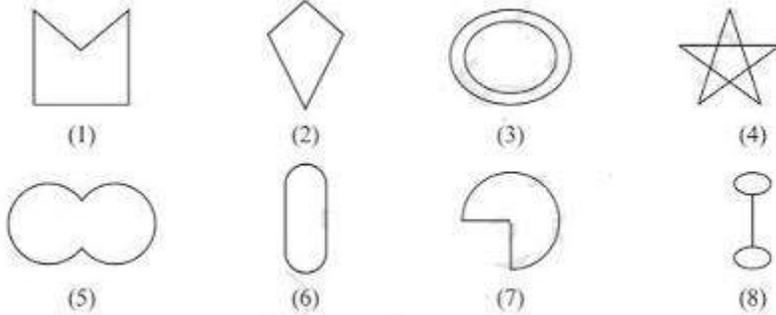


Exercise 3.1

1. Given here are some figures.



Classify each of them on the basis of the following.

- (a) Simple curve    (b) Simple closed curve    (c) Polygon  
(d) Convex polygon    (e) Concave polygon

Solution:

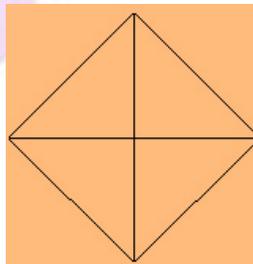
- a) Simple curve: 1, 2, 5, 6 and 7
- b) Simple closed curve: 1, 2, 5, 6 and 7
- c) Polygon: 1 and 2
- d) Convex polygon: 2
- e) Concave polygon: 1

2. How many diagonals does each of the following have?

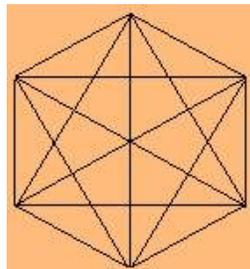
- (a) A convex quadrilateral    (b) A regular hexagon    (c) A triangle

Solution:

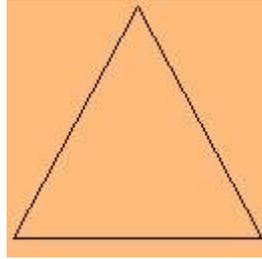
- a) A convex quadrilateral: 2.



- b) A regular hexagon: 9.

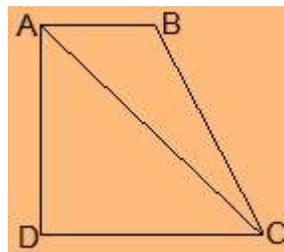


- c) A triangle: 0.



3. What is the sum of the measures of the angles of a convex quadrilateral? Will this property hold if the quadrilateral is not convex? (Make a non-convex quadrilateral and try!)

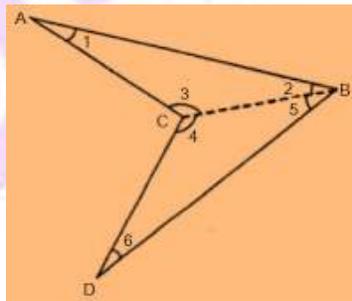
Solution:



Let ABCD be a convex quadrilateral.

From the figure, we infer that the quadrilateral ABCD is formed by two triangles, i.e.  $\triangle ADC$  and  $\triangle ABC$ .

Since, we know that sum of interior angles of triangle is  $180^\circ$ ,  
the sum of the measures of the angles is  $180^\circ + 180^\circ = 360^\circ$



Let us take another quadrilateral ABCD which is not convex .

Join BC, Such that it divides ABCD into two triangles  $\triangle ABC$  and  $\triangle BCD$ .

In  $\triangle ABC$ ,

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ \text{ (angle sum property of triangle)}$$

In  $\triangle BCD$ ,

$$\angle 4 + \angle 5 + \angle 6 = 180^\circ \text{ (angle sum property of triangle)}$$

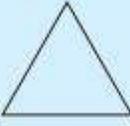
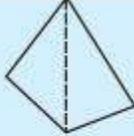
$$\therefore, \angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 + \angle 6 = 180^\circ + 180^\circ$$

$$\Rightarrow \angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 + \angle 6 = 360^\circ$$

$$\Rightarrow \angle A + \angle B + \angle C + \angle D = 360^\circ$$

Thus, this property hold if the quadrilateral is not convex.

4. Examine the table. (Each figure is divided into triangles and the sum of the angles deduced from that.)

Figure				
Side	3	4	5	6
Angle sum	$180^\circ$	$2 \times 180^\circ$ $= (4 - 2) \times 180^\circ$	$3 \times 180^\circ$ $= (5 - 2) \times 180^\circ$	$4 \times 180^\circ$ $= (6 - 2) \times 180^\circ$

What can you say about the angle sum of a convex polygon with number of sides?

