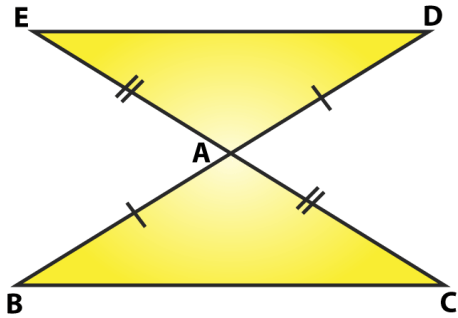


Exercise 10.1

Page No: 10.12

**Question 1:** In figure, the sides BA and CA have been produced such that BA = AD and CA = AE. Prove that segment DE || BC.



**Solution:**

Sides BA and CA have been produced such that BA = AD and CA = AE.

To prove: DE || BC

Consider  $\triangle BAC$  and  $\triangle DAE$ ,

BA = AD and CA = AE (Given)

$\angle BAC = \angle DAE$  (vertically opposite angles)

By SAS congruence criterion, we have

$\triangle BAC \cong \triangle DAE$

We know, corresponding parts of congruent triangles are equal

So, BC = DE and  $\angle DEA = \angle BCA$ ,  $\angle EDA = \angle CBA$

Now, DE and BC are two lines intersected by a transversal DB s.t.

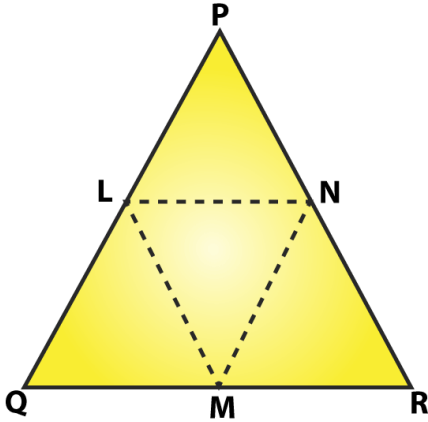
$\angle DEA = \angle BCA$  (alternate angles are equal)

Therefore, DE || BC. Proved.

**Question 2:** In a  $\triangle PQR$ , if  $PQ = QR$  and  $L, M$  and  $N$  are the mid-points of the sides  $PQ, QR$  and  $RP$  respectively. Prove that  $LN = MN$ .

**Solution:**

Draw a figure based on given instruction,



In  $\triangle PQR$ ,  $PQ = QR$  and  $L, M, N$  are midpoints of the sides  $PQ, QR$  and  $RP$  respectively (Given)

To prove :  $LN = MN$

As two sides of the triangle are equal, so  $\triangle PQR$  is an isosceles triangle

$PQ = QR$  and  $\angle QPR = \angle QRP$  ..... (i)

Also,  $L$  and  $M$  are midpoints of  $PQ$  and  $QR$  respectively

$PL = LQ = QM = MR = QR/2$

Now, consider  $\triangle LPN$  and  $\triangle MRN$ ,

$LP = MR$

$\angle LPN = \angle MRN$  [From (i)]

$\angle QPR = \angle LPN$  and  $\angle QRP = \angle MRN$

$PN = NR$  [N is midpoint of PR]

By SAS congruence criterion,

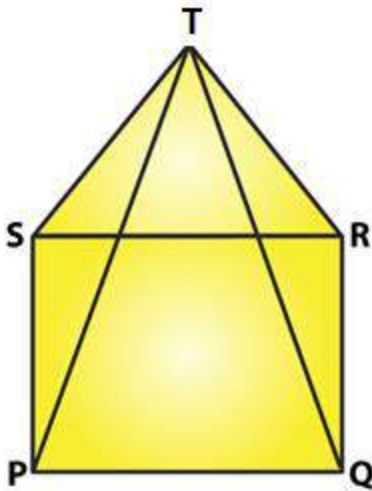
$\triangle LPN \cong \triangle MRN$

We know, corresponding parts of congruent triangles are equal.

So  $LN = MN$

Proved.

**Question 3: In figure, PQRS is a square and SRT is an equilateral triangle. Prove that  
(i)  $PT = QT$     (ii)  $\angle TQR = 15^\circ$**



**Solution:**

Given: PQRS is a square and SRT is an equilateral triangle.

