

## PUNJAB BOARD CLASS 10 MATHS SAMPLE PAPER-SET 1

### Answers & Explanations SECTION-A

**1. Solution:**

Let  $n$  be the no. of rational numbers.

Here,  $n=4$

Denominator =  $n + 1 = 4 + 1 = 5$ .

$$3 = \frac{3}{1} \times \frac{5}{5} = \frac{15}{5} \quad \text{and} \quad 4 = \frac{4}{1} \times \frac{5}{5} = \frac{20}{5}$$

∴ Four rational numbers between 3 and 4 are: -

$$\frac{16}{5}, \frac{17}{5}, \frac{18}{5}, \frac{19}{5}$$

**2. Solution:**

$$14x^2 + 25x + 6 = 0$$

$$\Rightarrow 14x^2 + 21x + 4x + 6 = 0$$

$$\Rightarrow 7x(2x + 3) + 2(2x + 3) = 0$$

$$\Rightarrow (2x + 3)(7x + 2) = 0$$

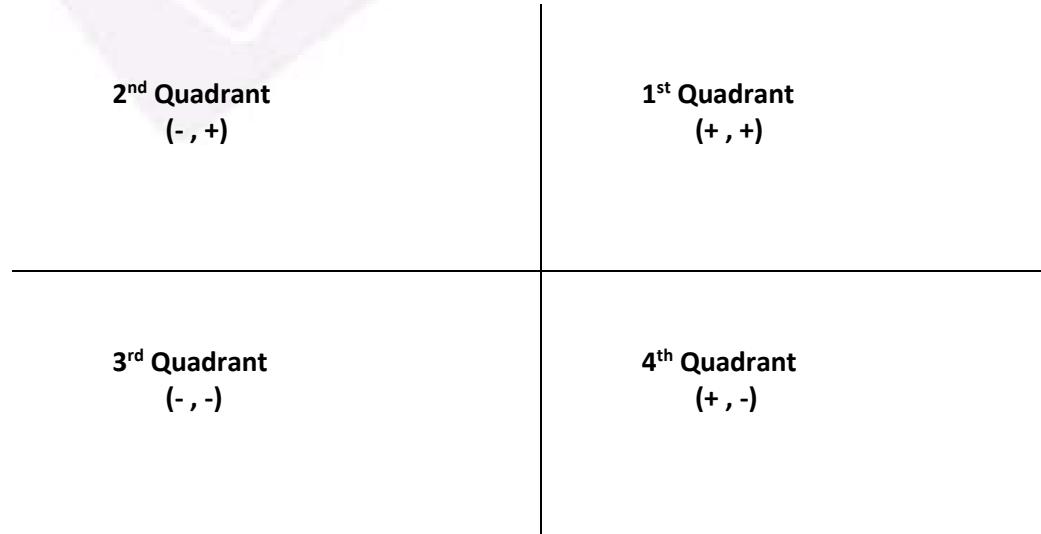
Therefore, the value of  $x = -\frac{3}{2}$  or  $-\frac{2}{7}$

**3. Solution:**

Given,  $a = 17$ ,  $d = 6$ ,  $n = 100$ .

$$\begin{aligned}\therefore \text{Sum of 100 terms} &= \frac{n}{2}(2a + (n - 1)d) \\ &= \frac{100}{2}(2 \times 17 + (100 - 1)6) \\ &= 50(34 + 99 \times 6) \\ &= 50(34 + 594) \\ &= 50 \times 628 \\ &= 31400\end{aligned}$$

**4. Solution:**



(-3,1) lies in 2<sup>nd</sup> quadrant.

(1, -2) lies in 4<sup>th</sup> quadrant.

**5. Solution:**

$$\frac{\sin\theta}{\cos(90^\circ-\theta)} - \frac{\cos(90^\circ-\theta)}{\sin\theta} = \frac{\sin\theta}{\sin\theta} + \frac{\sin\theta}{\sin\theta} = 1 + 1 = 2$$

[ $\because \cos(90^\circ - \theta) = \sin\theta$ ]

**6. Solution:**

120° can be constructed using a compass and scale only, by constructing 60° twice.

30° can be constructed using a compass and scale only, by bisecting 60°.