- (a) 7      (b) 8      (c) 10      (d) n

Solution:

The angle sum of a polygon having side  $n = (n-2) \times 180^\circ$

- a) 7  
Here,  $n = 7$   
Thus, angle sum =  $(7-2) \times 180^\circ = 5 \times 180^\circ = 900^\circ$
- b) 8  
Here,  $n = 8$   
Thus, angle sum =  $(8-2) \times 180^\circ = 6 \times 180^\circ = 1080^\circ$
- c) 10  
Here,  $n = 10$   
Thus, angle sum =  $(10-2) \times 180^\circ = 8 \times 180^\circ = 1440^\circ$
- d) n  
Here,  $n = n$   
Thus, angle sum =  $(n-2) \times 180^\circ$

5. What is a regular polygon?

State the name of a regular polygon of

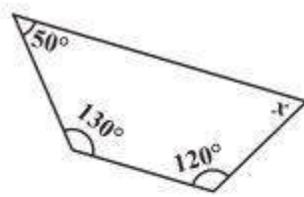
- (i) 3 sides      (ii) 4 sides      (iii) 6 sides

Solution:

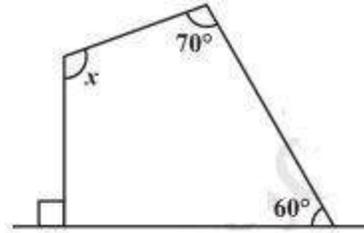
Regular polygon: A polygon having sides of equal length and angles of equal measures is called regular polygon. i.e., A regular polygon is both equilateral and equiangular.

- (i) A regular polygon of 3 sides is called equilateral triangle.  
(ii) A regular polygon of 4 sides is called square.  
(iii) A regular polygon of 6 sides is called regular hexagon.

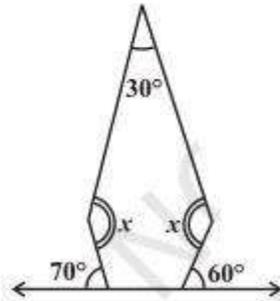
6. Find the angle measure x in the following figures.



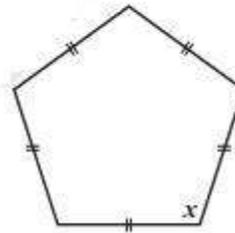
(a)



(b)



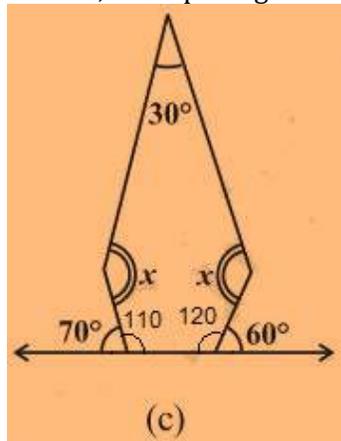
(c)



(d)

**Solution:**

- a) The figure is having 4 sides. Hence, it is a quadrilateral.  
Sum of angles of the quadrilateral =  $360^\circ$   
 $\Rightarrow 50^\circ + 130^\circ + 120^\circ + x = 360^\circ$   
 $\Rightarrow 300^\circ + x = 360^\circ$   
 $\Rightarrow x = 360^\circ - 300^\circ = 60^\circ$
- b) The figure is having 4 sides. Hence, it is a quadrilateral. Also, one side is perpendicular forming right angle.  
Sum of angles of the quadrilateral =  $360^\circ$   
 $\Rightarrow 90^\circ + 70^\circ + 60^\circ + x = 360^\circ$   
 $\Rightarrow 220^\circ + x = 360^\circ$   
 $\Rightarrow x = 360^\circ - 220^\circ = 140^\circ$
- c) The figure is having 5 sides. Hence, it is a pentagon.



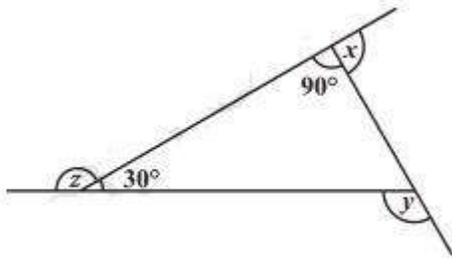
(c)

Sum of angles of the pentagon =  $540^\circ$   
 Two angles at the bottom are linear pair.  
 $\therefore, 180^\circ - 70^\circ = 110^\circ$   
 $180^\circ - 60^\circ = 120^\circ$   
 $\Rightarrow 30^\circ + 110^\circ + 120^\circ + x + x = 540^\circ$   
 $\Rightarrow 260^\circ + 2x = 540^\circ$   
 $\Rightarrow 2x = 540^\circ - 260^\circ = 280^\circ$   
 $\Rightarrow x = \frac{280}{2}$   
 $= 140^\circ$