To prove:

(i)  $PT = QT$  and (ii)  $\angle TQR = 15^\circ$

Now,

**PQRS is a square:**

$$PQ = QR = RS = SP \quad \dots\dots (i)$$

$$\text{And } \angle SPQ = \angle PQR = \angle QRS = \angle RSP = 90^\circ$$

**Also,  $\triangle SRT$  is an equilateral triangle:**

$$SR = RT = TS \quad \dots\dots(ii)$$

$$\text{And } \angle TSR = \angle SRT = \angle RTS = 60^\circ$$

From (i) and (ii)

$$PQ = QR = SP = SR = RT = TS \quad \dots\dots(iii)$$

From figure,

$$\angle TSP = \angle TSR + \angle RSP = 60^\circ + 90^\circ = 150^\circ \quad \text{and}$$

$$\angle TRQ = \angle TRS + \angle SRQ = 60^\circ + 90^\circ = 150^\circ$$

$$\Rightarrow \angle TSR = \angle TRQ = 150^\circ \quad \dots\dots\dots (iv)$$

By SAS congruence criterion,  $\Delta TSP \cong \Delta TRQ$

We know, corresponding parts of congruent triangles are equal  
So,  $PT = QT$

Proved part (i).

Now, consider  $\Delta TQR$ .

$$QR = TR \quad [\text{From (iii)}]$$

$\Delta TQR$  is an isosceles triangle.

$$\angle QTR = \angle TQR \quad [\text{angles opposite to equal sides}]$$

Sum of angles in a triangle =  $180^\circ$

$$\Rightarrow \angle QTR + \angle TQR + \angle TRQ = 180^\circ$$

$$\Rightarrow 2 \angle TQR + 150^\circ = 180^\circ \quad [\text{From (iv)}]$$

$$\Rightarrow 2 \angle TQR = 30^\circ$$

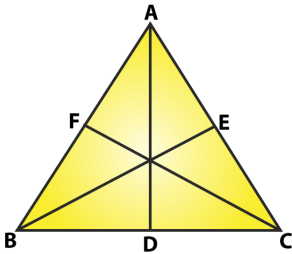
$$\Rightarrow \angle TQR = 15^\circ$$

Hence proved part (ii).

**Question 4: Prove that the medians of an equilateral triangle are equal.**

**Solution:**

Consider an equilateral  $\triangle ABC$ , and Let D, E, F are midpoints of BC, CA and AB.



Here, AD, BE and CF are medians of  $\triangle ABC$ .

Now,

D is midpoint of BC  $\Rightarrow$   $BD = DC$

Similarly,  $CE = EA$  and  $AF = FB$

Since  $\triangle ABC$  is an equilateral triangle

$AB = BC = CA$  .....(i)

$BD = DC = CE = EA = AF = FB$  .....(ii)

And also,  $\angle ABC = \angle BCA = \angle CAB = 60^\circ$  .....(iii)

Consider  $\triangle ABD$  and  $\triangle BCE$

$AB = BC$  [From (i)]

$BD = CE$  [From (ii)]

$\angle ABD = \angle BCE$  [From (iii)]

By SAS congruence criterion,

$\triangle ABD \cong \triangle BCE$

$\Rightarrow AD = BE$  .....(iv)

[Corresponding parts of congruent triangles are equal in measure]

Now, consider  $\Delta BCE$  and  $\Delta CAF$ ,

$$BC = CA \quad \text{[From (i)]}$$

$$\angle BCE = \angle CAF \quad \text{[From (ii)]}$$

$$CE = AF \quad \text{[From (ii)]}$$

By SAS congruence criterion,

$$\Delta BCE \cong \Delta CAF$$

$$\Rightarrow BE = CF \quad \dots\dots\dots(v)$$

[Corresponding parts of congruent triangles are equal]

From (iv) and (v), we have

$$AD = BE = CF$$

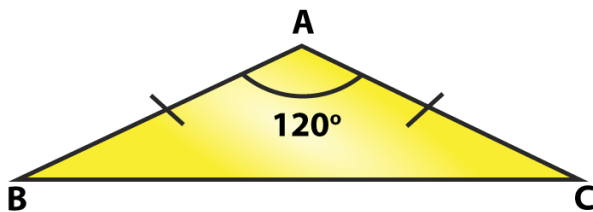
$$\text{Median } AD = \text{Median } BE = \text{Median } CF$$

The medians of an equilateral triangle are equal.