45° be constructed using a compass and scale only, by constructing a 90° and then bisecting it.

20° cannot be constructed using a compass and scale only, a protractor is needed for this construction.

**7. Solution:**

The angle subtended by a chord at the centre of a circle is twice the angle subtended by a chord at the circumference of a circle.

$\therefore$  The angle it makes on the circumference

$$= \frac{148^\circ}{2} = 74^\circ$$

**8. Solution:**

Out of 80 students, 32 are girls, 48 are boys.

$$\therefore \text{Probability of a boy winning} = \frac{48}{80} = \frac{3}{5}$$

## SECTION-B

**9. Solution:**

Given,  $x = \sqrt{2} + 1$

$$\begin{aligned}\therefore \left(x + \frac{1}{x}\right)^2 &= \left((\sqrt{2} + 1) + \frac{1}{\sqrt{2}+1}\right)^2 \\ &= \left(\frac{(\sqrt{2}+1)^2+1}{\sqrt{2}+1}\right)^2 \\ &= \left(\frac{2+2\sqrt{2}+1+1}{\sqrt{2}+1}\right)^2 \\ &= \left(\frac{4+2\sqrt{2}}{\sqrt{2}+1}\right)^2 \\ &= \frac{16+16\sqrt{2}+8}{2+2\sqrt{2}+1} \\ &= \frac{24+16\sqrt{2}}{3+2\sqrt{2}}\end{aligned}$$

Rationalizing the denominator,

$$\begin{aligned}&= \frac{24+16\sqrt{2}}{3+2\sqrt{2}} \times \frac{3-2\sqrt{2}}{3-2\sqrt{2}} \\ &= \frac{72+48\sqrt{2}-48\sqrt{2}-64}{((3)^2-(2\sqrt{2})^2} \\ &= \frac{8}{9-8}\end{aligned}$$

$$= \frac{8}{1} \\ = 8$$

**10. Solution:**

Let,  $f(x) = x^4 - 3x^2 + kx - 5$

Given,  $f(x)$  when divided by  $(x - 2)$  leaves a remainder 3, i.e.  $f(2) = 3$

$$\Rightarrow 2^4 - 3 \cdot 2^2 + k \cdot 2 - 5 = 3$$

$$\Rightarrow 16 - 12 + 2k - 5 = 3$$

$$\Rightarrow 2k - 1 = 3$$

$$\Rightarrow 2k = 3 + 1 = 4$$

$$\Rightarrow k = \frac{4}{2} = 2$$

Thus, the value of  $k$  is 2 and the polynomial is

$$x^4 - 3x^2 + 2x - 5.$$

**11. Solution:**

Given,  $y = 14 - x$

$$\begin{array}{r} x + y = 14 \quad \dots(i) \\ x - y = 8 \quad \dots(ii) \\ \hline 2x = 22 \\ \Rightarrow x = \frac{22}{2} = 11 \end{array}$$

Putting  $x = 11$  in (i), we get,

$$11 + y = 14$$

$$\Rightarrow y = 14 - 11$$

$$\Rightarrow y = 3$$

$$\therefore x = 11$$

$$y = 3$$

**12. Solution:**

$$x^2 - 3x - 4 = 0 \quad \dots(i)$$

Comparing (i) with standard quadratic equation

$$ax^2 + bx + c = 0, \text{ we get, } a = 1, b = -3, c = -4$$

Putting these values of  $a, b, c$  in Sridhar Acharya Formula, we get,

$$x = \frac{(-b) \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \times 1 \times (-4)}}{2 \times 1}$$

$$\Rightarrow x = \frac{3 \pm \sqrt{9 - 4 \times 1 \times (-4)}}{2}$$

$$\Rightarrow x = \frac{3 \pm \sqrt{9 + 16}}{2}$$

$$\Rightarrow x = \frac{3 \pm \sqrt{25}}{2}$$

$$\Rightarrow x = \frac{3 \pm 5}{2}$$

$$\Rightarrow x = \frac{3+5}{2}, \frac{3-5}{2}$$

$$\Rightarrow x = \frac{8}{2}, -\frac{2}{2}$$

$$\Rightarrow x = 4, -1.$$

**13. Solution:**

Base (b) = 12cm,  
 Hypotenuse (h) = 13cm.  
 $\therefore$  Perpendicular (p) = ?