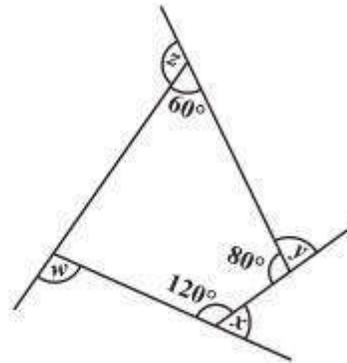
d) The figure is having 5 equal sides. Hence, it is a regular pentagon. Thus, its all angles are equal.

$5x = 540^\circ$   
 $\Rightarrow x = \frac{540}{5}$   
 $\Rightarrow x = 108^\circ$

7.



(a) Find  $x + y + z$



(b) Find  $x + y + z + w$

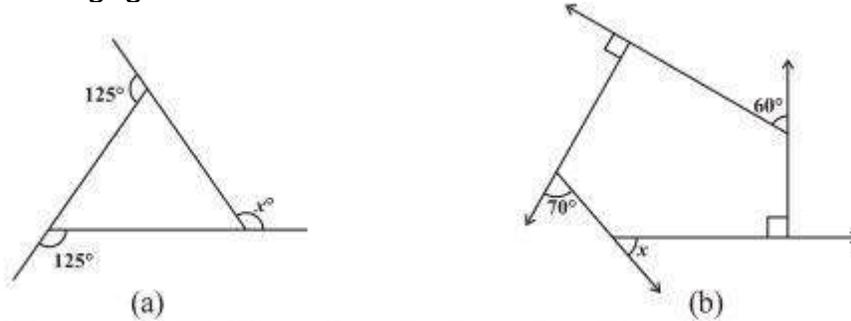
Solution:

a) Sum of all angles of triangle =  $180^\circ$   
 One side of triangle =  $180^\circ - (90^\circ + 30^\circ) = 60^\circ$   
 $x + 90^\circ = 180^\circ \Rightarrow x = 180^\circ - 90^\circ = 90^\circ$   
 $y + 60^\circ = 180^\circ \Rightarrow y = 180^\circ - 60^\circ = 120^\circ$   
 $z + 30^\circ = 180^\circ \Rightarrow z = 180^\circ - 30^\circ = 150^\circ$   
 $x + y + z = 90^\circ + 120^\circ + 150^\circ = 360^\circ$

b) Sum of all angles of quadrilateral =  $360^\circ$   
 One side of quadrilateral =  $360^\circ - (60^\circ + 80^\circ + 120^\circ) = 360^\circ - 260^\circ = 100^\circ$   
 $x + 120^\circ = 180^\circ \Rightarrow x = 180^\circ - 120^\circ = 60^\circ$   
 $y + 80^\circ = 180^\circ \Rightarrow y = 180^\circ - 80^\circ = 100^\circ$   
 $z + 60^\circ = 180^\circ \Rightarrow z = 180^\circ - 60^\circ = 120^\circ$   
 $w + 100^\circ = 180^\circ \Rightarrow w = 180^\circ - 100^\circ = 80^\circ$   
 $x + y + z + w = 60^\circ + 100^\circ + 120^\circ + 80^\circ = 360^\circ$

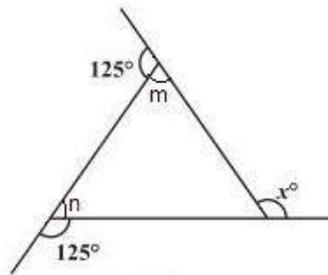
Exercise 3.2

1. Find  $x$  in the following figures.



Solution:

a)



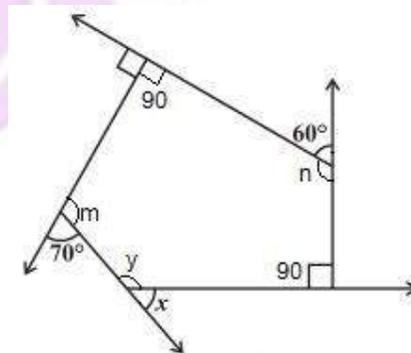
$$125^\circ + m = 180^\circ \Rightarrow m = 180^\circ - 125^\circ = 55^\circ \text{ (Linear pair)}$$

$$125^\circ + n = 180^\circ \Rightarrow n = 180^\circ - 125^\circ = 55^\circ \text{ (Linear pair)}$$

$x = m + n$  (exterior angle of a triangle is equal to the sum of 2 opposite interior angles)

$$\Rightarrow x = 55^\circ + 55^\circ = 110^\circ$$

b)



Two interior angles are right angles =  $90^\circ$

$$70^\circ + m = 180^\circ \Rightarrow m = 180^\circ - 70^\circ = 110^\circ \text{ (Linear pair)}$$

$$60^\circ + n = 180^\circ \Rightarrow n = 180^\circ - 60^\circ = 120^\circ \text{ (Linear pair)}$$

The figure is having five sides and is a pentagon.

