## CBSE Class 12 Physics Question Paper Solution

## QUESTION PAPER CODE 55/1/1/D

| $\begin{aligned} & \text { Q. } \\ & \text { No. } \end{aligned}$ | Expected Answer/value Points | Marks | Total <br> Marks |
| :---: | :---: | :---: | :---: |
|  | It is defined as the opposition to the flow of current in ac circuits offered by a capacitor. |  |  |
|  | Alternatively: |  |  |
|  | $X_{c}=\frac{1}{\omega C}$ | 1/2 |  |
|  | S.lunit: ohm | 1/2 | 1 |
| 2. | Zero | 1 | 1 |
| 3. | Converging (convex lens), | 1 | 1 |
|  | Side bands are produced due to the superposition of carrier waves of frequency $\omega_{c}$ over modulating / audio signal of frequency $\omega_{m}$. | 1 |  |
|  | Alternatively: |  |  |
|  | (Credit may be given if a student mentions the side bands as $\omega_{\mathrm{c}} \pm \omega_{\mathrm{m}}$ ) |  | 1 |
| 5. | DE: Negative resistance region | 1/2 |  |
|  | AB: Where Ohm's law is obeyed.(Also accept BC) | 1/2 | 1 |
| 6. | Determination of ratio (i) accelerating potential <br> (ii) speed <br> 1 |  |  |
|  | (i) $\lambda=\frac{h}{\sqrt{2 m q V}} \Rightarrow V=\frac{h^{2}}{2 m q \lambda^{2}}$ | 1/2 |  |

$$
\begin{aligned}
& m_{\alpha}=4 m_{p}, q_{\alpha}=2 q_{p} \\
& \Rightarrow \begin{aligned}
\frac{V_{p}}{V_{\alpha}} & =\frac{m_{\alpha} q_{\alpha}}{m_{p} q_{p}} \\
& =\frac{4 m_{p} \times 2 q_{p}}{m_{p} q_{p}} \\
& =8: 1
\end{aligned}
\end{aligned}
$$

(ii) $\lambda=\frac{h}{m v} \Rightarrow v=\frac{h}{m \lambda}$

$$
\Rightarrow \frac{V_{p}}{V_{\alpha}}=\frac{m_{\alpha}}{m_{p}}=4
$$

7. Showing that the radius of orbit varies as $n^{2}$

$$
\frac{m v^{2}}{r}=\frac{1}{4 \pi \epsilon_{0}} \frac{e^{2}}{r^{2}}
$$

Or $m v^{2} r=\frac{1}{4 \pi \epsilon_{0}} e^{2}$
$m v r=\frac{n h}{2 \pi}$
$m^{2} v^{2} r^{2}=\frac{n^{2} h^{2}}{4 \pi^{2}}$

Divide (ii) by (i)
$m r=\frac{n^{2} h^{2}}{4 \pi^{2}} \times \frac{4 \pi \epsilon_{0}}{e^{2}}$
$\therefore r=\frac{n^{2} h^{2}}{4 \pi^{2} m e^{2}} \cdot 4 \pi \epsilon_{0}$
$\therefore r \propto n^{2}$
(Give full credit to any other correct alternative method)
8. Distinction between intrinsic \& extrinsic semiconductors 2

|  | Intrinsic Semiconductor |  | Extrinsic Semiconductor |
| :--- | :--- | :--- | :--- |
| (i) | Without any impurity | (i) | Doped with trivalent// |
|  | atoms. | pentavalent impurity atoms. |  |
| (ii) $\quad n_{e}=n_{h}$ | (ii) $n_{e} \neq n_{h}$ |  |  |

(Any other correct distinguishing features.)
9.

$$
\begin{gathered}
\text { Derivation o } \\
\frac{1}{f}=\frac{1}{v}+\frac{1}{u}
\end{gathered}
$$

For concave mirror $f<0$ and $u<0$
As object lies between $f$ and $2 f$
(i) At $u=-f$

$$
\begin{aligned}
& \frac{1}{v}=-\frac{1}{f}+\frac{1}{f} \\
& \Rightarrow \quad v=\propto
\end{aligned}
$$

At $u=-2 f$

$$
\begin{aligned}
& \Rightarrow \frac{1}{v}=-\frac{1}{f}+\frac{1}{2 f}=-\frac{1}{2 f} \\
& \Rightarrow \quad v=-2 f \\
& \Rightarrow \text { Hence, image distance } v \geq-2 f
\end{aligned}
$$

Since $v$ is negative, therefore, the image is real.