According to Pythagoras Theorem,

$$\begin{aligned} p^2 + b^2 &= h^2 \\ \Rightarrow p^2 + 12^2 &= 13^2 \\ \Rightarrow p^2 + 144 &= 169 \\ \Rightarrow p^2 &= 169 - 144 \\ \Rightarrow p^2 &= 25 \\ \Rightarrow p &= \sqrt{25} \\ \Rightarrow p &= 5 \end{aligned}$$

#### 14. Solution:

Given, AB || CD.

In  $\triangle ABM$ ,

$$\angle MAB + \angle ABM + \angle AMB = 180^\circ$$

[Sum of all 3 angles of a  $\triangle$  is  $180^\circ$ ]

$$\begin{aligned} \Rightarrow 56^\circ + 78^\circ + \angle AMB &= 180^\circ \\ \Rightarrow 134^\circ + \angle AMB &= 180^\circ \\ \Rightarrow \angle AMB &= 180^\circ - 134^\circ = 46^\circ \\ \angle AMB &= \angle CMD \end{aligned}$$

$[\because$  Vertically Opposite Angles]

$$\angle CMD = 46^\circ$$

In  $\triangle CDM$ ,

$$\angle MCD + \angle CMD + \angle CDM = 180^\circ$$

[Sum of all 3 angles of a  $\triangle$  is  $180^\circ$ ]

$$\begin{aligned} \Rightarrow 62^\circ + 46^\circ + \angle CDM &= 180^\circ \\ \Rightarrow 108^\circ + \angle CDM &= 180^\circ \\ \Rightarrow \angle CDM &= 180^\circ - 108^\circ = 72^\circ \\ \therefore \angle AMB &= 46^\circ, \\ \angle CDM &= 72^\circ \end{aligned}$$

#### 15. Solution:

Given data: 8, 11, 23, 27, 35, 44, 67, 73, 85.

$$\therefore \text{Mean} = \frac{8+11+23+27+35+44+67+73+85}{9} = \frac{373}{9}$$

$$= 41\frac{4}{9}$$

$$\therefore \text{Median} = \frac{n+1}{2}^{\text{th}} \text{ observation}$$

[when n=odd number; here n = 9]

$$\begin{aligned} &= \frac{9+1}{2}^{\text{th}} \text{ observation} \\ &= \frac{10}{2}^{\text{th}} \text{ observation} \\ &= 5^{\text{th}} \text{ observation} \\ &= 35. \end{aligned}$$

$$\therefore \text{Mean} = 41\frac{4}{9}$$

$$\therefore \text{Median} = 35$$

#### 16. Solution:

Let H be the event of hitting a boundary.

$$\text{Then } P(H) = \frac{\text{No.of times he hits boundary}}{\text{Total no.of balls he plays}}$$

$$= \frac{12}{30} = \frac{2}{5}$$

$\therefore$  Probability of not hitting boundary =  $1 - P(H)$

$$\begin{aligned}&= 1 - \frac{2}{5} \\&= \frac{5-2}{5} = \frac{3}{5}\end{aligned}$$

## SECTION -C

### 17. Solution:

Given the common difference (d) is 3.