Thus, sum of the angles of pentagon =  $540^\circ$

$$90^\circ + 90^\circ + 110^\circ + 120^\circ + y = 540^\circ$$

$$\Rightarrow 410^\circ + y = 540^\circ \Rightarrow y = 540^\circ - 410^\circ = 130^\circ$$

$$x + y = 180^\circ \text{ (Linear pair)}$$

$$\Rightarrow x + 130^\circ = 180^\circ$$

$$\Rightarrow x = 180^\circ - 130^\circ = 50^\circ$$

2. Find the measure of each exterior angle of a regular polygon of  
 (i) 9 sides      (ii) 15 sides

Solution:

Sum of angles a regular polygon having side n =  $(n-2) \times 180^\circ$

(i) Sum of angles a regular polygon having side 9 =  $(9-2) \times 180^\circ$   
 $= 7 \times 180^\circ = 1260^\circ$

Each interior angle =  $\frac{1260}{9} = 140^\circ$

Each exterior angle =  $180^\circ - 140^\circ = 40^\circ$

Or,

Each exterior angle =  $\frac{\text{Sum of exterior angles}}{\text{Number of sides}} = \frac{360}{9} = 40^\circ$

(ii) Sum of angles a regular polygon having side 15 =  $(15-2) \times 180^\circ$   
 $= 13 \times 180^\circ = 2340^\circ$

Each interior angle =  $\frac{2340}{15} = 156^\circ$

Each exterior angle =  $180^\circ - 156^\circ = 24^\circ$

Or,

Each exterior angle =  $\frac{\text{Sum of exterior angles}}{\text{Number of sides}} = \frac{360}{15} = 24^\circ$

3. How many sides does a regular polygon have if the measure of an exterior angle is  $24^\circ$ ?

Solution:

Each exterior angle =  $\frac{\text{Sum of exterior angles}}{\text{Number of sides}}$

$24^\circ = \frac{360}{\text{Number of sides}}$

$\Rightarrow \text{Number of sides} = \frac{360}{24} = 15$

Thus, the regular polygon have 15 sides.

4. How many sides does a regular polygon have if each of its interior angles is  $165^\circ$ ?

Solution:

Interior angle =  $165^\circ$

Exterior angle =  $180^\circ - 165^\circ = 15^\circ$

Number of sides =  $\frac{\text{Sum of exterior angles}}{\text{exterior angles}}$

$\Rightarrow \text{Number of sides} = \frac{360}{15} = 24$

Thus, the regular polygon have 24 sides.

5.

- a) Is it possible to have a regular polygon with measure of each exterior angle as  $22^\circ$ ?  
b) Can it be an interior angle of a regular polygon? Why?

Solution:

a) Exterior angle =  $22^\circ$

$$\text{Number of sides} = \frac{\text{Sum of exterior angles}}{\text{exterior angles}}$$

$$\Rightarrow \text{Number of sides} = \frac{360}{22} = 16.36$$

No, we can't have a regular polygon with each exterior angle as  $22^\circ$  as it is not divisor of 360.

b) Interior angle =  $22^\circ$

$$\text{Exterior angle} = 180^\circ - 22^\circ = 158^\circ$$

No, we can't have a regular polygon with each exterior angle as  $158^\circ$  as it is not divisor of 360.

6.

- a) What is the minimum interior angle possible for a regular polygon? Why?  
b) What is the maximum exterior angle possible for a regular polygon?

Solution:

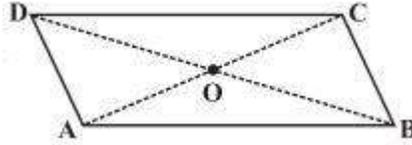
- a) Equilateral triangle is regular polygon with 3 sides has the least possible minimum interior angle because the regular with minimum sides can be constructed with 3 sides at least.  
Since, sum of interior angles of a triangle =  $180^\circ$

$$\text{Each interior angle} = \frac{180}{3} = 60^\circ$$

- b) Equilateral triangle is regular polygon with 3 sides has the maximum exterior angle because the regular polygon with least number of sides have the maximum exterior angle possible.  
Maximum exterior possible =  $180 - 60^\circ = 120^\circ$

