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- 1. Make correct statements by filling in the symbols \subset or $\not\subset$ in the blank spaces:
- i. $\{2, 3, 4\} \dots \{1, 2, 3, 4, 5\}$
- ii. $\{a, b, c\} \dots \{b, c, d\}$
- iii. {x: x is a student of Class XI of your school} ... {x: x student of your school}
- iv. $\{x: x \text{ is a circle in the plane}\} \dots \{x: x \text{ is a circle in the same plane with radius 1 unit}\}$
- v. $\{x: x \text{ is a triangle in a plane}\}...\{x: x \text{ is a rectangle in the plane}\}$
- vi. $\{x: x \text{ is an equilateral triangle in a plane}\}...\{x: x \text{ is a triangle in the same plane}\}$
- vii. $\{x: x \text{ is an even natural number}\} ... \{x: x \text{ is an integer}\}$

- (i) $\{2,3,4\} \subset \{1,2,3,4,5\}$
- (ii) $\{a,b,c\} \not\subset \{b,c,d\}$
- (iii) $\{x: x \text{ is a student of class XI of your school}\}\subset \{x: x \text{ is student of your school}\}$
- (iv) $\{x: x \text{ is a circle in the plane}\} \not\subset \{x: x \text{ is a circle in the same plane with radius 1}\}$
- (v) $\{x: x \text{ is a triangle in a plane}\} \not\subset \{x: x \text{ is a rectangle in the plane}\}$
- (vi) $\{x: x \text{ is an equilateral triangle in a plane}\} \subset \{x: x \text{ in a triangle in the same plane}\}$
- (vii) $\{x: x \text{ is an even natural number}\} \subset \{x: x \text{ is an integer}\}$
- 2. Examine whether the following statements are true or false:
 - (i) $\{a, b\} \not\subset \{b, c, a\}$
 - (ii) $\{a, e\} \subset \{x: x \text{ is a vowel in the Englishalphabet}\}$
 - (iii) $\{1, 2, 3\} \subset \{1, 3, 5\}$
 - (iv) $\{a\} \subset \{a, b, c\}$
 - $(v) \{a\} \in (a, b, c)$
 - (vi) $\{x: x \text{ is an even natural number less than } 6\} \subset \{x: x \text{ is a natural number which divides}\}$



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Solution:

- (i) False. Each element of $\{a, b\}$ is also an element of $\{b, c, a\}$.
- (ii) True. *a, e* are two vowels of the English alphabet.
- (iii) False. $2 \in \{1, 2, 3\}$; however, $2 \notin \{1, 3, 5\}$
- (iv) True. Each element of {a} is also an element of {a, b, c}.
- (v) False. The elements of $\{a, b, c\}$ are a, b, c. Therefore, $\{a\} \subset \{a, b, c\}$
- (vi) True. $\{x:x \text{ is an even natural number less than } 6\} = \{2, 4\}$ $\{x:x \text{ is a natural number which divides } 36\} = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$

3. Let $A = \{1, 2, \{3, 4,\}, 5\}$. Which of the following statements are incorrect and why?

- (i) $\{3, 4\} \subset A$
- (ii) $\{3, 4\}\}\in A$
- (iii) {{3,4}}⊂ A
- (iv) 1∈ A
- (v) 1⊂ A
- (vi) $\{1, 2, 5\} \subset A$
- (vii) $\{1, 2, 5\} \in A$
- (viii) $\{1, 2, 3\} \subset A$
- (ix) $\Phi \in A$
- $(x) \Phi \subset A$
- (xi) $\{\Phi\} \subset A$

- (i) $A = \{1, 2, \{3, 4\}, 5\}$
- (ii) The statement $\{3, 4\} \subset A$ is incorrect because $3 \in \{3, 4\}$; however, $3 \notin A$.
- (iii) The statement $\{3,4\} \in A$ is correct because $\{3,4\}$ is an element of A.
- (iv) The statement $\{\{3,4\}\}\subset A$ is correct because $\{3,4\}\in \{\{3,4\}\}$ and $\{3,4\}\in A$.
- (v) The statement $1 \in A$ is correct because 1 is an element of A.
- (vi) The statement 1 ⊂ A is incorrect because an element of a set can never be a subset of itself.
- (vii) The statement $\{1,2,5\} \subset A$ is correct because each element of $\{1,2,5\}$ is also an

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element of A.