$$T_n = 35, \quad 2S_n = 430 \Rightarrow S_n = \frac{430}{2} = 21$$

Let the first term be a

We know,

$$T_n = a + (n-1)d$$

$$\Rightarrow 35 = a + (n-1)3$$

$$\Rightarrow 35 = a + (n-1)3$$

$$\Rightarrow (n-1)3 = 35 - a \dots(i)$$

$$\Rightarrow 3n - 3 = 35 - a$$

$$\Rightarrow 3n = 35 + 3 - a$$

$$\Rightarrow n = \frac{38-a}{3} \dots(ii)$$

$$\text{and } S_n = \frac{n}{2}(2a + (n-1)3)$$

$$\Rightarrow 215 = \frac{n}{2}(2a + 35 - a) \quad [\text{From (i)}]$$

$$\Rightarrow 215 = \frac{n}{2}(a + 35)$$

$$\Rightarrow 215 = \frac{38-a}{2 \times 3}(a + 35) \quad [\text{From (ii)}]$$

$$\Rightarrow 215 \times 6 = (38-a)(a+35)$$

$$\Rightarrow 1290 = 38a - a^2 + 1330 - 35a$$

$$\Rightarrow a^2 - 3a - 40 = 0$$

$$\Rightarrow a^2 - 8a + 5a - 40 = 0$$

$$\Rightarrow a(a-8) + 5(a-8) = 0$$

$$\Rightarrow (a-8)(a+5) = 0$$

Either

$$(a-8) = 0$$

$$a = 8$$

Putting

a = 8 in (ii), we get,

$$\Rightarrow n = \frac{38-8}{3}$$

$$\Rightarrow n = \frac{30}{3}$$

$$\Rightarrow n = 10$$

Or

$$a = -5$$

a = -5 in (ii), we get,

$$\Rightarrow n = \frac{38-(-5)}{3}$$

$$\Rightarrow n = \frac{43}{3}$$

$$\Rightarrow n = 14\frac{1}{3}$$

As no. of terms is whole number, and cannot be fraction,  $\therefore n = 10$  and  $a = 8$ .

**18. Solution:**

In  $\triangle ABC$  and  $\triangle BDC$ ,

$$\angle ABC = \angle BDC = 90^\circ$$

BC is common for both  $\triangle$

$$\therefore \triangle ABC \sim \triangle BDC \quad [\text{A.S. Axiom}]$$

$$\therefore \frac{AB}{CD} = \frac{BC}{BD} = \frac{AC}{BC}$$

Given, BC = 20cm, AB = 15 cm, BD = 12cm.

$$\frac{AB}{CD} = \frac{BC}{BD} \Rightarrow \frac{15}{CD} = \frac{20}{12}$$

$$\Rightarrow CD = \frac{15 \times 12}{20} = 9 \text{ cm}$$

$$\text{and, } \frac{BC}{BD} = \frac{AC}{BC} \Rightarrow \frac{20}{12} = \frac{AC}{20}$$

$$\Rightarrow AC = \frac{20 \times 20}{12} = 33.33 \text{ cm}$$

$$\therefore AD = AC + CD = 33.33 \text{ cm} + 9 \text{ cm} \\ = 42.33 \text{ cm}$$

**Or**

**Solution:**

Distance between 2 points is given by

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

(i) Distance between (2,3) and (1,4)

$$= \sqrt{(1 - 2)^2 + (4 - 3)^2}$$

$$= \sqrt{(-1)^2 + 1^2} = \sqrt{1 + 1}$$

$$= \sqrt{2} \text{ units}$$

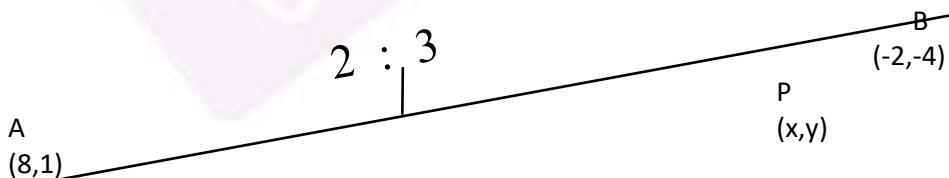
(ii) Distance between (-5,1) and (2,-7)

$$= \sqrt{(2 - (-5))^2 + (-7 - 1)^2}$$

$$= \sqrt{7^2 + (-8)^2} = \sqrt{49 + 64}$$

$$= \sqrt{113} \text{ units}$$

**19. Solution:**



Let,  $m_1:m_2 = 2:3$ ,

$$(x_1, y_1) = (8, 1) \text{ and } (x_2, y_2) = (-2, -4)$$

According to Section Formula

$$(x, y) = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$\Rightarrow (x, y) = \frac{2 \times (-2) + 3 \times 8}{2+3}, \frac{2 \times (-4) + 3 \times 1}{2+3}$$

$$\Rightarrow (x, y) = \frac{-4 + 24}{5}, \frac{-8 + 3}{5}$$

$$\Rightarrow (x, y) = \frac{20}{5}, \frac{-5}{5}$$

$$\Rightarrow (x, y) = (4, -1)$$

**Or**

**Solution:**

Given,  $\sin A = \frac{6}{10}$  and  $\cos A = \frac{8}{10}$

(i) R.H.S  $\rightarrow \sin^2 A + \cos^2 A = 1$

$$\begin{aligned}\text{L.H.S} &\rightarrow \sin^2 A + \cos^2 A = \left(\frac{6}{10}\right)^2 + \left(\frac{8}{10}\right)^2 \\ &= \frac{36}{100} + \frac{64}{100} = \frac{36+64}{100} = \frac{100}{100} = 1 = \text{R.H.S}\end{aligned}$$

