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#### 1. Is zero a rational number? Can you write it in the form $\frac{p}{q}$ where p and q are integers and $q \neq 0$ ? Solution:

We know that, a number is said to be rational if it can be written in the form  $\frac{p}{q}$ , where p and q are integers and q≠0.

Taking the case of '0',

Zero can be written in the form  $\frac{0}{1}, \frac{0}{2}, \frac{0}{3}$ ... as well as,  $\frac{0}{-1}, \frac{0}{-2}, \frac{0}{-3}$ ...

Since it satisfies the necessary condition, we can conclude that 0 can be written in the  $\frac{p}{q}$  form, where q can

either be positive or negative number. Hence, 0 is a rational number.

#### 2. Find six rational numbers between 3 and 4.

#### Solution:

There are infinite rational numbers between 3 and 4.

As we have to find 6 rational numbers between 3 and 4, we will multiply both the numbers, 3 and 4, with 6+1=7 (or any number greater than 6)

i.e.,  $3 \times \frac{7}{7} = \frac{21}{7}$ and,  $4 \times \frac{7}{7} = \frac{28}{7}$  $\therefore$  The numbers in between  $\frac{21}{7}$  and  $\frac{28}{7}$  will be rational and will fall between 3 and 4. Hence,  $\frac{22}{7}$ ,  $\frac{23}{7}$ ,  $\frac{24}{7}$ ,  $\frac{25}{7}$ ,  $\frac{26}{7}$ ,  $\frac{27}{7}$  are the 6 rational numbers between 3 and 4.

# 3. Find five rational numbers between $\frac{3}{5}$ and $\frac{4}{5}$ .

#### Solution:

There are infinite rational numbers between  $\frac{3}{r}$  and  $\frac{4}{r}$ . To find out 5 rational numbers between  $\frac{3}{5}$  and  $\frac{4}{5}$ , we will multiply both the numbers,  $\frac{3}{5}$  and  $\frac{4}{5}$ , with 5+1=6 (or any number greater than 5)

nd, 
$$\frac{5}{4} \times \frac{6}{4} =$$

any number greater than 37 i.e.,  $\frac{3}{5} \times \frac{6}{6} = \frac{18}{30}$ and,  $\frac{4}{5} \times \frac{6}{6} = \frac{24}{30}$   $\therefore$  The numbers in between  $\frac{18}{30}$  and  $\frac{24}{30}$  will be rational and will fall between  $\frac{3}{5}$  and  $\frac{4}{5}$ . Hence,  $\frac{19}{30}$ ,  $\frac{20}{30}$ ,  $\frac{21}{30}$ ,  $\frac{22}{30}$ ,  $\frac{23}{30}$  are the 5 rational numbers between  $\frac{3}{5}$  and  $\frac{4}{5}$ .



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- 4. State whether the following statements are true or false. Give reasons for your answers.
- (i) Every natural number is a whole number.
- Solution:

#### True

Natural numbers- Numbers starting from 1 to infinity (without fractions or decimals)

i.e., Natural numbers= 1,2,3,4...

Whole numbers- Numbers starting from 0 to infinity (without fractions or decimals)

i.e., Whole numbers = 0, 1, 2, 3...

Or, we can say that whole numbers have all the elements of natural numbers and zero.

 $\therefore$  Every natural number is a whole number, however, every whole number is not a natural number.

#### (ii) Every integer is a whole number.

#### Solution:

#### False

Integers- Integers are set of numbers that contain positive, negative and 0; excluding fractional and decimal numbers.

i.e., integers= {...-4,-3,-2,-1,0,1,2,3,4...}

Whole numbers- Numbers starting from 0 to infinity (without fractions or decimals)

i.e., Whole numbers= 0,1,2,3....

Hence, we can say that integers includes whole numbers as well as negative numbers.

 $\therefore$  Every whole number is an integer, however, every integer is not a whole number.

#### (iii) Every rational number is a whole number.

#### Solution:

#### False

Rational numbers- All numbers in the form  $\frac{p}{q}$ , where p and q are integers and  $q \neq 0$ .

i.e., Rational numbers=  $0, \frac{19}{30}, 2, \frac{9}{-3}, \frac{-12}{7}$ ...