- (viii) The statement $\{1, 2, 5\} \in A$ is incorrect because $\{1, 2, 5\}$ is not an element of A.
- (ix) The statement $\{1, 2, 3\} \subset A$ is incorrect because $3 \in \{1, 2, 3\}$; however, $3 \notin A$.
- (x) The statement $\Phi \in A$ is incorrect because Φ is not an element of A.
- (xi) The statement $\Phi \subset A$ is correct because Φ is a subset of every set.
- (xii) The statement $\{\Phi\} \subset A$ is incorrect because $\Phi \in \{\Phi\}$; however, $\Phi \in A$.
- 4. Write down all the subsets of the following sets:
- (i) {a}
- (ii) {a, b}
- (iii) {1, 2, 3}
- (iv) Φ

Solution:

- (i) The subsets of $\{a\}$ are Φ and $\{a\}$.
- (ii) The subsets of $\{a, b\}$ are Φ , $\{a\}$, $\{b\}$, and $\{a, b\}$.
- (iii) The subsets of $\{1, 2, 3\}$ are Φ , $\{1\}$, $\{2\}$, $\{3\}$, $\{1, 2\}$, $\{2, 3\}$, $\{1, 3\}$ and $\{1, 2, 3\}$
- (iv) The only subset of Φ is Φ .
- 5. How many elements has P(A), if $A = \Phi$?

Solution:

We know that if A is a set with m elements i.e., n(A) = m, then n[P(A)] = 2m.

If
$$A = \Phi$$
, then $n(A) = 0$.

:
$$n[P(A)] = 20 = 1$$

Hence, P(A) has one element.

- 6. Write the following as intervals:
- (i) $\{x: x \in \mathbb{R}, -4 < x \le 6\}$
- (ii) $\{x: x \in \mathbb{R}, -12 < x < -10\}$
- (iii) $\{x: x \in \mathbb{R}, 0 \le x < 7\}$
- (iv) $\{x: x \in \mathbb{R}, 3 \le x \le 4\}$

(i)
$$\{x: x \in \mathbb{R}, -4 < x \le 6\} = (-4, 6]$$

(ii)
$$\{x: x \in \mathbb{R}, -12 < x < -10\} = (-12, -10)$$

(iii)
$$\{x: x \in \mathbb{R}, 0 \le x < 7\} = [0,7)$$

(iv)
$$\{x: x \in \mathbb{R}, 3 \le x \le 4\} = [3,4]$$

- 7. Write the following intervals in set-builder form:
 - (i) (-3,0)
 - (ii) [6, 12]
 - (iii) (6, 12]
 - (iv) [-23, 5)

Solution:

- (i) $(-3, 0) = \{x: x \in \mathbb{R}, -3 < x < 0\}$
- (ii) $[6, 12] = \{x: x \in \mathbb{R}, 6 \le x \le 12\}$
- (iii) $(6, 12] = \{x: x \in \mathbb{R}, 6 < x \le 12\}$
- (iv) $[-23, 5) = \{x: x \in \mathbb{R}, -23 \le x < 5\}$
- 8. What universal set (s) would you propose for each of the following?
 - (i) The set of right triangles
 - (ii) The set of isosceles triangles

- (i) For the set of right triangles, the universal set can be the set of triangles or the set of polygons.
- (ii) For the set of isosceles triangles, the universal set can be the set of triangles or the set of polygons or the set of two-dimensional figures.
- 9. Given the sets $A = \{1, 3, 5\}$, $B = \{2, 4, 6\}$ and $C = \{0, 2, 4, 6, 8\}$, which of the following may be considered as universals set (s) for all the three sets A,B and C
 - $(i) \ \{0,1,2,3,4,5,6\}$
 - (ii) Ф
 - (iii) {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
 - (iv) {1, 2, 3, 4, 5, 6, 7, 8}



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Solution:

(i) It can be seen that $A \subset \{0, 1, 2, 3, 4, 5, 6\} B \subset \{0, 1, 2, 3, 4, 5, 6\}$ However, $C \not\subset \{0, 1, 2, 3, 4, 5, 6\}$

Therefore, the set {0, 1, 2, 3, 4, 5, 6} cannot be the universal set for the sets A, B, and C.

(ii) $A \not\subset \Phi$, $B \not\subset \Phi$, $C \not\subset \Phi$

Therefore, Φ cannot be the universal set for the sets A, B, and C.

(iii) $A \subset \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $B \subset \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $C \subset \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

Therefore, set {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10} is the universal set for the sets A, B, and C.

(iv) $A \subset \{1, 2, 3, 4, 5, 6, 7, 8\}$ $B \subset \{1, 2, 3, 4, 5, 6, 7, 8\}$ However, $C \not\subset \{1, 2, 3, 4, 5, 6, 7, 8\}$

Therefore, set {1, 2, 3, 4, 5, 6, 7, 8} cannot be the universal set for the sets A, B, and C.