[Hence Proved.]

(ii) Given  $\rightarrow 1 + \tan^2 A = \sec^2 A$

$$\begin{aligned}\text{L.H.S} &\rightarrow 1 + \tan^2 A = 1 + \left(\frac{\sin A}{\cos A}\right)^2 = 1 + \left(\frac{\frac{6}{10}}{\frac{8}{10}}\right)^2 \\ &= 1 + \left(\frac{6}{8}\right)^2 \\ &= 1 + \frac{36}{64} \\ &= \frac{64+36}{64} = \frac{100}{64} \\ &= \left(\frac{10}{8}\right)^2 \\ &= \left(\frac{5}{4}\right)^2 \\ &= \left[\because \cos A = \frac{8}{10} \therefore \sec A = \frac{1}{\cos A} = \frac{10}{8}\right] \\ &= \sec^2 A = \text{R.H.S} \quad [\text{Hence Proved.}]\end{aligned}$$

**20. Solution:**

Given,  $5 \tan \theta = 12$

$$\Rightarrow \tan \theta = \frac{12}{5}$$

We know,  $1 + \tan^2 \theta = \sec^2 \theta$

$$\Rightarrow 1 + \left(\frac{12}{5}\right)^2 = \sec^2 \theta$$

$$\Rightarrow 1 + \frac{144}{25} = \sec^2 \theta$$

$$\Rightarrow \sec^2 \theta = \frac{25+144}{25}$$

$$\Rightarrow \sec^2 \theta = \frac{169}{25}$$

$$\Rightarrow \sec \theta = \sqrt{\frac{169}{25}} = \frac{13}{5}$$

$$\therefore \cos \theta = \frac{1}{\sec \theta} = \frac{1}{\frac{13}{5}} = \frac{5}{13}$$

$$\therefore \sin \theta = \tan \theta \times \cos \theta \quad \left[ \because \tan \theta = \frac{\sin \theta}{\cos \theta} \right]$$

$$= \frac{12}{5} \times \frac{5}{13}$$

$$= \frac{12}{13}$$

$$\therefore \cot \theta = \frac{1}{\tan \theta} = \frac{1}{\frac{12}{5}} = \frac{5}{12}$$

$$\begin{aligned}\therefore \frac{\sin\theta - \cos\theta}{\cot\theta} &= \frac{\frac{12}{13} - \frac{5}{13}}{\frac{5}{12}} = \frac{\frac{12-5}{13}}{\frac{5}{12}} = \frac{\frac{7}{13}}{\frac{5}{12}} = \frac{7}{13} \div \frac{5}{12} \\ &= \frac{7}{13} \times \frac{12}{5} = \frac{84}{65}\end{aligned}$$

**21. Solution:**

Given,  $(1 - \sin\theta)(\sec\theta + \tan\theta) = \cos\theta$

L.H.S.