## Alternative Method

$\frac{1}{f}=\frac{1}{v}+\frac{1}{u}$
For concave mirror
$f<0, u<0$
$\therefore 2 f<u<f$
$\Rightarrow \frac{1}{2 f}>\frac{1}{u}>\frac{1}{f}$
$\frac{1}{2 f}-\frac{1}{f}>\frac{1}{u}-\frac{1}{f}>\frac{1}{f}-\frac{1}{f}$
$\Rightarrow \frac{1}{2 f}>\frac{1}{v}>0 \quad \because \frac{1}{u}>\frac{1}{f}>\frac{1}{-v}$
$\Rightarrow \frac{1}{2 f}<\frac{1}{v}<0$
$\Rightarrow v<0 \quad \therefore$ Image is real
Also $v>2 f \quad$ image is formed beyond $2 f$.
(Any alternative correct method should be given full credit.)

## OR

| Finding the expression for intensity | $11 / 2$ |
| :--- | :---: |
| Position of polaroid sheet for maximum intensity | $1 / 2$ |

Let the rotating polaroid sheet makes an angle $\theta$ with the first polaroid $\therefore$ Angle with the other polaroid will be $(90-\theta)$


Applying Malus's law between $\mathrm{P}_{1}$ and $\mathrm{P}_{3}$
$I^{\prime}=I_{0} \cos ^{2} \theta$
Between $\mathrm{P}_{3}$ and $\mathrm{P}_{2}$
$I^{\prime \prime}=\left(I_{0} \cos ^{2} \theta\right) \cos ^{2}(90-\theta)$
$\Rightarrow \quad I^{\prime \prime}=\frac{I_{0}}{4} \cdot \sin ^{2} 2 \theta$
$\therefore$ Transmitted intensity will be maximum when $\theta=\frac{\pi}{4}$
10. Obtaining condition for the balance Wheatstone bridge 2

$-I_{1} R_{1}+0+I_{2} R_{2}=0 \quad\left(I_{\mathrm{g}}=0\right)$
For loop CBDC
Applying Kirchoff's loop rule to closed loop ADBA

$-I_{2} R_{4}+0+I_{1} R_{3}=0$
(ii)
$\Rightarrow$ from equation (i) $\quad \frac{I_{1}}{I_{2}}=\frac{R_{1}}{R_{2}}$
From equation (ii) $\quad \frac{I_{1}}{I_{2}}=\frac{R_{4}}{R_{3}}$
$\therefore \quad \frac{R_{1}}{R_{2}}=\frac{R_{4}}{R_{3}}$
11. Name of the parts of e.m. spectrum for a,b,c $1 / 2+1 / 2+1 / 2$

Production $1 / 2+1 / 2+1 / 2$
(a) Microwave

Production: Klystron/magnetron/Gunn diode (any one)
(b) Infrared Radiation

Production: Hot bodies / vibrations of atoms and molecules (any one)
(c) X-Rays

Production: Bombarding high energy electrons on metal target/ x -ray tube/inner shell electrons (any one).
12.

| (i) | Calculation of angular magnification | $11 / 2$ |
| :--- | :--- | :--- |
| (ii) | Calculation of image of diameter of Moon | $11 / 2$ |

Angular Magnification

$$
\begin{aligned}
m & =\frac{f_{0}}{f_{e}} \\
& =\frac{15}{10^{-2}}=1500
\end{aligned}
$$



