



Given that, the zeroes of the polynomial = 2 and -3,

When  $x = 2$

$$2^2 + (a+1)(2) + b = 0$$

$$4 + 2a + 2 + b = 0$$

$$6 + 2a + b = 0$$

$$2a + b = -6 \text{ ----- (1)}$$

When  $x = -3$ ,

$$(-3)^2 + (a+1)(-3) + b = 0$$

$$9 - 3a - 3 + b = 0$$

$$6 - 3a + b = 0$$

$$-3a + b = -6 \text{ ----- (2)}$$

Subtracting equation (2) from (1)

$$2a + b - (-3a + b) = -6 - (-6)$$

$$2a + b + 3a - b = -6 + 6$$

$$5a = 0$$

$$a = 0$$

Substituting the value of 'a' in equation (1), we get,

$$2a + b = -6$$

$$2(0) + b = -6$$

$$b = -6$$

Hence, **option (D)** is the correct answer.

**4. The number of polynomials having zeroes as -2 and 5 is**

(A) 1

(B) 2

(C) 3

(D) more than 3

**Solution:**

(D) more than 3

Explanation:

According to the question,

The zeroes of the polynomials = -2 and 5

We know that the polynomial is of the form,

$$p(x) = ax^2 + bx + c.$$

Sum of the zeroes = - (coefficient of x) ÷ coefficient of  $x^2$  i.e.

Sum of the zeroes = - b/a

$$- 2 + 5 = - b/a$$

$$3 = - b/a$$

$$b = - 3 \text{ and } a = 1$$

Product of the zeroes = constant term ÷ coefficient of  $x^2$  i.e.

Product of zeroes = c/a

$$(- 2)5 = c/a$$

$$- 10 = c$$

Substituting the values of a, b and c in the polynomial  $p(x) = ax^2 + bx + c$ .

We get,  $x^2 - 3x - 10$

Therefore, we can conclude that x can take any value.

Hence, **option (D)** is the correct answer.

5. Given that one of the zeroes of the cubic polynomial  $ax^3 + bx^2 + cx + d$  is zero, the product of the other two zeroes is

(A)  $(-c/a)$

(B)  $c/a$

(C) 0

(D)  $(-b/a)$

**Solution:**

(B)  $(c/a)$

Explanation:

According to the question,

We have the polynomial,

$$ax^3 + bx^2 + cx + d$$

We know that,

Sum of product of roots of a cubic equation is given by  $c/a$

It is given that one root = 0

Now, let the other roots be  $\alpha, \beta$

So, we get,

$$\alpha\beta + \beta(0) + (0)\alpha = c/a$$

$$\alpha\beta = c/a$$

Hence the product of other two roots is  $c/a$

Hence, **option (B)** is the correct answer

## EXERCISE 2.2

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### 1. Answer the following and justify:

(i) Can  $x^2 - 1$  be the quotient on division of  $x^6 + 2x^3 + x - 1$  by a polynomial in  $x$  of degree 5?

**Solution:**

No,  $x^2 - 1$  cannot be the quotient on division of  $x^6 + 2x^3 + x - 1$  by a polynomial in  $x$  of degree 5.

Justification:

When a degree 6 polynomial is divided by degree 5 polynomial,

The quotient will be of degree 1.

Assume that  $(x^2 - 1)$  divides the degree 6 polynomial with and the quotient obtained is degree 5 polynomial (1)

According to our assumption,

$$(\text{degree 6 polynomial}) = (x^2 - 1)(\text{degree 5 polynomial}) + r(x) \quad [\text{Since, } (a = bq + r)]$$

$$= (\text{degree 7 polynomial}) + r(x) \quad [\text{Since, } (x^2 \text{ term} \times x^5 \text{ term} = x^7 \text{ term})]$$

$$= (\text{degree 7 polynomial})$$

From the above equation, it is clear that, our assumption is contradicted.

$x^2 - 1$  cannot be the quotient on division of  $x^6 + 2x^3 + x - 1$  by a polynomial in  $x$  of degree 5

Hence Proved.

(ii) What will the quotient and remainder be on division of  $ax^2 + bx + c$  by  $px^3 + qx^2 + rx + s, p \neq 0$ ?

**Solution:**

Degree of the polynomial  $px^3 + qx^2 + rx + s$  is 3

Degree of the polynomial  $ax^2 + bx + c$  is 2

Here, degree of  $px^3 + qx^2 + rx + s$  is greater than degree of the  $ax^2 + bx + c$

Therefore, the quotient would be zero,

And the remainder would be the dividend  $= ax^2 + bx + c$ .