$$\begin{aligned}(1 - \sin\theta)(\sec\theta + \tan\theta) &= (\sec\theta - \sin\theta \sec\theta + \tan\theta - \sin\theta \tan\theta) \\ &= \left(\sec\theta - \frac{\sin\theta}{\cos\theta} + \tan\theta - \sin\theta \tan\theta\right) \\ &\quad \left[\because \sec\theta = \frac{1}{\cos\theta}\right] \\ &= (\sec\theta - \tan\theta + \tan\theta - \sin\theta \tan\theta) \\ &\quad \left[\because \frac{\sin\theta}{\cos\theta} = \tan\theta\right] \\ &= (\sec\theta - \sin\theta \tan\theta) \\ &\quad = \left(\sec\theta - \sin\theta \frac{\sin\theta}{\cos\theta}\right) \quad \left[\because \tan\theta = \frac{\sin\theta}{\cos\theta}\right] \\ &= \left(\frac{1}{\cos\theta} - \frac{\sin^2\theta}{\cos\theta}\right) \quad \left[\because \sec\theta = \frac{1}{\cos\theta}\right] \\ &= \frac{1-\sin^2\theta}{\cos\theta} = \frac{\cos^2\theta}{\cos\theta} \quad [\because \sin^2\theta + \cos^2\theta = 1] \\ &\quad \therefore [1 - \sin^2\theta = \cos^2\theta] \\ &= \cos\theta = \text{R.H.S} \\ &[\text{Hence Proved}]\end{aligned}$$

**22. Solution:**

Given,  $\angle CDB = 65^\circ$  and  $\angle ABD = 35^\circ$ .

BD is the diameter of the circle.

We know, angle in a semi-circle is right angle.

$$\therefore \angle CBD = 90^\circ$$

In  $\triangle DCB$

$$\angle CDB = 65^\circ$$

$$\angle CBD = 90^\circ$$

$$\therefore \angle DCB = 180^\circ - (\angle CDB + \angle CBD)$$

[ $\because$  Sum of all 3 angles of a  $\triangle$  is  $180^\circ$ .]

$$= 180^\circ - (65^\circ + 90^\circ)$$

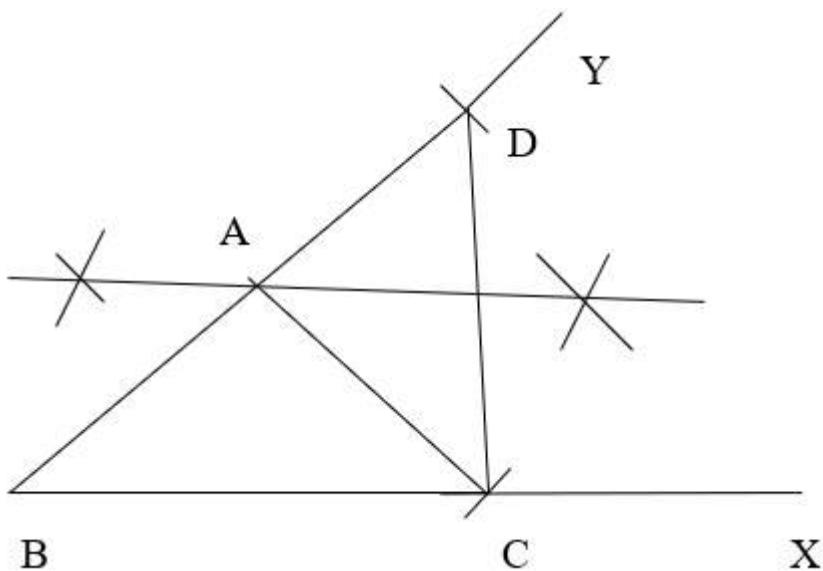
$$= 180^\circ - 155^\circ$$

$$= 25^\circ$$

$$\therefore \angle BAD = \angle DCB = 25^\circ$$

[Angles in the same segment of a circle are equal.]

23.



Steps of Construction: -

- i) Draw a line BX of length greater than BC and cut off line segment BC = 9.2 cm from it.
  - ii) Construct  $\angle CBY = 45^\circ$ .
  - iii) From BY, cut off a line segment BD = 16.4 cm.
  - iv) Join CD.
  - v) Draw perpendicular bisector of CD, Intersecting BY at a point A.
  - vi) Join AC.
- Hence, the required Triangle ABC.