Hence proved

**Question 5:** In a  $\Delta ABC$ , if  $\angle A = 120^\circ$  and  $AB = AC$ . Find  $\angle B$  and  $\angle C$ .

**Solution:**



To find:  $\angle B$  and  $\angle C$ .

Here,  $\Delta ABC$  is an isosceles triangle since  $AB = AC$

$$\angle B = \angle C \quad \dots\dots\dots (i)$$

[Angles opposite to equal sides are equal]

We know, sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle B + \angle B = 180^\circ \text{ (using (i))}$$

$$120^\circ + 2\angle B = 180^\circ$$

$$2\angle B = 180^\circ - 120^\circ = 60^\circ$$

$$\angle B = 30^\circ$$

$$\text{Therefore, } \angle B = \angle C = 30^\circ$$

**Question 6:** In a  $\Delta ABC$ , if  $AB = AC$  and  $\angle B = 70^\circ$ , find  $\angle A$ .

**Solution:**

Given: In a  $\Delta ABC$ ,  $AB = AC$  and  $\angle B = 70^\circ$

$\angle B = \angle C$  [Angles opposite to equal sides are equal]

Therefore,  $\angle B = \angle C = 70^\circ$

Sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 70^\circ + 70^\circ = 180^\circ$$

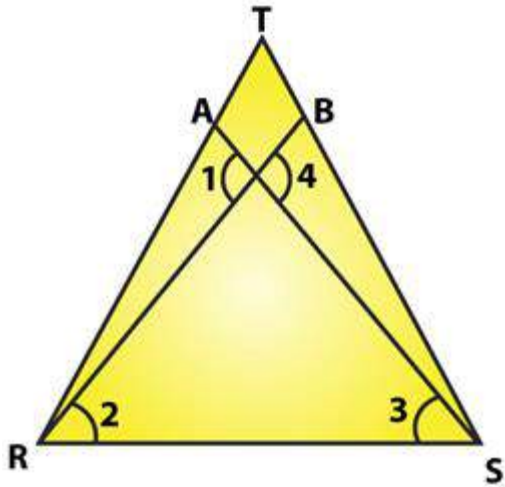
$$\angle A = 180^\circ - 140^\circ$$

$$\angle A = 40^\circ$$

Exercise 10.2

Page No: 10.21

**Question 1:** In figure, it is given that  $RT = TS$ ,  $\angle 1 = 2 \angle 2$  and  $\angle 4 = 2(\angle 3)$ . Prove that  $\Delta RBT \cong \Delta SAT$ .