(iii) If on division of a polynomial  $p(x)$  by a polynomial  $g(x)$ , the quotient is zero, what is the relation between the degrees of  $p(x)$  and  $g(x)$ ?

**Solution:**

We know that,

$$p(x) = g(x) \times q(x) + r(x)$$

According to the question,

$$q(x) = 0$$

When  $q(x) = 0$ , then  $r(x)$  is also  $= 0$

So, now when we divide  $p(x)$  by  $g(x)$ ,

Then  $p(x)$  should be equal to zero

Hence, the relation between the degrees of  $p(x)$  and  $g(x)$  is the degree  $p(x) < \text{degree } g(x)$

(iv) If on division of a non-zero polynomial  $p(x)$  by a polynomial  $g(x)$ , the remainder is zero, what is the relation between the degrees of  $p(x)$  and  $g(x)$ ?

**Solution:**

In order to divide  $p(x)$  by  $g(x)$

We know that,

Degree of  $p(x) >$  degree of  $g(x)$

or

Degree of  $p(x) =$  degree of  $g(x)$

Therefore, we can say that,

The relation between the degrees of  $p(x)$  and  $g(x)$  is degree of  $p(x) \geq$  degree of  $g(x)$

(v) Can the quadratic polynomial  $x^2 + kx + k$  have equal zeroes for some odd integer  $k > 1$ ?

**Solution:**

A Quadratic Equation will have equal roots if it satisfies the condition:

$$b^2 - 4ac = 0$$

Given equation is  $x^2 + kx + k = 0$

$$a = 1, b = k, c = k$$

Substituting in the equation we get,

$$k^2 - 4(1)(k) = 0$$

$$k^2 - 4k = 0$$

$$k(k - 4) = 0$$

$$k = 0, k = 4$$

But in the question, it is given that  $k$  is greater than 1.

Hence the value of  $k$  is 4 if the equation has common roots.

Hence if the value of  $k = 4$ , then the equation ( $x^2 + kx + k$ ) will have equal roots.

## EXERCISE 2.3

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Find the zeroes of the following polynomials by factorisation method.

1.  $4x^2 - 3x - 1$

**Solution:**

$$4x^2 - 3x - 1$$

Splitting the middle term, we get,

$$4x^2 - 4x + 1x - 1$$

Taking the common factors out, we get,

$$4x(x-1) + 1(x-1)$$

On grouping, we get,

$$(4x+1)(x-1)$$

So, the zeroes are,

$$4x+1=0 \Rightarrow 4x=-1 \Rightarrow x=(-1/4)$$

$$(x-1)=0 \Rightarrow x=1$$

Therefore, zeroes are  $(-1/4)$  and  $1$ Verification:Sum of the zeroes =  $-(\text{coefficient of } x) \div \text{coefficient of } x^2$ 

$$\alpha + \beta = -b/a$$

$$1 - 1/4 = -(-3)/4 = 3/4$$

Product of the zeroes =  $\text{constant term} \div \text{coefficient of } x^2$ 

$$\alpha \beta = c/a$$

$$1(-1/4) = -1/4$$

$$-1/4 = -1/4$$

2.  $3x^2 + 4x - 4$

**Solution:**

$$3x^2 + 4x - 4$$

Splitting the middle term, we get,

$$3x^2 + 6x - 2x - 4$$

Taking the common factors out, we get,

$$3x(x+2) - 2(x+2)$$

On grouping, we get,

$$(x+2)(3x-2)$$

So, the zeroes are,

$$x+2=0 \Rightarrow x=-2$$

$$3x-2=0 \Rightarrow 3x=2 \Rightarrow x=2/3$$

Therefore, zeroes are  $(2/3)$  and  $-2$ Verification:Sum of the zeroes =  $-(\text{coefficient of } x) \div \text{coefficient of } x^2$ 

$$\alpha + \beta = -b/a$$

$$-2 + (2/3) = -(4)/3$$

$$= -4/3 = -4/3$$

Product of the zeroes =  $\text{constant term} \div \text{coefficient of } x^2$

$$\alpha \beta = c/a$$

$$\text{Product of the zeroes} = (-2)(2/3) = -4/3$$

### 3. $5t^2 + 12t + 7$

**Solution:**

$$5t^2 + 12t + 7$$

Splitting the middle term, we get,

$$5t^2 + 5t + 7t + 7$$

Taking the common factors out, we get,

$$5t(t+1) + 7(t+1)$$

On grouping, we get,

$$(t+1)(5t+7)$$

So, the zeroes are,

$$t+1=0 \Rightarrow t = -1$$

$$5t+7=0 \Rightarrow 5t = -7 \Rightarrow t = -7/5$$

Therefore, zeroes are  $(-7/5)$  and  $-1$

Verification:

Sum of the zeroes =  $-(\text{coefficient of } x) \div \text{coefficient of } x^2$

$$\alpha + \beta = -b/a$$

$$(-1) + (-7/5) = -(12)/5$$

$$= -12/5 = -12/5$$

Product of the zeroes =  $\text{constant term} \div \text{coefficient of } x^2$

$$\alpha \beta = c/a$$

$$(-1)(-7/5) = -7/5$$

$$-7/5 = -7/5$$

### 4. $t^3 - 2t^2 - 15t$

**Solution:**

$$t^3 - 2t^2 - 15t$$

Taking  $t$  common, we get,

$$t(t^2 - 2t - 15)$$

Splitting the middle term of the equation  $t^2 - 2t - 15$ , we get,

$$t(t^2 - 5t + 3t - 15)$$

Taking the common factors out, we get,

$$t(t(t-5) + 3(t-5))$$

On grouping, we get,

$$t(t+3)(t-5)$$

So, the zeroes are,

$$t=0$$

$$t+3=0 \Rightarrow t = -3$$

$$t-5=0 \Rightarrow t=5$$

Therefore, zeroes are  $0, 5$  and  $-3$

Verification:

Sum of the zeroes =  $-(\text{coefficient of } x^2) \div \text{coefficient of } x^3$

$$\alpha + \beta + \gamma = -b/a$$

$$(0) + (-3) + (5) = -(-2)/1$$

$$= 2 = 2$$

Sum of the products of two zeroes at a time = coefficient of  $x \div$  coefficient of  $x^3$

$$\alpha\beta + \beta\gamma + \alpha\gamma = c/a$$

$$(0)(-3) + (-3)(5) + (0)(5) = -15/1$$

$$= -15 = -15$$

Product of all the zeroes = - (constant term)  $\div$  coefficient of  $x^3$

$$\alpha\beta\gamma = -d/a$$

$$(0)(-3)(5) = 0$$

$$0 = 0$$

### 5. $2x^2 + (7/2)x + 3/4$

**Solution:**

$$2x^2 + (7/2)x + 3/4$$

The equation can also be written as,

$$8x^2 + 14x + 3$$

Splitting the middle term, we get,

$$8x^2 + 12x + 2x + 3$$

Taking the common factors out, we get,

$$4x(2x+3) + 1(2x+3)$$

On grouping, we get,

$$(4x+1)(2x+3)$$

So, the zeroes are,

$$4x+1=0 \Rightarrow x = -1/4$$

$$2x+3=0 \Rightarrow x = -3/2$$

Therefore, zeroes are  $-1/4$  and  $-3/2$

Verification:

Sum of the zeroes = - (coefficient of  $x$ )  $\div$  coefficient of  $x^2$

$$\alpha + \beta = -b/a$$

$$(-3/2) + (-1/4) = -(7)/4$$

$$= -7/4 = -7/4$$

Product of the zeroes = constant term  $\div$  coefficient of  $x^2$

$$\alpha\beta = c/a$$

$$(-3/2)(-1/4) = (3/4)/2$$

$$3/8 = 3/8$$



## EXERCISE 2.4

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1. For each of the following, find a quadratic polynomial whose sum and product respectively of the zeroes are as given. Also find the zeroes of these polynomials by factorisation.