#### 24. Solution:

We know, angle in a semi-circle is right angle.

$$\therefore \angle PRQ = 90^\circ$$

Given, PQ(h) = 12 cm, PR(b) = 5 cm

Applying Pythagoras Theorem,

$$QR^2 = PQ^2 + PR^2$$

$$\Rightarrow QR^2 = 12^2 + 5^2$$

$$\Rightarrow QR^2 = 144 + 25 = 169$$

$$\Rightarrow QR = \sqrt{169} = 13 \text{ cm.}$$

$$\therefore \text{Radius (r)} = OR = \frac{13}{2} \text{ cm.}$$

$\therefore$  Area of shaded region = Area of circle – Area of Triangle PQR

$$\begin{aligned}
 &= (\pi r^2) - \left( \frac{1}{2} \times b \times h \right) \\
 &= \left( \frac{22}{7} \times \left( \frac{13}{2} \right)^2 \right) - \left( \frac{1}{2} \times 5 \times 12 \right) \\
 &= \left( \frac{1859}{14} \right) - (30) \\
 &= \frac{1859 - 420}{14} = \frac{1439}{14} \\
 &= 102\frac{11}{14} \text{ cm}^2
 \end{aligned}$$

**Or**

**Solution:**

Given, Circumference = 44 cm

$$\Rightarrow 2\pi r = 44 \text{ cm}$$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 44 \text{ cm}$$

$$\Rightarrow r = \frac{44 \times 7}{2 \times 22} \text{ cm}$$

$$\Rightarrow r = 7 \text{ cm}$$

$\therefore$  Sum of the area of one semicircle and area of one quadrant of the circle

= Area of one semicircle + Area one quadrant of the circle

$$= \frac{1}{2}\pi r^2 + \frac{1}{4}\pi r^2$$

$$= \pi r^2 \left(\frac{1}{2} + \frac{1}{4}\right)$$

$$= \frac{\pi r^2(2+1)}{4}$$

$$= \frac{3}{4} \times \frac{22}{7} \times 7 \times 7 \text{ cm}^2$$

$$= \frac{231}{2} \text{ cm}^2 = 115\frac{1}{2} \text{ cm}^2.$$

## SECTION-D

**25. Solution:**

Let the numerator be x.

And, the denominator be y.

So, the fraction =  $\frac{x}{y}$

$$\text{Given, } \frac{x-5}{y+3} = \frac{6}{15} = \frac{2}{5}$$

$$\Rightarrow 5(x-5) = 2(y+3)$$

$$\Rightarrow 5x - 25 = 2y + 6$$

$$\Rightarrow 5x - 2y = 31 \quad \dots \dots (i)$$

$$\text{and } 2x + 3y = 58 \quad \dots \dots (ii)$$

$$(ii) \times 2 \rightarrow 4x + 6y = 116$$

$$(i) \times 3 \rightarrow 15x - 6y = 93$$

$$19x = 209$$

$$\Rightarrow x = \frac{209}{19} = 11$$

Putting  $x = 11$ , in (i), we get,

$$5 \times 11 - 2y = 31$$

$$\Rightarrow 55 - 31 = 2y$$

$$\Rightarrow 2y = 24$$

$$\Rightarrow y = \frac{24}{2} = 12.$$

Hence, the fraction is  $\frac{x}{y} = \frac{11}{12}$ .

Reciprocal of the fraction =  $\frac{12}{11}$ .

**Or**

**Solution:**

Let, Cost of 1 shirt be Rs x

Cost of 1 pant be Rs y.

$$\begin{aligned} \text{Given, } 2x + 3y &= 4250 & \dots (i) \\ 3x + 2y &= 3500 & \dots (ii) \end{aligned}$$

$$\begin{array}{rcl} (ii) \times 3 \rightarrow & 9x + 6y = 10500 \\ (i) \times 2 \rightarrow & 4x + 6y = 8500 \\ \hline \text{Subtracting, } - & - & - \\ & 5x & = 2000 \\ & \Rightarrow x & = \frac{2000}{5} = 400 \end{array}$$

Putting  $x = 400$  in (i), we get,

$$2 \times 400 + 3y = 4250$$

$$\Rightarrow 800 + 3y = 4250$$

$$\Rightarrow 3y = 4250 - 800$$

$$\Rightarrow 3y = 3450$$

$$\Rightarrow y = \frac{3450}{3} = 1150$$

$\therefore$  Cost of 1 shirt = Rs 400.

Cost of 1 pant = Rs 1150.