Angular size of the moon $=\left(\frac{3.48 \times 10^{6}}{3.8 \times 10^{8}}\right)=\frac{3.48}{3.8} \times 10^{-2}$ radian
$\therefore$ Angular size of the image $=\left(\frac{3.48}{3.8} \times 10^{-2} \times 1500\right)$ radian
Diameter of the image $=\frac{3.48}{3.8} \times 15 \times$ focal length of eye piece

$$
\begin{aligned}
& =\frac{3.48}{3.8} \times 15 \times 1 \mathrm{~cm} \\
& =13.7 \mathrm{~cm}
\end{aligned}
$$

(Also accept alternative correct method.)
13.
(i) Einstein's photoelectric equation 1⁄2
(ii) Important features
(iii) Derivation of expressions for $\lambda_{0}$ and work function
$h \nu=\varphi_{0}+k_{\text {max }}$
or $h v=h v_{0}+\frac{1}{2} m v_{\max }^{2}$

Important features
(i) $\quad k_{\max }$ depends linearly on frequency $v$
(ii) Existence of threshold frequency for the metal surface.
(Any other two correct features.)
$h v=\varphi_{0}+k_{\text {max }}$
$\frac{h c}{\lambda_{1}}=\frac{h c}{\lambda_{0}}+k_{\max }$
$\frac{h c}{\lambda_{2}}=\frac{h c}{\lambda_{0}}+2 k_{\max }$
From (i) and (ii)
$\frac{2 h c}{\lambda_{1}}-\frac{h c}{\lambda_{2}}=\frac{h c}{\lambda_{0}}$
$\frac{1}{\lambda_{0}}=\left(\frac{2}{\lambda_{1}}-\frac{1}{\lambda_{2}}\right)$
$\lambda_{0}=\frac{\lambda_{1} \lambda_{2}}{2 \lambda_{2}-\lambda_{1}}$
Work function $\phi_{0}=\frac{h c}{\lambda_{0}}=\frac{h c\left(2 \lambda_{2}-\lambda_{1}\right)}{\lambda_{1} \lambda_{2}}$
14.
(i) Drawing of trajectory
(ii) Explanation of information on the size of nucleus $1 / 2$
(iii) Proving that nuclear density is independent of A $11 / 2$


Only a small fraction of the incident $\alpha$-particles rebound. This shows that the mass of the atom is concentrated in a small volume in the form of nucleus and gives an idea of the size of the nucleus.

Radius of the nucleus

$$
\begin{aligned}
& R=R_{0} A^{\frac{1}{3}} \\
& \text { Density }=\frac{\text { mass }}{\text { volume }}
\end{aligned}
$$

$$
\begin{gathered}
=\frac{m A}{\frac{4}{3} \pi R^{3}} \quad \text { where, } m: \text { mass of one nucleon } \\
A: \text { Mass number }
\end{gathered}
$$

$$
=\frac{m A}{\frac{4}{3} \pi\left(R_{0} A^{\frac{1}{3}}\right)^{3}}
$$

$$
=\frac{3 m}{4 \pi R_{0}{ }^{3}}
$$

$\Rightarrow$ Nuclear matter density is independent of $A$

## OR

| Distinction between nuclear fission and nuclear fusion | $1 / 2+1 / 2$ |
| :--- | :--- |
| Showing release of energy in both processes | $1 / 2$ |
| Calculation ofrelease of energy | $11 / 2$ |

The breaking of heavy nucleus into smaller fragments is called nuclear fission; the joining of lighter nuclei to form a heavy nucleus is called nuclear fusion.

Binding energy per nucleon, of the daughter nuclei, in both processes, is more than that of the parent nuclei. The difference in binding energy is released in the form of energy. In both processes some mass gets converted into energy.

## Alternatively:

In both processes, some mass gets converted into energy.