(i)  $(-8/3), 4/3$

(ii)  $21/8, 5/16$

(iii)  $-2\sqrt{3}, -9$

(iv)  $(-3/(2\sqrt{5})), -1/2$

**Solution:**

(i) Sum of the zeroes =  $-8/3$

Product of the zeroes =  $4/3$

$P(x) = x^2 - (\text{sum of the zeroes}) + (\text{product of the zeroes})$

Then,  $P(x) = x^2 - 8x/3 + 4/3$

$P(x) = 3x^2 - 8x + 4$

Using splitting the middle term method,

$$3x^2 - 8x + 4 = 0$$

$$3x^2 - (6x + 2x) + 4 = 0$$

$$3x^2 - 6x - 2x + 4 = 0$$

$$3x(x - 2) - 2(x - 2) = 0$$

$$(x - 2)(3x - 2) = 0$$

$$\Rightarrow x = 2, 2/3$$

(ii) Sum of the zeroes =  $21/8$

Product of the zeroes =  $5/16$

$P(x) = x^2 - (\text{sum of the zeroes}) + (\text{product of the zeroes})$

Then,  $P(x) = x^2 - 21x/8 + 5/16$

$P(x) = 16x^2 - 42x + 5$

Using splitting the middle term method,

$$16x^2 - 42x + 5 = 0$$

$$16x^2 - (2x + 40x) + 5 = 0$$

$$16x^2 - 2x - 40x + 5 = 0$$

$$2x(8x - 1) - 5(8x - 1) = 0$$

$$(8x - 1)(2x - 5) = 0$$

$$\Rightarrow x = 1/8, 5/2$$

(iii) Sum of the zeroes =  $-2\sqrt{3}$

Product of the zeroes =  $-9$

$P(x) = x^2 - (\text{sum of the zeroes}) + (\text{product of the zeroes})$

Then,  $P(x) = x^2 - 2\sqrt{3}x - 9$

Using splitting the middle term method,

$$x^2 - 2\sqrt{3}x - 9 = 0$$

$$x^2 - (-\sqrt{3}x + 3\sqrt{3}x) - 9 = 0$$

$$x^2 + \sqrt{3}x - 3\sqrt{3}x - 9 = 0$$

$$x(x + \sqrt{3}) - 3\sqrt{3}(x + \sqrt{3}) = 0$$

$$(x + \sqrt{3})(x - 3\sqrt{3}) = 0$$

$$\Rightarrow x = -\sqrt{3}, 3\sqrt{3}$$

(iv) Sum of the zeroes =  $-3/2\sqrt{5}x$

Product of the zeroes =  $-1/2$

$P(x) = x^2 - (\text{sum of the zeroes}) + (\text{product of the zeroes})$

Then,  $P(x) = x^2 - 3/2\sqrt{5}x - 1/2$

$P(x) = 2\sqrt{5}x^2 - 3x - \sqrt{5}$

Using splitting the middle term method,

$$2\sqrt{5}x^2 - 3x - \sqrt{5} = 0$$

$$2\sqrt{5}x^2 - (5x - 2x) - \sqrt{5} = 0$$

$$2\sqrt{5}x^2 - 5x + 2x - \sqrt{5} = 0$$

$$\sqrt{5}x(2x - \sqrt{5}) - (2x - \sqrt{5}) = 0$$

$$(2x - \sqrt{5})(\sqrt{5} - 1) = 0$$

$$\Rightarrow x = -1/\sqrt{5}, \sqrt{5}/2$$

**2. Given that the zeroes of the cubic polynomial  $x^3 - 6x^2 + 3x + 10$  are of the form  $a, a + b, a + 2b$  for some real numbers  $a$  and  $b$ , find the values of  $a$  and  $b$  as well as the zeroes of the given polynomial.**

**Solution:**

Given that  $a, a+b, a+2b$  are roots of given polynomial  $x^3 - 6x^2 + 3x + 10$

Sum of the roots  $\Rightarrow a+2b+a+a+b = -\text{coefficient of } x^2 / \text{coefficient of } x^3$

$$\Rightarrow 3a+3b = -(-6)/1 = 6$$

$$\Rightarrow 3(a+b) = 6$$

$$\Rightarrow a+b = 2 \text{ ----- (1) } b = 2-a$$

Product of roots  $\Rightarrow (a+2b)(a+b)a = -\text{constant/coefficient of } x^3$

$$\Rightarrow (a+b+b)(a+b)a = -10/1$$

Substituting the value of  $a+b=2$  in it

$$\Rightarrow (2+b)(2)a = -10$$

$$\Rightarrow (2+b)2a = -10$$

$$\Rightarrow (2+2-a)2a = -10$$

$$\Rightarrow (4-a)2a = -10$$

$$\Rightarrow 4a - a^2 = -5$$

$$\Rightarrow a^2 - 4a - 5 = 0$$

$$\Rightarrow a^2 - 5a + a - 5 = 0$$

$$\Rightarrow (a-5)(a+1) = 0$$

$$a-5 = 0 \text{ or } a+1 = 0$$

$$a = 5 \text{ or } a = -1$$

$$a = 5, -1 \text{ in (1) } a+b = 2$$

$$\text{When } a = 5, 5+b=2 \Rightarrow b=-3$$

$$a = -1, -1+b=2 \Rightarrow b=3$$

$\therefore$  If  $a=5$  then  $b= -3$