**26. Solution:**

In  $\Delta XYZ$ ,  $XY = XZ = 14\text{cm}$  (Given)

$$\therefore \angle Y = \angle Z \quad \dots \text{(i)}$$

(Angles opposite to equal sides)

Again

$YZ = XZ = 14\text{cm}$  (Given)

$$\therefore \angle X = \angle Y \quad \dots \text{(ii)}$$

(Angles opposite to equal sides)

From (i) and (ii)

$$\angle X = \angle Y = \angle Z$$

And in  $\Delta XYZ$ , we have,

$$\angle X + \angle Y + \angle Z = 180^\circ$$

$$\therefore \angle X = \angle Y = \angle Z = \frac{180^\circ}{3} = 60^\circ.$$

Hence,  $\Delta XYZ$  is an Equilateral Triangle.

$$\begin{aligned} \therefore \text{Area of } \Delta XYZ &= \frac{\sqrt{3}}{4} \text{ side}^2 = \frac{\sqrt{3}}{4} \times 14^2 = \frac{1.732}{4} \times 14 \times 14 \\ &= 84.868 \text{ cm}^2 \end{aligned}$$

Or

**Solution:**

In  $\Delta TBC$ ;

$$\angle TBC = 40^\circ,$$

$$\angle BTC = 90^\circ,$$

$$\angle TCB = x$$

$$\angle TBC + \angle BTC + \angle TCB = 180^\circ$$

(Sum of angles in a triangle =  $180^\circ$ )

$$40^\circ + 90^\circ + x = 180^\circ$$

$$x = 50^\circ$$

**27. Solution:**

Given  $l = 5\text{m}$ ,  $b = 4\text{m}$ ,  $h = 3\text{m}$

$$\begin{aligned}\therefore \text{Surface area of the box} &= 2(lb + bh + lh) \\ &= 2(5.4 + 4.3 + 5.3)\text{m}^2 \\ &= 2(20 + 12 + 15)\text{m}^2 = 94 \text{ m}^2\end{aligned}$$

Cost of wrapping  $1\text{m}^2 = \text{Rs } 2$ .

$$\begin{aligned}\text{Cost of wrapping } 94\text{m}^2 &= \text{Rs } 2 \times 94 \\ &= \text{Rs } 188\end{aligned}$$

**Or**

**Solution:**

Given,

Dimensions of cuboid =  $80\text{m} \times 70\text{m} \times 60\text{m}$

Dimension of cube =  $5\text{m} \times 5\text{m} \times 5\text{m}$

$$\begin{aligned}\therefore \text{No. of cubes} &= \frac{80\text{m} \times 70\text{m} \times 60\text{m}}{5\text{m} \times 5\text{m} \times 5\text{m}} = 16 \times 14 \times 12 \\ &= 2688\end{aligned}$$

Dimension of box =  $4\text{m} \times 3\text{m} \times 2\text{m} = 24\text{m}^2$

$$\therefore \text{No. of boxes} = \frac{2688}{24} = 112$$

**28. Solution:**

Number of hours ( $x_i$ )	Number of people ( $f_i$ )	$f_i x_i$
5	10	50
10	14	140
15	10	150
20	6	120
TOTAL	40	460

$$\begin{aligned}\therefore \text{Mean working hours per person} &= \frac{\sum f_i x_i}{\sum f_i} = \frac{460}{40} \\ &= 11\frac{1}{2} \text{ hours}\end{aligned}$$

**Or**

**Solution:**

Weight (in kg)( $x_i$ )	Number of children ( $f_i$ )	$f_i x_i$
15	4	60
22	5	110
27	7	189
30	8	240
32	6	192
TOTAL	30	791

$$\therefore \text{Mean weight} = \frac{\sum f_i x_i}{\sum f_i} = \frac{791}{30} = 26.367 \text{ kg } (\text{Ans.})$$

$$\begin{aligned}\therefore \text{Median} &= \frac{\frac{n}{2}^{\text{th}} \text{ observation} + \left(\frac{n}{2} + 1\right)^{\text{th}} \text{ observation}}{2} \\ &= \left( \frac{15^{\text{th}} \text{ observation} + 16^{\text{th}} \text{ observation}}{2} \right) \\ &= \frac{27+27}{2} = 27 \quad (\text{Ans.})\end{aligned}$$

$\therefore \text{Mode} = x_i$  with maximum  $f_i$  value = 30. (Ans.)