (x + 5)(x - 1)$

(vi) $x^2 + 3x + 1 = (x - 2)^2$

(vii) $(x + 2)^3 = 2x(x^2 - 1)$

(viii) $x^3 - 4x^2 - x + 1 = (x - 2)^3$

Solutions:

(i) Given,

$$(x + 1)^2 = 2(x - 3)$$

By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$

$$\Rightarrow x^2 + 2x + 1 = 2x - 6$$

$$\Rightarrow x^2 + 7 = 0$$

Since the above equation is in the form of $ax^2 + bx + c = 0$.

Therefore, the given equation is quadratic equation.

(ii) Given, $x^2 - 2x = (-2)(3 - x)$

By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$

$$\Rightarrow x^2 - 2x = -6 + 2x$$

$$\Rightarrow x^2 - 4x + 6 = 0$$

Since the above equation is in the form of $ax^2 + bx + c = 0$.

Therefore, the given equation is quadratic equation.

(iii) Given, $(x - 2)(x + 1) = (x - 1)(x + 3)$

By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$

$$\Rightarrow x^2 - x - 2 = x^2 + 2x - 3$$

$$\Rightarrow 3x - 1 = 0$$

Since the above equation is not in the form of $ax^2 + bx + c = 0$.

Therefore, the given equation is not a quadratic equation.

(iv) Given, $(x - 3)(2x + 1) = x(x + 5)$

By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$

$$\Rightarrow 2x^2 - 5x - 3 = x^2 + 5x$$

$$\Rightarrow x^2 - 10x - 3 = 0$$

Since the above equation is in the form of $ax^2 + bx + c = 0$.

Therefore, the given equation is quadratic equation.

(v) Given, $(2x - 1)(x - 3) = (x + 5)(x - 1)$

By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$

$$\Rightarrow 2x^2 - 7x + 3 = x^2 + 4x - 5$$

$$\Rightarrow x^2 - 11x + 8 = 0$$

Since the above equation is in the form of $ax^2 + bx + c = 0$.

Therefore, the given equation is quadratic equation.

(vi) Given, $x^2 + 3x + 1 = (x - 2)^2$
By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$
 $\Rightarrow x^2 + 3x + 1 = x^2 + 4 - 4x$
 $\Rightarrow 7x - 3 = 0$

Since the above equation is not in the form of $ax^2 + bx + c = 0$.
Therefore, the given equation is not a quadratic equation.

(vii) Given, $(x + 2)^3 = 2x(x^2 - 1)$
By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$
 $\Rightarrow x^3 + 8 + x^2 + 12x = 2x^3 - 2x$
 $\Rightarrow x^3 + 14x - 6x^2 - 8 = 0$

Since the above equation is not in the form of $ax^2 + bx + c = 0$.
Therefore, the given equation is not a quadratic equation.

(viii) Given, $x^3 - 4x^2 - x + 1 = (x - 2)^3$
By using the formula for $(a+b)^2 = a^2 + 2ab + b^2$
 $\Rightarrow x^3 - 4x^2 - x + 1 = x^3 - 8 - 6x^2 + 12x$
 $\Rightarrow 2x^2 - 13x + 9 = 0$

Since the above equation is in the form of $ax^2 + bx + c = 0$.
Therefore, the given equation is quadratic equation.

2. Represent the following situations in the form of quadratic equations:

- (i) The area of a rectangular plot is 528 m^2 . The length of the plot (in metres) is one more than twice its breadth. We need to find the length and breadth of the plot.
- (ii) The product of two consecutive positive integers is 306. We need to find the integers.
- (iii) Rohan's mother is 26 years older than him. The product of their ages (in years) 3 years from now will be 360. We would like to find Rohan's present age.
- (iv) A train travels a distance of 480 km at a uniform speed. If the speed had been 8 km/h less, then it would have taken

Solutions:

- (i) Let us consider,
Breadth of the rectangular plot = $x \text{ m}$

Thus, the length of the plot = $(2x + 1) \text{ m}$.

As we know,

Area of rectangle = length \times breadth = 528 m²

Putting the value of length and breadth of the plot in the formula, we get,

$$(2x + 1) \times x = 528$$

$$\Rightarrow 2x^2 + x = 528$$

$$\Rightarrow 2x^2 + x - 528 = 0$$

Therefore, the length and breadth of plot, satisfies the quadratic equation, $2x^2 + x - 528 = 0$, which is the required representation of the problem mathematically.

(ii) Let us consider,

The first integer number = x

Thus, the next consecutive positive integer will be = $x + 1$

Product of two consecutive integers = $x \times (x + 1) = 306$

$$\Rightarrow x^2 + x = 306$$

$$\Rightarrow x^2 + x - 306 = 0$$

Therefore, the two integers x and $x + 1$, satisfies the quadratic equation, $x^2 + x - 306 = 0$, which is the required representation of the problem mathematically.

(iii) Let us consider,

Age of Rohan's = x years

Therefore, as per the given question,

Rohan's mother's age = $x + 26$

After 3 years,

Age of Rohan's = $x + 3$

Age of Rohan's mother will be = $x + 26 + 3 = x + 29$

The product of their ages after 3 years will be equal to 360, such that

$$(x + 3)(x + 29) = 360$$

$$\Rightarrow x^2 + 29x + 3x + 87 = 360$$

$$\Rightarrow x^2 + 32x + 87 - 360 = 0$$

$$\Rightarrow x^2 + 32x - 273 = 0$$

Therefore, the age of Rohan and his mother, satisfies the quadratic equation, $x^2 + 32x - 273 = 0$, which is the required representation of the problem mathematically.

- (iv) Let us consider,
The speed of train = x km/h
And

$$\text{Time taken to travel 480 km} = \frac{480}{x} \text{ km/h}$$

As per second condition, the speed of train = $(x - 8)$ km/h

Also given, the train will take 3 hours to cover the same distance.

$$\text{Therefore, time taken to travel 480 km} = \frac{480}{x + 3} \text{ km/h}$$

As we know,
Speed \times Time = Distance
Therefore,

$$(x - 8)(480/x + 3) = 480$$

$$\Rightarrow 480 + 3x - 3840/x - 24 = 480$$

$$\Rightarrow 3x - 3840/x = 24$$

$$\Rightarrow 3x^2 - 8x - 1280 = 0$$

Therefore, the speed of the train, satisfies the quadratic equation, $3x^2 - 8x - 1280 = 0$, which is the required representation of the problem mathematically.