Whole numbers- Numbers starting from 0 to infinity (without fractions or decimals)

i.e., Whole numbers= 0,1,2,3....

Hence, we can say that integers includes whole numbers as well as negative numbers.

 $\therefore$  Every whole numbers are rational, however, every rational numbers are not whole numbers.



## Exercise 1.2

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## State whether the following statements are true or false. Justify your answers. (i) Every irrational number is a real number.

#### Solution:

#### True

Irrational Numbers- A number is said to be irrational, if it **cannot** be written in the  $\frac{p}{q}$ , where p and q are integers and  $q \neq 0$ .

i.e., Irrational numbers=  $0, \frac{19}{30}, 2, \frac{9}{-3}, \frac{-12}{7}, \sqrt{2}, \sqrt{5}, \pi, 0.102...$ 

Real numbers- The collection of both rational and irrational numbers are known as real numbers.

i.e., Real numbers =  $\sqrt{2}$ .  $\sqrt{5}$ ,  $\pi$ , 0.102...

: Every irrational number is a real number, however, every real numbers are not irrational numbers.

## (ii) Every point on the number line is of the form $\sqrt{m}$ , where m is a natural number. Solution:

#### False

The statement is false since as per the rule, a negative number cannot be expressed as square roots.

E.g.,  $\sqrt{9}=3$  is a natural number.

But  $\sqrt{2}=1.414$  is not a natural number.

Similarly, we know that there are negative numbers on the number line but when we take the root of a negative number it becomes a complex number and not a natural number.

E.g.,  $\sqrt{-7}=7i$ , where  $i=\sqrt{-1}$ 

 $\therefore$  The statement that every point on the number line is of the form  $\sqrt{m}$ , where m is a natural number is false.

#### (iii) Every real number is an irrational number.

#### Solution:

#### False

The statement is false, the real numbers include both irrational and rational numbers. Therefore, every real number cannot be an irrational number.

Real numbers- The collection of both rational and irrational numbers are known as real numbers.

i.e., Real numbers=  $\sqrt{2}$ .  $\sqrt{5}$ ,  $\pi$ , 0.102...

Irrational Numbers- A number is said to be irrational, if it **cannot** be written in the  $\frac{p}{q}$ , where p and q are integers

and  $q \neq 0$ .

i.e., Irrational numbers=  $0, \frac{19}{30}, 2, \frac{9}{-3}, \frac{-12}{7}, \sqrt{2}, \sqrt{5}, \pi, 0.102...$ 

.. Every irrational number is a real number, however, every real number is not irrational.

# 2. Are the square roots of all positive integers irrational? If not, give an example of the square root of a number that is a rational number.

#### Solution:

No, the square roots of all positive integers are not irrational.

For example,

 $\sqrt{4} = 2$  is rational.

 $\sqrt{9} = 3$  is rational.

Hence, the square roots of positive integers 4 and 9 are not irrational. (2 and 3, respectively).



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3. Show how 5 can be represented on the number line. Solution: Step 1: Let line AB be of 2 unit on a number line. Step 2: At B, draw a perpendicular line BC of length 1 unit. Step 3: Join CA Step 4: Now, ABC is a right angled triangle. Applying Pythagoras theorem,  $AB^2+BC^22=CA^2$  $2^2+1^2=CA^2 \Rightarrow CA^2=5$  $\Rightarrow CA = \sqrt{5}$  Thus, CA is a line of length  $\sqrt{5}$  unit. Step 4: Taking CA as a radius and A as a center draw an arc touching the number line. The point at which number line get intersected by arc is at  $\sqrt{5}$  distance from 0 because it is a radius of the circle whose center was A.

Thus,  $\sqrt{5}$  is represented on the number line as shown in the figure.