Energy Released

$$
\begin{aligned}
& \mathrm{Q}=\left[m\left({ }_{1}^{2} \mathrm{H}\right)+m\left({ }_{1}^{3} \mathrm{H}\right)-m\left({ }_{2}^{4} \mathrm{He}\right)-m(\mathrm{n})\right] \times 931.5 \mathrm{MeV} \\
& =[2.014102+3.016049-4.002603-1.008665] \times 931.5 \mathrm{MeV} \\
& =0.018883 \times 931.5 \mathrm{MeV} \\
& =17.59 \mathrm{MeV}
\end{aligned}
$$

15. 

| Drawing block diagram of detector | 1 |
| :--- | :--- |
| Showing detection of message signal from input AM Wave | 2 |


[Note: Award these 3 marks irrespective of the way the student attempts the question.]
16.

Drawing of Plots of Part (i) \& (ii) $1 / 2+1 / 2$
Finding the values of emf and internal resistance $\quad 1+1$


(If the student just writes the relations $V=\varepsilon-I R$ and $V=\frac{\in R}{R+r}$ but does not draw the plots, award $1 / 2$ mark)
$I=\frac{E}{R+r}$
$I=\frac{E}{4+r}$
$\Rightarrow E=4+r$

Also
$0.5=\frac{E}{9+r}$
$E=4.5+0.5 r$

From equation (i) \& (ii)
$4+r=4.5+0.5 r$
$\therefore r=1 \Omega$

Using this value of $r$, we get
$E=5 \mathrm{~V}$

| Determination of $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ | 2 |
| :--- | ---: |
| Determination of charge on each capacitor in parallel combination | $1 / 2+1 / 2$ |

Energy stored in a capacitor
$E=\frac{1}{2} C V^{2}$

In series combination
$0.045=\frac{1}{2} \frac{c_{1} c_{2}}{c_{1}+c_{2}}(100)^{2}$
$\Rightarrow \frac{c_{1} c_{2}}{c_{1}+c_{2}}=0.09 \times 10^{-4}$

In parallel combination
$0.25=\frac{1}{2}\left(C_{1}+C_{2}\right)(100)^{2}$
$\Rightarrow \quad C_{1}+C_{2}=0.5 \times 10^{-4}$
On simplifying (i) \& (ii)

$$
\begin{align*}
& C_{1} C_{2}=0.045 \times 10^{-8} \\
& \begin{aligned}
\left(C_{1}-C_{2}\right)^{2} & =\left(C_{1}+C_{2}\right)^{2}-4 C_{1} C_{2} \\
& =\left(0.5 \times 10^{-4}\right)^{2}-4 \times 0.045 \times 10^{-8} \\
& =0.25 \times 10^{-8}-0.180 \times 10^{-8} \\
\left(C_{1}-C_{2}\right)^{2} & =0.07 \times 10^{-8} \\
\left(C_{1}-C_{2}\right)^{2} & =2.6 \times 10^{-5}=0.26 \times 10^{-4} \ldots .
\end{aligned}
\end{align*}
$$

From (ii) and (iii) we have
$\Rightarrow \quad C_{1}=0.38 \times 10^{-4} \mathrm{~F}$ and $C_{2}=0.12 \times 10^{-4} \mathrm{~F}$
Charges on capacitor $C_{1}$ and $C_{2}$ in parallel combination
$Q_{1}=C_{1} V=\left(0.38 \times 10^{-4} \times 100\right)=0.38 \times 10^{-2} \mathrm{C}$
$Q_{2}=C_{2} V=\left(0.12 \times 10^{-4} \times 100\right)=0.12 \times 10^{-2} \mathrm{C}$
[Note: If the student writes the relations / equations
$E=\frac{1}{2} C V^{2}$
and $0.045=\frac{1}{2}\left(\frac{c_{1} c_{2}}{c_{1}+c_{2}}\right)(100)^{2}$
$0.25=\frac{1}{2}\left(C_{1}+C_{2}\right)(100)^{2}$
but is unable to calculate $C_{1}$ and $C_{2}$, award him/her full 2 marks.
Also if the student just writes
$Q_{1}=C_{1} V=C_{1}(100)$ and $Q_{2}=C_{2} V=C_{2}(100)$
award him/her one mark for this part of the question.]
18.

| Working principle | 1 |
| :--- | :--- |
| Finding the required resistance | 1 |
| Finding the resistance $G$ of the galvanometer | 1 |