**Solution:**

In the figure,

$$RT = TS \quad \dots(i)$$

$$\angle 1 = 2 \angle 2 \quad \dots(ii)$$

$$\text{And } \angle 4 = 2 \angle 3 \quad \dots(iii)$$

To prove:  $\Delta RBT \cong \Delta SAT$

Let the point of intersection RB and SA be denoted by O

$$\angle AOR = \angle BOS \quad [\text{Vertically opposite angles}]$$

$$\text{or } \angle 1 = \angle 4$$

$$2 \angle 2 = 2 \angle 3 \quad [\text{From (ii) and (iii)}]$$

$$\text{or } \angle 2 = \angle 3 \quad \dots(iv)$$

Now in  $\Delta TRS$ , we have  $RT = TS$



$\Rightarrow \Delta TRS$  is an isosceles triangle

$$\angle TRS = \angle TSR \quad \dots\dots(v)$$

But,  $\angle TRS = \angle TRB + \angle 2 \quad \dots\dots(vi)$

$$\angle TSR = \angle TSA + \angle 3 \quad \dots\dots(vii)$$

Putting (vi) and (vii) in (v) we get

$$\angle TRB + \angle 2 = \angle TSA + \angle 3$$

$$\Rightarrow \angle TRB = \angle TSA \quad [\text{From (iv)}]$$

Consider  $\Delta RBT$  and  $\Delta SAT$

$$RT = ST \quad [\text{From (i)}]$$

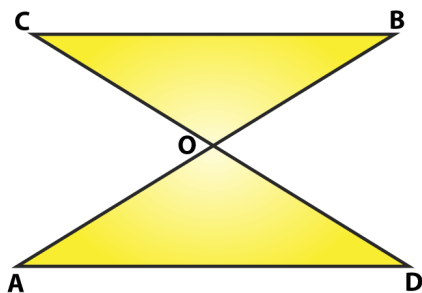
$$\angle TRB = \angle TSA \quad [\text{From (iv)}]$$

By ASA criterion of congruence, we have

$$\Delta RBT \cong \Delta SAT$$

**Question 2: Two lines AB and CD intersect at O such that BC is equal and parallel to AD. Prove that the lines AB and CD bisect at O.**

**Solution:** Lines AB and CD Intersect at O



Such that  $BC \parallel AD$  and

$$BC = AD \quad \dots\dots(i)$$

To prove : AB and CD bisect at O.

First we have to prove that  $\Delta AOD \cong \Delta BOC$

$$\angle OCB = \angle ODA \quad [AD \parallel BC \text{ and } CD \text{ is transversal}]$$

$$AD = BC \quad [\text{from (i)}]$$

$$\angle OBC = \angle OAD \quad [AD \parallel BC \text{ and } AB \text{ is transversal}]$$

By ASA Criterion:

$$\Delta AOD \cong \Delta BOC$$

$$OA = OB \text{ and } OD = OC \text{ (By c.p.c.t.)}$$

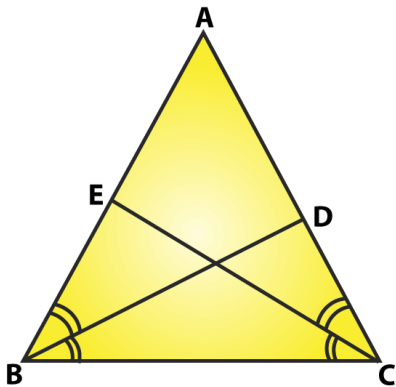
Therefore, AB and CD bisect each other at O.

Hence Proved.

**Question 3:** BD and CE are bisectors of  $\angle B$  and  $\angle C$  of an isosceles  $\Delta ABC$  with  $AB = AC$ . Prove that  $BD = CE$ .

**Solution:**

$\Delta ABC$  is isosceles with  $AB = AC$  and BD and CE are bisectors of  $\angle B$  and  $\angle C$  We have to prove  $BD = CE$ .  
(Given)



Since  $AB = AC$

$$\Rightarrow \angle ABC = \angle ACB \quad \dots(i)$$

[Angles opposite to equal sides are equal]

Since BD and CE are bisectors of  $\angle B$  and  $\angle C$

$$\angle ABD = \angle DBC = \angle BCE = \angle ECA = \angle B/2 = \angle C/2 \quad \dots(ii)$$

Now, Consider  $\Delta EBC = \Delta DCB$

$\angle EBC = \angle DCB$  [From (i)]

$BC = BC$  [Common side]

$\angle BCE = \angle CBD$  [From (ii)]

By ASA congruence criterion,  $\Delta EBC \cong \Delta DCB$

Since corresponding parts of congruent triangles are equal.

$\Rightarrow CE = BD$

or,  $BD = CE$

Hence proved.

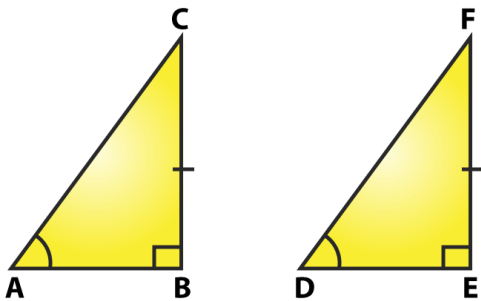


Exercise 10.3

**Question 1:** In two right triangles one side and acute angle of one are equal to the corresponding side and angle of the other. Prove that the triangles are congruent.