4. Classroom activity (Constructing the 'square root spiral') : Take a large sheet of paper and construct the 'square root spiral' in the following fashion. Start with a point O and draw a line segment OP1 of unit length. Draw a line segment P1P2 perpendicular to OP1 of unit length (see Fig. 1.9). Now draw a line segment P2P3 perpendicular to OP2. Then draw a line segment P3P4 perpendicular to OP3. Continuing in Fig. 1.9 :



Constructing this manner, you can get the line segment Pn-1Pn by square root spiral drawing a line segment of unit length perpendicular to OPn-1. In this manner, you will have created the points P2, P3,..., Pn,..., and joined them to create a beautiful spiral depicting 2, 3, 4, ... Solution:





- Step 1: Mark a point O on the paper. Here, O will be the center of the square root spiral.
- Step 2: From O, draw a straight line, OA, of 1cm horizontally.
- Step 3: From A, draw a perpendicular line, AB, of 1 cm.
- Step 4: Join OB. Here, OB will be of  $\sqrt{2}$
- Step 5: Now, from B, draw a perpendicular line of 1 cm and mark the end point C.
- Step 6: Join OC. Here, OC will be of  $\sqrt{3}$
- Step 7: Repeat the steps to draw  $\sqrt{4}$ ,  $\sqrt{5}$ ,  $\sqrt{6}$  ...



## Exercise 1.3

- Page: 14 1. Write the following in decimal form and say what kind of decimal expansion each has :
- (i)  $\frac{36}{100}$

Solution:

= 0.36 (Terminating)

(ii) 
$$\frac{1}{11}$$

Solution:



= 0.0909... = 0.09 (Non terminating and repeating)

$$(iii)4\frac{1}{8}$$

Solution:

$$4\frac{1}{8} = \frac{33}{8}$$



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Exercise 1.3	Page:
$ \begin{array}{r} 4.125 \\ 8 \overline{)33} \\ 32 \\ 10 \\ 8 \\ 20 \\ 16 \\ 40 \\ 0 \\ \end{array} $ = 4.125 (Terminating)	
(iv) $\frac{3}{13}$ Solution:	
$ \begin{array}{c}             0.230769 \\             13 \overline{ 30} \\             26 \\             40 \\             39 \\             10 \\             0 \\           $	
$= 0.230769 = 0.\overline{230769}$ (Non terminating and repeating)	
$\left(v\right)\frac{2}{11}$ Solution:	
$ \begin{array}{c} 0.18 \\ 11 \\ 2 \\ 0 \\ 20 \\ 11 \\ 90 \\ 88 \\ 2 \end{array} $	

=  $0.181818181818... = 0.\overline{18}$  (Non terminating and repeating)