Exercise 3.3

1. Given a parallelogram ABCD. Complete each statement along with the definition or property used.

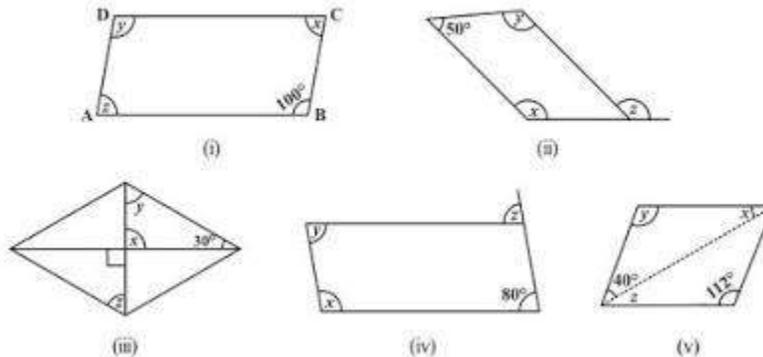


- (i)  $AD = \dots\dots$       (ii)  $\angle DCB = \dots\dots$   
 (iii)  $OC = \dots\dots$       (iv)  $m\angle DAB + m\angle CDA = \dots\dots$

Solution:

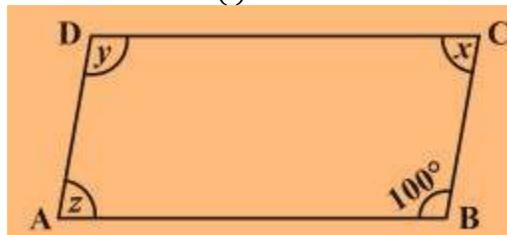
- (i)  $AD = BC$  (Opposite sides of a parallelogram are equal)  
 (ii)  $\angle DCB = \angle DAB$  (Opposite angles of a parallelogram are equal)  
 (iii)  $OC = OA$  (Diagonals of a parallelogram are equal)  
 (iv)  $m\angle DAB + m\angle CDA = 180^\circ$

2. Consider the following parallelograms. Find the values of the unknowns x, y, z.



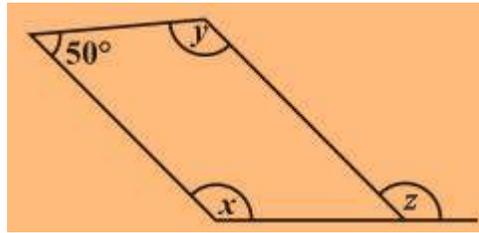
Solution:

(i)



- $y = 100^\circ$  (opposite angles of a parallelogram)  
 $x + 100^\circ = 180^\circ$  (Adjacent angles of a parallelogram)  
 $\Rightarrow x = 180^\circ - 100^\circ = 80^\circ$   
 $x = z = 80^\circ$  (opposite angles of a parallelogram)  
 $\therefore, x = 80^\circ, y = 100^\circ$  and  $z = 80^\circ$

(ii)

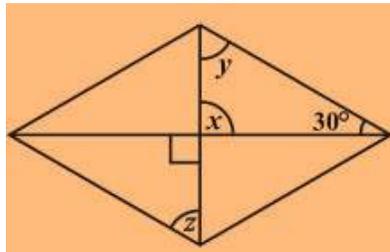


$$50^\circ + x = 180^\circ \Rightarrow x = 180^\circ - 50^\circ = 130^\circ \text{ (Adjacent angles of a parallelogram)}$$

$$x = y = 130^\circ \text{ (opposite angles of a parallelogram)}$$

$$x = z = 130^\circ \text{ (corresponding angle)}$$

(iii)



$$x = 90^\circ \text{ (vertical opposite angles)}$$

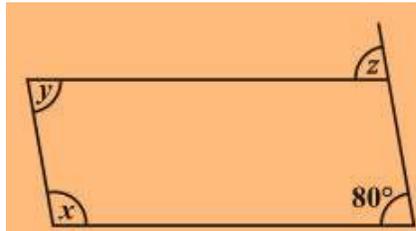
$$x + y + 30^\circ = 180^\circ \text{ (angle sum property of a triangle)}$$

$$\Rightarrow 90^\circ + y + 30^\circ = 180^\circ$$

$$\Rightarrow y = 180^\circ - 120^\circ = 60^\circ$$

$$\text{also, } y = z = 60^\circ \text{ (alternate angles)}$$

(iv)