Working principle: A current carrying coil experiences a torque when placed in a magnetic field which tends to rotate the coil and produces an angular deflection.

$$
\begin{aligned}
& V=I\left(G+R_{l}\right) \\
& \frac{V}{2}=I\left(G+R_{2}\right) \\
& \Rightarrow 2=\frac{G+R_{1}}{G+R_{2}} \\
& \Rightarrow G=R_{1}-2 R_{2}
\end{aligned}
$$

Let $R_{3}$ be the resistance required for conversion into voltmeter of range 2 V

$$
\begin{aligned}
& \therefore 2 V=I_{g}\left(G+R_{3}\right) \\
& \text { also } V=I_{g}\left(G+R_{l}\right) \\
& \therefore 2=\frac{G+R_{3}}{G+R_{1}} \\
& \therefore R_{3}=G+2 R_{l}=R_{1}-2 R_{2}+2 R_{1}=3 R_{l}-2 R_{2}
\end{aligned}
$$

19. 

| Fabrication of photodiode | $1 / 2$ |
| :--- | :---: |
| Working with suitable diagram | $1 \frac{1}{2}$ |
| Reason | 1 |

It is fabricated with a transparent window to allow light to fall on diode.
When the photodiode is illuminated with photons of energy ( $h v>E_{g}$ ) greater than the energy gap of the semiconductor, electron - holes pairs are generated. These gets separated due to the junction electric field (before they recombine) which produces an emf.


Reason: It is easier to observe the change in the current, with change in light intensity, if a reverse bias is applied.

## Alternatively,

The fractional change in the minority carrier current, obtained under reverse bias, is much more than the corresponding fractional change in majority carrier current obtained under forward bias.

| Circuit diagram oftransistor amplifier in CE-configuration | $11 / 2$ |
| :--- | :---: |
| Definition and determination of |  |
| (i) input resistance |  |
| (ii) current amplification factor | $11 / 2$ |



Input reisistance
$\mathrm{R}_{\mathrm{i}_{\mathrm{B}}}=\left(\frac{\Delta V_{B E}}{\Delta I_{B}}\right)_{V_{C E}}$
Current amplification factor
$\beta_{\mathrm{ac}}=\left(\frac{\Delta V_{c}}{\Delta I_{B}}\right)_{V_{C B}}$
The value of input resistance is determined from the slope of $I_{B}$ verses $V_{B E}$ plot at constant $V_{C E}$.

The value of current amplification factor is obtained from the slope of collector $I_{C}$ verses $V_{C E}$ plot using different values of $I_{B}$.
(If a student uses typical charateristics to determine these values, full credit of one mark should be given)
21.

| Finding the spacing between two slits | 1 |
| :--- | :--- |
| Effect on wavelength and frequency of reflected and refracted light | 2 |

(a) Angular width of fringes
$\theta=\lambda / d$,
where $d=$ separation between two slits

Here $\theta=0.1^{\circ}=0.1 \times \frac{\pi}{180}$ radian
$\therefore \quad d=\frac{600 \times 10^{-9} \times 180}{0.1 \times \pi} \mathrm{m}$

$$
=3.43 \times 10^{-4} \mathrm{~m}
$$

$$
=0.34 \mathrm{~cm}
$$

(b) For Reflected light:

Wavelength remains same
Frequency remains same

## For Refracted light:

Wavelength decreases
Frequency remains same

| Change in the Brightness of the bulb in cases (i), (ii) \& (iii) $1 / 2+1 / 2+1 / 2$ |
| :--- |
| Justification |
| $1 / 2+1 / 2+1 / 2$ |

(i) Increases
$X_{L}=\omega L$
As number of turns decreases, $L$ decreases, hence current through bulb increases. / voltage across bulb increases.
(ii) Decreases

Iron rod increases the inductance, which increases $X_{L}$, hence current through the bulb decreases / voltage across bulb decreases.
(iii) Increases