## Exercise 1.3

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(vi) \frac{329}{400}
Solution:
```

	0.8225
400	329
	0
	3290
	3200
	900
	800
	1000
	800
	2000
	2000
	0

= 0.8225 (Terminating)

2. You know that  $\frac{1}{7} = 0.\overline{142857}$ . Can you predict what the decimal expansions of  $\frac{2}{7}, \frac{3}{7}, \frac{4}{7}, \frac{5}{7}, \frac{6}{7}$  are, without actually doing the long division? If so, how?

[Hint: Study the remainders while finding the value of  $\frac{1}{7}$  carefully.] Solution:

$$\frac{1}{7} = 0.\overline{142857}$$
  

$$\therefore 2 \times \frac{1}{7} = 2 \times 0.\overline{142857} = 0.\overline{285714}$$
  

$$3 \times \frac{1}{7} = 3 \times 0.\overline{142857} = 0.\overline{428571}$$
  

$$4 \times \frac{1}{7} = 4 \times 0.\overline{142857} = 0.\overline{571428}$$
  

$$5 \times \frac{1}{7} = 5 \times 0.\overline{142857} = 0.\overline{714285}$$
  

$$6 \times \frac{1}{7} = 6 \times 0.\overline{142857} = 0.\overline{857142}$$

3. Express the following in the form  $\frac{p}{q}$ , where p and q are integers and  $q \neq 0$ .

(i)  $0.\,\overline{6}$ 

Solution: 0.  $\overline{6} = 0.666...$ Assume that x = 0.666...Then, 10x = 6.666... 10x = 6 + x 9x = 6 $x = \frac{2}{3}$ 



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(ii) 
$$0.\overline{47}$$
  
Solution:  
 $0.\overline{47} = 0.4777...$   
 $= \frac{4}{10} + \frac{0.777}{10}$   
Assume that  $x = 0.777...$   
 $10x = 7 + x$   
 $x = \frac{7}{9}$   
 $\frac{4}{10} + \frac{0.777...}{10} = \frac{4}{10} + \frac{7}{90} (\because x = \frac{7}{9} \text{ and } x = 0.777... \Rightarrow \frac{0.777...}{10} = \frac{7}{9\times10} = \frac{7}{90})$   
 $= \frac{36}{90} + \frac{7}{90} = \frac{43}{90}$   
(iii)  $0.\overline{001}$   
Solution:  
 $0.\overline{001} = 0.001001...$   
Assume that  $x = 0.001001...$   
Then,  $1000x = 1.001001...$   
 $1000x = 1 + x$   
 $999x = 1$   
 $x = \frac{1}{999}$ 

4. Express 0.99999.... in the form  $\frac{p}{q}$ . Are you surprised by your answer? With your teacher and classmates discuss why the answer makes sense.

Solution: Assume that x = 0.9999... Eq. (a) Multiplying both sides by 10, 10x = 9.9999... Eq. (b) Eq.(b) – Eq.(a), we get  $10x = 9.9999... - \frac{x = 0.9999...}{9x = 9}$ x = 1

The difference between 1 and 0.9999999 is 0.000001 which is negligible. Hence, we can conclude that, 0.999 is too much near 1, therefore, 1 as the answer can be justified.

5. What can the maximum number of digits be in the repeating block of digits in the decimal expansion of  $\frac{1}{17}$ ? Perform the division to check your answer.

Solution:  $\frac{1}{17}$ 



Exercise 1.3	
Dividing 1 by 17:	

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 $\frac{1}{17} = 0.\overline{0588235294117647}$ 

:, There are 16 digits in the repeating block of the decimal expansion of  $\frac{1}{17}$ 



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6. Look at several examples of rational numbers in the form  $\frac{p}{q}$  (q  $\neq$  0), where p and q are integers with no common factors other than 1 and having terminating decimal representations (expansions). Can you guess what property q must satisfy? Solution:

We observe that when q is 2, 4, 5, 8, 10... Then the decimal expansion is terminating. For example:

$$\frac{1}{2} = 0.5$$
, denominator  $q = 2^{1}$ 

 $\frac{7}{8} = 0.875$ , denominator q = 2<sup>3</sup>

 $\frac{4}{5} = 0.8$ , denominator  $q = 5^1$ 

We can observe that the terminating decimal may be obtained in the situation where prime factorization of the denominator of the given fractions has the power of only 2 or only 5 or both.

## 7. Write three numbers whose decimal expansions are non-terminating non-recurring. Solution:

We know that all irrational numbers are non-terminating non-recurring. ∴, three numbers with decimal expansions that are non-terminating non-recurring are:

- a)  $\sqrt{3} = 1.732050807568$
- b)  $\sqrt{26} = 5.099019513592$
- c)  $\sqrt{101} = 10.04987562112$
- 8. Find three different irrational numbers between the rational numbers  $\frac{5}{7}$  and  $\frac{9}{11}$ .

Solution:

$$\frac{5}{7} = 0.$$
 714285

 $\frac{9}{11} = 0.\overline{81}$ 

∴,Three different irrational numbers are:

- a) 0.73073007300073000073...
- b) 0.75075007300075000075...
- c) 0.7607600760007600076...
- 9. Classify the following numbers as rational or irrational according to their type:

(i)  $\sqrt{23}$  Solution:

 $\sqrt{23} = 4.79583152331...$ 

Since the number is non-terminating non-recurring therefore, it is an irrational number.



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# (ii) $\sqrt{225}$ Solution:

 $\sqrt{225} = 15 = 15/1$ 

Since the number can be represented in  $\frac{p}{q}$  form, it is a rational number.

#### (iii) **0.3796**

Solution: Since the number, 0.3796, is terminating, it is a rational number.

#### (iv) 7.478478

Solution: The number, 7.478478, is non-terminating but recurring, it is a rational number.

#### (v) 1.101001000100001...

#### Solution:

Since the number, 1.101001000100001..., is non-terminating non-repeating (non-recurring), it is an irrational number.



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# **2.** Visualise $4.\overline{26}$ on the number line, up to 4 decimal places. Solution:

- 4.26=4.26262626.....
- $4.\overline{26}$  up to 4 decimal places= 4.2626





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1. Classify the following numbers as rational or irrational:

(i)  $2 - \sqrt{5}$ 

Solution:

We know that,  $\sqrt{5} = 2.2360679...$ Here, 2.2360679...is non-terminating and non-recurring. Now, substituting the value of  $\sqrt{5}$  in  $2 - \sqrt{5}$ , we get,  $2 - \sqrt{5} = 2 - 2.2360679... = -0.2360679...$ Since the number, -0.2360679... is non-terminating non-recurring,  $2 - \sqrt{5}$  is an irrational number.

(ii) 
$$(3 + \sqrt{23}) - \sqrt{23}$$
  
Solution:  
 $(3 + \sqrt{23}) - \sqrt{23} = 3 + \sqrt{23} - \sqrt{23}$   
 $= 3$   
 $= \frac{3}{1}$ 

Since the number,  $\frac{3}{1}$ , is in  $\frac{p}{q}$  form,  $(3 + \sqrt{23}) - \sqrt{23}$  is rational.

# (iii) $\frac{2\sqrt{7}}{7\sqrt{7}}$

Solution:

$$\frac{2\sqrt{7}}{7\sqrt{7}} = \frac{2}{7} \times \frac{\sqrt{7}}{\sqrt{7}}$$

We know that,  $\frac{\sqrt{7}}{\sqrt{7}} = 1$ Hence,

$$\frac{2}{7} \times \frac{\sqrt{7}}{\sqrt{7}} = \frac{2}{7} \times 1$$
$$= \frac{2}{7}$$

Since the number,  $\frac{2}{7}$ , is in  $\frac{p}{q}$  form,  $\frac{2\sqrt{7}}{7\sqrt{7}}$  is rational.

(iv) 
$$\frac{1}{\sqrt{2}}$$

Solution:

Multiplying and dividing numerator and denominator by  $\sqrt{2}$ , we get,