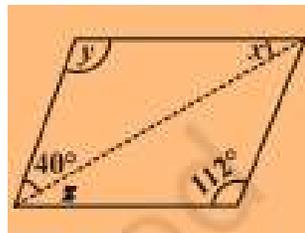
$$z = 80^\circ \text{ (corresponding angle)}$$

$$z = y = 80^\circ \text{ (alternate angles)}$$

$$x + y = 180^\circ \text{ (adjacent angles)}$$

$$\Rightarrow x + 80^\circ = 180^\circ \Rightarrow x = 180^\circ - 80^\circ = 100^\circ$$

(v)



$$x = 28^\circ$$

$$y = 112^\circ$$

$$z = 28^\circ$$

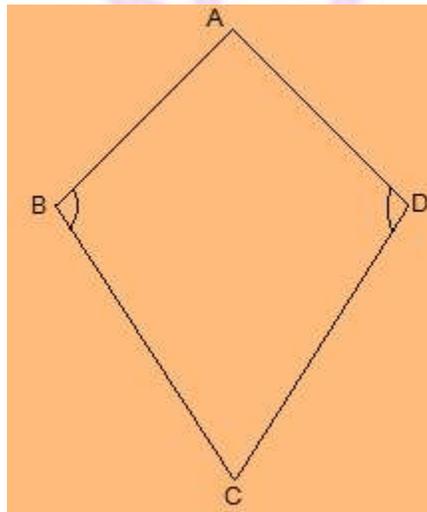
3. Can a quadrilateral ABCD be a parallelogram if
- $\angle D + \angle B = 180^\circ$ ?
  - $AB = DC = 8 \text{ cm}$ ,  $AD = 4 \text{ cm}$  and  $BC = 4.4 \text{ cm}$ ?
  - $\angle A = 70^\circ$  and  $\angle C = 65^\circ$ ?

Solution:

- (i) Yes, a quadrilateral ABCD be a parallelogram if  $\angle D + \angle B = 180^\circ$  but it should also fulfilled some conditions which are:
- The sum of the adjacent angles should be  $180^\circ$ .
  - Opposite angles must be equal.
- (ii) No, opposite sides should be of same length. Here,  $AD \neq BC$
- (iii) No, opposite angles should be of same measures.  $\angle A \neq \angle C$

4. Draw a rough figure of a quadrilateral that is not a parallelogram but has exactly two opposite angles of equal measure.

Solution:



ABCD is a figure of quadrilateral that is not a parallelogram but has exactly two opposite angles that is  $\angle B = \angle D$  of equal measure. It is not a parallelogram because  $\angle A \neq \angle C$ .

5. The measures of two adjacent angles of a parallelogram are in the ratio 3 : 2. Find the measure of each of the angles of the parallelogram.

Solution:

Let the measures of two adjacent angles  $\angle A$  and  $\angle B$  be  $3x$  and  $2x$  respectively in parallelogram ABCD.

$$\angle A + \angle B = 180^\circ$$

$$\Rightarrow 3x + 2x = 180^\circ$$

$$\Rightarrow 5x = 180^\circ$$

$$\Rightarrow x = 36^\circ$$

We know that opposite sides of a parallelogram are equal.

$$\angle A = \angle C = 3x = 3 \times 36^\circ = 108^\circ$$

$$\angle B = \angle D = 2x = 2 \times 36^\circ = 72^\circ$$

6. Two adjacent angles of a parallelogram have equal measure. Find the measure of each of the angles of the parallelogram.

**Solution:**

Let ABCD be a parallelogram.

Sum of adjacent angles of a parallelogram =  $180^\circ$

$$\angle A + \angle B = 180^\circ$$

$$\Rightarrow 2\angle A = 180^\circ$$

$$\Rightarrow \angle A = 90^\circ$$

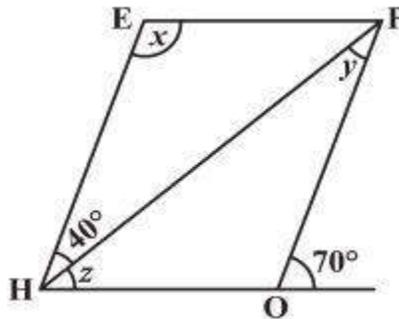
also,  $90^\circ + \angle B = 180^\circ$

$$\Rightarrow \angle B = 180^\circ - 90^\circ = 90^\circ$$

$$\angle A = \angle C = 90^\circ$$

$$\angle B = \angle D = 90^\circ$$

7. The adjacent figure HOPE is a parallelogram. Find the angle measures x, y and z. State the properties you use to find them.