Under this condition $\left(X_{C}=X_{L}\right)$ the current through the bulb will become maximum/increase.
23. (i) Name of device and principle of working $1 / 2+1$
(ii) Possibility and explanation $1 / 2$
(iii) Values displayed by students and teachers $1+1$
(i) Transformer

Working principle: Mutual induction
Whenever an alternative voltage is applied in the primary windings, an emf is induced in the secondary windings.
(ii) No, There is no induced emf for a dc voltage in the primary
(iii) Inquisitive nature / Scientific temperament (any one)

Conceren for students / Helpfulness / Professional honesty (any one)
(Any other relevant values)
24.

| (a) | Statement of Ampere's circuital law | 1 |
| :--- | :--- | :--- |
|  | Expression for the magnetic field | $11 / 2$ |
| (b) | Depiction of magnetic field lines and specifying polarity | $1 / 2+1 / 2$ |
|  | Showing the solenoid as bar magnet | $11 / 2$ |

(a) Line integral of magnetic field over a closed loop is equal to the $\mu_{0}$ times the total current passing through the surface enlosed by the loop .

## Alternatively

$$
\oint \vec{B} \cdot \overrightarrow{d l}=\mu_{0} I
$$


(b)

Let the current flowing through each turn of the toroid be $I$. The total number of turns equals $n .(2 \pi r)$ where $n$ is the number of turns per unit length.

Applying Ampere's circuital law, for the Amperian loop, for interior points.

$$
\begin{aligned}
& \oint \vec{B} \cdot \overrightarrow{d l}=\mu_{0}(n 2 \pi r I) \\
& \oint B d l \cos \theta=\mu_{0} n 2 \pi r I \\
& \Rightarrow B \times 2 \pi r=\mu_{0} n 2 \pi r I \\
\therefore \quad & B=\mu_{0} n I
\end{aligned}
$$

(b)


The solenoid contains $N$ loops, each carrying a current $I$. Therefore, each loop acts as a magnetic dipole. The magnetic moment for a current $I$, flowing in loop of area (vector) $\mathbf{A}$ is given by $\mathbf{m}=\mathbf{I A}$

The magnetic moments of all loops are aligned along the same direction. Hence, net magnetic moment equals NIA.

## OR

| (a) | Definition of mutual inductance and S.I. unit | $11 / 2$ |
| :--- | :--- | :--- |
| (b) | Derivation of expression for the mutual inductance |  |
|  | oftwo long coaxial solenoids | $21 / 2$ |

(c) Finding out the expression for the induced emf 1
(a) $\phi=M I$

Mutual inductance of two coils is equal to the magnetic flux linked with one coil when a unit current is passed in the other coil.

## Alternatively,

$$
e=-M \frac{d I}{d t}
$$

Mutual inductance is equal to the induced emf set up in one coil when the rate of change of current flowing through the other coil is unity.

SI unit: henry / (weber ampere ${ }^{-1}$ ) / (volt second ampere ${ }^{-1}$ )
(Any one)
(b)


Let a current $I_{2}$ flow through $\mathrm{S}_{2}$. This sets up a magnetic flux $\phi_{1}$ through each turn of the coil $\mathrm{S}_{1}$.

Total flux linked with $S$
$N_{1} \phi_{1}=M_{12} I_{2}$
where $M_{12}$ is the mutual inductance between the two solenoids
Magnetic field due to the current $I_{2}$ in $\mathrm{S}_{2}$ is $\mu_{0} n_{2} I_{2}$.
Therefore, resulting flux linked with $\mathrm{S}_{1}$.
$N_{l} \phi_{l}=\left[\left(n_{l} l\right) \pi r_{l}^{2}\right]\left(\mu_{0} n_{2} I_{2}\right)$
Comparing (i) \& (ii), we get
$M_{12} \mathrm{I}_{2}=\left(n_{l} l\right) \pi r_{l}^{2}\left(\mu_{0} n_{2} I_{2}\right)$
$\therefore \quad M_{12}=\mu_{0} n_{1} n_{2} \pi r_{l}^{2} l$
(c) Let a magnetic flux be $\left(\phi_{I}\right)$ linked with coil $\mathrm{C}_{1}$ due to current $\left(I_{2}\right){\text { in coil } \mathrm{C}_{2}}$