$$\frac{1}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2} \text{ [Since } \sqrt{2} \times \sqrt{2} = 2\text{]}$$



## Exercise 1.5

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We know that,  $\sqrt{2} = 1.4142...$ Then,  $\frac{\sqrt{2}}{2} = \frac{1.4142...}{2} = 0.7071...$ Since the number, 0.7071..., is non-terminating non-recurring,  $\frac{1}{\sqrt{2}}$  is an irrational number.

#### (v) 2π

Solution:

We know that, the value of  $\pi = 3.1415 ...$ Hence,  $2\pi = 2 \times 3.1415 ...$ = 6.2830...

Since the number, 6.2830..., is non-terminating non-recurring,  $2\pi$  is an irrational number.

#### 2. Simplify each of the following expressions:

(i)  $(3 + \sqrt{3}) (2 + \sqrt{2})$ Solution:  $(3 + \sqrt{3}) (2 + \sqrt{2})$ Opening the brackets, we get,  $(3 \times 2) + (3 \times \sqrt{2}) + (\sqrt{3} \times 2) + \sqrt{3} \times \sqrt{2}$  $= 6 + 3\sqrt{2} + 2\sqrt{3} + \sqrt{6}$ 

(ii)  $(3 + \sqrt{3}) (3 - \sqrt{3})$ Solution:  $(3 + \sqrt{3}) (3 - \sqrt{3}) = 3^2 - (\sqrt{3}^2) = 9 - 3$ 

= 6

(iii)  $(\sqrt{5} + \sqrt{2})^2$ Solution:

$$(\sqrt{5} + \sqrt{2})^2 = \sqrt{5}^2 + (2 \times \sqrt{5} \times \sqrt{2}) + \sqrt{2}^2$$
  
= 5 + 2 × \sqrt{10} + 2  
= 7 + 2\sqrt{10}

(iv) 
$$(\sqrt{5} - \sqrt{2}) (\sqrt{5} + \sqrt{2})$$
  
Solution:  
 $(\sqrt{5} - \sqrt{2}) (\sqrt{5} + \sqrt{2}) = \sqrt{5}^2 - \sqrt{2}^2)$   
 $= 5 - 2$   
 $= 7$ 



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3. Recall,  $\pi$  is defined as the ratio of the circumference (say c) of a circle to its diameter, (say d). That is,  $\pi = \frac{c}{d}$ . This seems to contradict the fact that  $\pi$  is irrational. How will you resolve this contradiction?

#### Solution:

There is no contradiction. When we measure a value with a scale, we only obtain an approximate value. We never obtain an exact value. Therefore, we may not realize whether c or d is irrational. The value of  $\pi$ is almost equal to  $\frac{22}{7}$  or 3.142857...

4. Represent  $(\sqrt{9.3})$  on the number line.

#### Solution:

Step 1: Draw a 9.3 units long line segment, AB. Extend AB to C such that BC=1 unit.

Step 2: Now, AC = 10.3 units. Let the centre of AC be O.

Step 3: Draw a semi-circle of radius OC with centre O.

Step 4: Draw a BD perpendicular to AC at point B intersecting the semicircle at D. Join OD.

Step 5: OBD, obtained, is a right angled triangle.

Here, OD  $\frac{10.3}{2}$  (radius of semi-circle), OC =  $\frac{10.3}{2}$ , BC = 1

$$OB^2 = OC - BC$$

$$\implies (\frac{10.3}{2}) - 1 = \frac{8}{2}$$

8.3 2 (-2) - 1 = -

Using Pythagoras theorem, We get,  $OD^2 - RD^2 + OB^2$ 

Thus, the length of BD is  $\sqrt{9.3}$ .

Step 6: Taking BD as radius and B as centre draw an arc which touches the line segment. The point where it touches the line segment is at a distance of  $\sqrt{9.3}$  from O as shown in the figure.





## Exercise 1.5

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- 5. Rationalize the denominators of the following:
- (i)  $\frac{1}{\sqrt{7}}$
- Solution:

Multiply and divide  $\frac{1}{\sqrt{7}}$  by  $\sqrt{7}$ 

$$\frac{1 \times \sqrt{7}}{\sqrt{7} \times \sqrt{7}} = \frac{\sqrt{7}}{7}$$

(ii)  $\frac{1}{\sqrt{7}-\sqrt{6}}$ Solution:

Multiply and divide  $\frac{1}{\sqrt{7}-\sqrt{6}}$  by  $\sqrt{7}+\sqrt{6}$  $\frac{1}{\sqrt{7}-\sqrt{6}} \times \frac{\sqrt{7}+\sqrt{6}}{\sqrt{7}+\sqrt{6}} = \frac{\sqrt{7}+\sqrt{6}}{(\sqrt{7}-\sqrt{6})(\sqrt{7}+\sqrt{6})}$ 

$$\frac{1}{\sqrt{7}-\sqrt{6}} \times \frac{\sqrt{7}+\sqrt{6}}{\sqrt{7}+\sqrt{6}} = \frac{\sqrt{7}+\sqrt{6}}{(\sqrt{7}-\sqrt{6})(\sqrt{7}+\sqrt{6})}$$

$$= \frac{\sqrt{7}+\sqrt{6}}{\sqrt{7}^2-\sqrt{6}^2} \qquad [\text{denominator is obtained by the property, } (a+b)(a-b)=a^2-b^2]$$

$$= \frac{\sqrt{7}+\sqrt{6}}{7-6}$$

$$= \frac{\sqrt{7}+\sqrt{6}}{1}$$

$$= \sqrt{7}+\sqrt{6}$$
(iii)  $\frac{1}{\sqrt{5}+\sqrt{2}}$ 
Solution:  
Multiply and divide  $\frac{1}{\sqrt{5}+\sqrt{2}}$  by  $\sqrt{5}-\sqrt{2}$ 

$$1 = \sqrt{5}-\sqrt{2}$$

Multiply and divide 
$$\frac{1}{\sqrt{5}+\sqrt{2}}$$
 by  $\sqrt{5}-\sqrt{2}$   
 $\frac{1}{\sqrt{5}+\sqrt{2}} \times \frac{\sqrt{5}-\sqrt{2}}{\sqrt{5}-\sqrt{2}} = \frac{\sqrt{5}-\sqrt{2}}{(\sqrt{5}+\sqrt{2})(\sqrt{5}-\sqrt{2})}$ 

$$= \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5}^2 - \sqrt{2}^2}$$
$$= \frac{\sqrt{5} - \sqrt{2}}{5 - 2}$$
$$= \frac{\sqrt{5} - \sqrt{2}}{3}$$

[denominator is obtained by the property,  $(a+b)(a-b)=a^2 - b^2$ ]



Exercise 1.5 Page: 24  $(iv)\frac{1}{\sqrt{7}-2}$ Solution: Multiply and divide  $\frac{1}{\sqrt{7}-2}$  by  $\sqrt{7}+2$  $\frac{1}{\sqrt{7}-2} \times \frac{\sqrt{7}+2}{\sqrt{7}+2} = \frac{\sqrt{7}+2}{(\sqrt{7}-2)(\sqrt{7}+2)}$  $=\frac{\sqrt{7}+2}{\sqrt{7}^2-2^2}$ [denominator is obtained by the property,  $(a+b)(a-b)=a^2 - b^2$ ]  $=\frac{\sqrt{7}+2}{7-4}$  $=\frac{\sqrt{7}+2}{3}$ 



Exercise 1.6		Page: 26
1. Find: (i) $64^{\frac{1}{2}}$ Solution: $64^{\frac{1}{2}} = (8 \times 8)^{\frac{1}{2}}$ $= (8^{2})^{\frac{1}{2}}$ $= 8^{1}$ = 8	$[2 \times \frac{1}{2} = \frac{2}{2} = 1]$	
(ii) $32^{\frac{1}{5}}$ Solution: $32^{\frac{1}{5}} = (2 \times 2 \times 2 \times 2^{5})^{\frac{1}{5}}$	$2 \times 2 \times 2)^{\frac{1}{5}}$	
$= 2^{1}$ = 2	$[5 \times \frac{1}{5} = \frac{5}{5} = 1]$	
(iii) 1253 Solution: $125^{\frac{1}{3}} = (5 \times 5 \times 5)$ $= (5^{3})^{\frac{1}{3}}$ $= 5^{1}$ = 5	$(5)^{\frac{1}{3}}$ $[3 \times \frac{1}{3} = \frac{3}{3} = 1]$	
2. Find: (i) $9^{\frac{3}{2}}$ Solution: $9^{\frac{3}{2}} = (3 \times 3)^{\frac{3}{2}}$ $= (3^2)^{\frac{1}{2}}$ $= 3^3$ = 27	$[2 \times \frac{3}{2} = 3]$	



<u>Exercise 1.6</u>	Page: 26
(ii) $32^{\frac{2}{5}}$	
$32^{\frac{2}{5}} = (2 \times 2 \times 2 \times 2 \times 2)^{\frac{2}{5}}$	
$= (2^5)^{2/5} - 2^2 \qquad [5 \times \frac{2}{5} - 2]$	
$=2$ $=4$ $[3 \times \frac{5}{5} - 2]$	
(iii) $16^{\frac{3}{4}}$ Solution:	
$16^{\frac{3}{4}} = (2 \times 2 \times 2 \times 2)^{\frac{3}{4}}$	
$= (2^4)^{3/4}$ = 2 <sup>3</sup> [4× $\frac{3}{2}$ = 3]	
= 8	
(iv) $125^{\frac{-1}{3}}$	
$125^{\frac{-1}{3}} = (5 \times 5 \times 5)^{\frac{-1}{3}}$	
$= (5^3)^{-1/3}$	
$= 5^{-1} \qquad [3 \times \frac{1}{3} = -1]$ $= \frac{1}{5}$	
3. Simplify:	
(i) $2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}}$	
Solution: $2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}} = 2^{(\frac{2}{3} + \frac{1}{5})}$ [Since, $a^{m} \cdot a^{n} = a^{m+n}$ Laws of exponents]	
$= 2^{\frac{13}{15}} \qquad \qquad \left[\frac{2}{3} + \frac{1}{5} = \frac{2 \times 5 + 3 \times 1}{3 \times 5} = \frac{13}{15}\right]$	
(ii) $\left(\frac{1}{3^3}\right)^7$ Solution:	