**Solution:**

$$y = 40^\circ \text{ (alternate interior angle)}$$

$$\angle P = 70^\circ \text{ (alternate interior angle)}$$

$$\angle P = \angle H = 70^\circ \text{ (opposite angles of a parallelogram)}$$

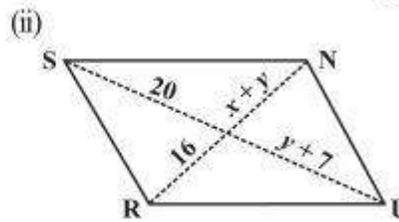
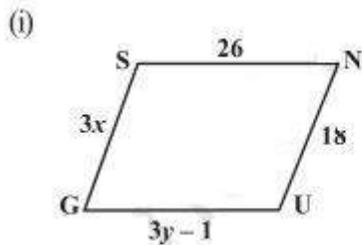
$$z = \angle H - 40^\circ = 70^\circ - 40^\circ = 30^\circ$$

$$\angle H + x = 180^\circ$$

$$\Rightarrow 70^\circ + x = 180^\circ$$

$$\Rightarrow x = 180^\circ - 70^\circ = 110^\circ$$

8. The following figures GUNS and RUNS are parallelograms. Find x and y. (Lengths are in cm)



**Solution:**

i)  $SG = NU$  and  $SN = GU$  (opposite sides of a parallelogram are equal)

$$3x = 18$$

$$\Rightarrow x = \frac{18}{3} = 6$$

$$3y - 1 = 26 \text{ and,}$$

$$\Rightarrow 3y = 26 + 1$$

$$\Rightarrow y = \frac{27}{3} = 9$$

$$x = 6 \text{ and } y = 9$$

ii)  $20 = y + 7$  and  $16 = x + y$  (diagonals of a parallelogram bisect each other)

$$y + 7 = 20$$

$$\Rightarrow y = 20 - 7 = 13 \text{ and,}$$

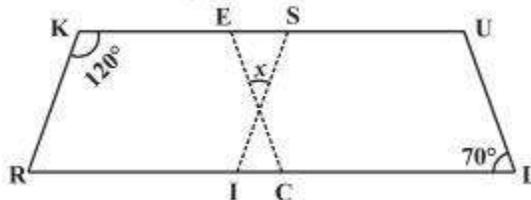
$$x + y = 16$$

$$\Rightarrow x + 13 = 16$$

$$\Rightarrow x = 16 - 13 = 3$$

$$x = 3 \text{ and } y = 13$$

9. In the above figure both RISK and CLUE are parallelograms. Find the value of  $x$ .



**Solution:**

$\angle K + \angle R = 180^\circ$  (adjacent angles of a parallelogram are supplementary)

$$\Rightarrow 120^\circ + \angle R = 180^\circ$$

$$\Rightarrow \angle R = 180^\circ - 120^\circ = 60^\circ$$

also,  $\angle R = \angle SIL$  (corresponding angles)

$$\Rightarrow \angle SIL = 60^\circ$$

also,  $\angle ECR = \angle L = 70^\circ$  (corresponding angles)

$x + 60^\circ + 70^\circ = 180^\circ$  (angle sum of a triangle)

$$\Rightarrow x + 130^\circ = 180^\circ$$

$$\Rightarrow x = 180^\circ - 130^\circ = 50^\circ$$

10. Explain how this figure is a trapezium. Which of its two sides are parallel? (Fig 3.32)

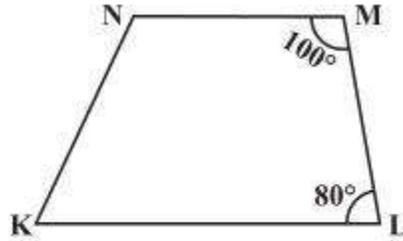


Fig 3.32

Solution:

When a transversal line intersects two lines in such a way that the sum of the adjacent angles on the same side of transversal is  $180^\circ$  then the lines are parallel to each other.  
 Here,  $\angle M + \angle L = 100^\circ + 80^\circ = 180^\circ$   
 Thus,  $MN \parallel LK$   
 As the quadrilateral KLMN has one pair of parallel line therefore it is a trapezium.  
 MN and LK are parallel lines.

11. Find  $m\angle C$  in Fig 3.33 if  $AB \parallel DC$  ?

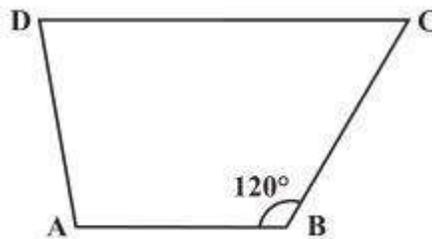


Fig 3.33

Solution:

$$\begin{aligned} m\angle C + m\angle B &= 180^\circ \text{ (angles on the same side of transversal)} \\ \Rightarrow m\angle C + 120^\circ &= 180^\circ \\ \Rightarrow m\angle C &= 180^\circ - 120^\circ = 60^\circ \end{aligned}$$

12. Find the measure of  $\angle P$  and  $\angle S$  if  $SP \parallel RQ$  ? in Fig 3.34. (If you find  $m\angle R$ , is there more than one method to find  $m\angle P$ ?)