We have:
$\phi_{1} \propto I_{2}$
$\Rightarrow \phi_{1}=M I_{2}$
$\therefore \frac{d \phi_{1}}{d t}=M \frac{d I_{2}}{d t}$
$\Rightarrow e=-M \frac{d I_{2}}{d t}$

| (a) | Explanation of diffraction pattern using Huygen's construction | 2 |
| :--- | :--- | :--- |
| (b) | Showing the angular width of first diffraction fringe as half of |  |
|  | the central fringe | 2 |
| (c) | Explanation of decrease in intensity with increasing $n$ | 1 |

(a)


We can regard the total contribution of the wavefront LN at some point P on the screen, as the resultant effect of the superposition of its wavelets like $\mathrm{LM}, \mathrm{MM}_{2}, \mathrm{M}_{2} \mathrm{~N}$. These have to be superposed taking into account their proper phase differences.$W e$, therefore, get maxima and minima, i.e. a diffraction pattern, on the screen.
(b)

$\therefore$ Angular width of the central fringe on the screen (from figure)
$=2 \theta=2 \lambda / a$
Angular width of first diffraction fringe (From fig) $=\lambda / a$
Hence angular width of central fringe is twice the angular width of first fringe.

Maxima become weaker and weaker with increasing $n$. This is because the effective part of the wavefront, contributing to the maxima. becomes
smaller and smaller, with increasing $n$.
(a)

(Deduct $1 / 2$ mark for not showing direction of propagation of rays)
For small angles
$\angle \mathrm{NOM} \simeq \tan \angle \mathrm{NOM}=\frac{\mathrm{MN}}{\mathrm{OM}}$
$\angle \mathrm{NCM} \simeq \tan \angle \mathrm{NCM}=\frac{\mathrm{MN}}{\mathrm{MC}}$
$\angle \mathrm{NIM} \simeq \tan \angle \mathrm{NIM}=\frac{\mathrm{MN}}{\mathrm{MI}}$
In $\triangle \mathrm{NOC}, \angle \mathrm{i}=\angle \mathrm{NOM}+\angle \mathrm{NCM}$
$\therefore \angle i=\frac{\mathrm{MN}}{\mathrm{OM}}+\frac{\mathrm{MN}}{\mathrm{MC}}$

Similarly

$$
\begin{align*}
\angle r= & \angle \mathrm{NCM}-\angle \mathrm{NIM} \\
& =\frac{\mathrm{MN}}{\mathrm{MC}}-\frac{\mathrm{MN}}{\mathrm{MI}} \tag{ii}
\end{align*}
$$

Using Snell's Law
$n_{1} \sin i .=n_{2} \sin r$

For small angles
$n_{1} i=n_{2} r$

Substituting for $i$ and $r$, we get
$\frac{n_{1}}{\mathrm{OM}}+\frac{n_{2}}{\mathrm{MI}}=\frac{n_{2}-n_{1}}{\mathrm{MC}}$

Here, $\mathrm{OM}=-u, \mathrm{MI}=+v, \mathrm{MC}=+R$

Substituting these, we get
$\Rightarrow \frac{n_{2}}{v}-\frac{n_{1}}{u}=\frac{n_{2}-n_{1}}{R}$
b)

(Alternatively accept this Ray diagram)


Similarly relation for the surface ADC.
$\frac{-n_{2}}{\mathrm{DI}_{1}}+\frac{n_{1}}{\mathrm{DI}}=\frac{n_{2}-n_{1}}{\mathrm{DC}_{2}}$

Refraction at the first surface $A B C$ of the lens.
$\frac{n_{1}}{\mathrm{IB}}+\frac{n_{2}}{\mathrm{BI}_{1}}=\frac{n_{2}-n_{1}}{\mathrm{BC}_{1}}$
Adding (i)and (ii), and taking $\mathrm{BI}_{1} \cong \mathrm{DI}_{1}$, we get
$\frac{n_{1}}{\mathrm{OB}}+\frac{n_{1}}{\mathrm{DI}}=\left(n_{1}-n_{1}\right)\left(\frac{1}{\mathrm{BC}_{1}}+\frac{1}{\mathrm{DC}_{2}}\right)$
Here, $\mathrm{OB}=-u$

$$
\begin{aligned}
& \mathrm{DI}=+v \\
& \mathrm{BC}_{1}=+R_{1} \\
& \mathrm{DC}_{2}=-R_{2} \\
& \Rightarrow \frac{n_{1}}{-u}+\frac{n_{1}}{v}=\left(n_{2}-n_{1}\right)\left(\frac{1}{R_{1}}+\frac{1}{R_{2}}\right) \\
& \Rightarrow n_{1}\left(\frac{1}{v}+\frac{1}{u}\right)=\left(n_{2}-n_{1}\right)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right) \\
& \Rightarrow \\
& \frac{1}{f}=\left(\frac{n_{2}}{n_{1}}-1\right)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right)
\end{aligned}
$$

26. a) Derivation of the expression for the electric field $E$ and its limiting value
b) Finding the net electric flux
a)


Electric field intensity at point $P$ due to charge $-q$

$$
\overrightarrow{E_{-q}}=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{q}{(x+a)^{2}}(\hat{x})
$$

Due to charge +q

$$
\overrightarrow{E_{+q}}=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{q}{(x-a)^{2}}(\hat{x})
$$

Net electric field at point $P$

$$
\begin{aligned}
& \vec{E}=\overrightarrow{E_{-q}}+\overrightarrow{E_{+q}} \\
& =\frac{q}{4 \pi \varepsilon_{0}} \times\left[\frac{1}{(x-a)^{2}}-\frac{1}{(x+a)^{2}}\right](\hat{x}) \\
& =\frac{q}{4 \pi \varepsilon_{0}} \times\left[\frac{4 a q x}{\left(x^{2}-a^{2}\right)^{2}}\right](\hat{x}) \\
& =\frac{1}{4 \pi \varepsilon_{0}} \frac{(q \times 2 a) 2 x}{\left(x^{2}-a^{2}\right)^{2}}(\hat{x}) \\
& \vec{E}=\frac{1}{4 \pi \varepsilon_{0}} \frac{2 p x}{\left(x^{2}-a^{2}\right)^{2}}(\hat{x})
\end{aligned}
$$



Total flux $\phi=\phi_{I}+\phi_{I I}$

$$
=\oint_{\mathrm{I}} \vec{E} \cdot \overrightarrow{d s}+\oint_{\mathrm{II}} \vec{E} \cdot \overrightarrow{d s}
$$

$$
\begin{aligned}
& =0+2(a) \cdot a^{2} \\
\therefore \quad & \phi=2 a^{3}
\end{aligned}
$$

## OR

a) Explanation of difference in behaviour of
(i) conductor (ii) dielectric

Definition of polarization and its relation with susceptibility
b) (i) Finding the force on the charge at centre and the charge at point A
(ii) Finding Electric flux through the shell

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In the presence of electric field, the free charge carriers, in a conductor, move the charge distribution in the conductor readjusts itself so that the net electric field within the conductor becomes zero.

In a dielectric, the external electric field induces a net dipole moment, by stretching / reorienting the molecules. The electric field, due to this induced dipole moment, opposes ,but does not exactly cancel, the external electric field.

Polarisation: Induced dipole moment, per unit volume, is called the polarization. For linear isotropic dielectrics having a susceptibility $X_{c}$, we have
$P=X_{e} E$
(b) (i) Net Force on the charge $\frac{Q}{2}$, placed at the centre of the shell, is zero.

Force on charge ' $2 Q$ ' kept at point A
$F=E \times 2 Q=\frac{1\left(\frac{3 Q}{2}\right) 2 Q}{4 \pi \varepsilon_{0} r^{2}}=\frac{(K) 3 Q^{2}}{r^{2}}$
Electric flux through the shell
$\phi=\frac{Q}{\varepsilon_{0}}$