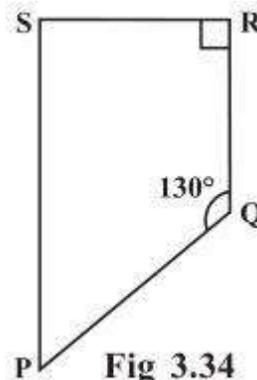


Fig 3.34

Solution:

$$\angle P + \angle Q = 180^\circ \text{ (angles on the same side of transversal)}$$

$$\Rightarrow \angle P + 130^\circ = 180^\circ$$

$$\Rightarrow \angle P = 180^\circ - 130^\circ = 50^\circ$$

$$\text{also, } \angle R + \angle S = 180^\circ \text{ (angles on the same side of transversal)}$$

$$\Rightarrow 90^\circ + \angle S = 180^\circ$$

$$\Rightarrow \angle S = 180^\circ - 90^\circ = 90^\circ$$

Thus,  $\angle P = 50^\circ$  and  $\angle S = 90^\circ$

Yes, there are more than one method to find  $m\angle P$ .

PQRS is a quadrilateral. Sum of measures of all angles is  $360^\circ$ .

Since, we know the measurement of  $\angle Q$ ,  $\angle R$  and  $\angle S$ .

$$\angle Q = 130^\circ, \angle R = 90^\circ \text{ and } \angle S = 90^\circ$$

$$\angle P + 130^\circ + 90^\circ + 90^\circ = 360^\circ$$

$$\Rightarrow \angle P + 310^\circ = 360^\circ$$

$$\Rightarrow \angle P = 360^\circ - 310^\circ = 50^\circ$$

## Exercise 3.4

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1. State whether True or False.

- a) All rectangles are squares.
- b) All rhombuses are parallelograms.
- c) All squares are rhombuses and also rectangles.
- d) All squares are not parallelograms.
- e) All kites are rhombuses.
- f) All rhombuses are kites.
- g) All parallelograms are trapeziums.
- h) All squares are trapeziums.

Solution:

- a) False.  
Because, all square are rectangles but all rectangles are not square.
- b) True
- c) True
- d) False.  
Because, all squares are parallelograms as opposite sides are parallel and opposite angles are equal.
- e) False.  
Because, for example, a length of the sides of a kite are not of same length.
- f) True
- g) True
- h) True

2. Identify all the quadrilaterals that have.

- (a) four sides of equal length    (b) four right angles

Solution:

- a) Rhombus and square have all four sides of equal length.
- b) Square and rectangle have four right angles.

3. Explain how a square is.

- (i) a quadrilateral    (ii) a parallelogram    (iii) a rhombus    (iv) a rectangle

Solution

- (i) Square is a quadrilateral because it has four sides.
- (ii) Square is a parallelogram because it's opposite sides are parallel and opposite angles are equal.
- (iii) Square is a rhombus because all the four sides are of equal length and diagonals bisect at right angles.
- (iv) Square is a rectangle because each interior angle, of the square, is  $90^\circ$

4. Name the quadrilaterals whose diagonals.

- (i) bisect each other    (ii) are perpendicular bisectors of each other    (iii) are equal

Solution

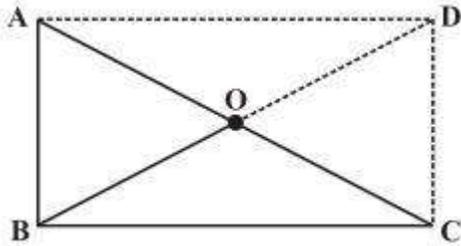
- (i) Parallelogram, Rhombus, Square and Rectangle
- (ii) Rhombus and Square
- (iii) Rectangle and Square

5. Explain why a rectangle is a convex quadrilateral.

**Solution**

Rectangle is a convex quadrilateral because both of its diagonals lie inside the rectangle.

6. ABC is a right-angled triangle and O is the mid-point of the side opposite to the right angle. Explain why O is equidistant from A, B and C. (The dotted lines are drawn additionally to help you).



**Solution**

AD and DC are drawn so that  $AD \parallel BC$  and  $AB \parallel DC$

$AD = BC$  and  $AB = DC$

ABCD is a rectangle as opposite sides are equal and parallel to each other and all the interior angles are of  $90^\circ$ .

In a rectangle, diagonals are of equal length and also bisect each other.

Hence,  $AO = OC = BO = OD$

Thus, O is equidistant from A, B and C.