**Solution:**

In two right triangles one side and acute angle of one are equal to the corresponding side and angles of the other. (Given)



To prove: Both the triangles are congruent.

Consider two right triangles such that

$$\angle B = \angle E = 90^\circ \quad \dots\dots(i)$$

$$AB = DE \quad \dots\dots(ii)$$

$$\angle C = \angle F \quad \dots\dots(iii)$$

Here we have two right triangles,  $\triangle ABC$  and  $\triangle DEF$

From (i), (ii) and (iii),

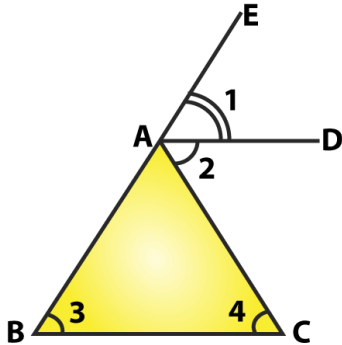
By AAS congruence criterion, we have  $\triangle ABC \cong \triangle DEF$

Both the triangles are congruent. Hence proved.

**Question 2:** If the bisector of the exterior vertical angle of a triangle be parallel to the base. Show that the triangle is isosceles.

**Solution:**

Let ABC be a triangle such that AD is the angular bisector of exterior vertical angle,  $\angle EAC$  and  $AD \parallel BC$ .



From figure,

$$\angle 1 = \angle 2 \quad [\text{AD is a bisector of } \angle \text{EAC}]$$

$$\angle 1 = \angle 3 \quad [\text{Corresponding angles}]$$

$$\text{and } \angle 2 = \angle 4 \quad [\text{alternative angle}]$$

From above, we have  $\angle 3 = \angle 4$

This implies,  $AB = AC$

Two sides AB and AC are equal.

$\Rightarrow \Delta ABC$  is an isosceles triangle.

**Question 3: In an isosceles triangle, if the vertex angle is twice the sum of the base angles, calculate the angles of the triangle.**

**Solution:**

Let  $\Delta ABC$  be isosceles where  $AB = AC$  and  $\angle B = \angle C$

Given: Vertex angle A is twice the sum of the base angles B and C. i.e.,  $\angle A = 2(\angle B + \angle C)$

$$\angle A = 2(\angle B + \angle B)$$

$$\angle A = 2(2 \angle B)$$

$$\angle A = 4(\angle B)$$

Now, We know that sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$4 \angle B + \angle B + \angle B = 180^\circ$$

$$6 \angle B = 180^\circ$$

$$\angle B = 30^\circ$$

Since,  $\angle B = \angle C$

$$\angle B = \angle C = 30^\circ$$

And  $\angle A = 4 \angle B$

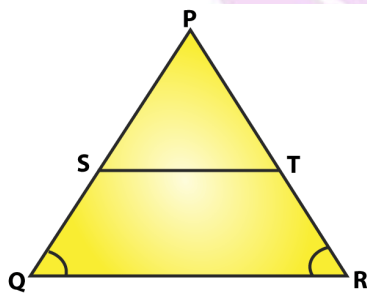
$$\angle A = 4 \times 30^\circ = 120^\circ$$

Therefore, angles of the given triangle are  $30^\circ$  and  $30^\circ$  and  $120^\circ$ .

**Question 4:** PQR is a triangle in which  $PQ = PR$  and S is any point on the side PQ. Through S, a line is drawn parallel to QR and intersecting PR at T. Prove that  $PS = PT$ .

**Solution:** Given that PQR is a triangle such that  $PQ = PR$  and S is any point on the side PQ and  $ST \parallel QR$ .

To prove:  $PS = PT$



Since,  $PQ = PR$ , so  $\triangle PQR$  is an isosceles triangle.

$$\angle PQR = \angle PRQ$$

Now,  $\angle PST = \angle PQR$  and  $\angle PTS = \angle PRQ$   
[Corresponding angles as  $ST$  parallel to  $QR$ ]

Since,  $\angle PQR = \angle PRQ$

$\angle PST = \angle PTS$

In  $\Delta PST$ ,  
 $\angle PST = \angle PTS$

$\Delta PST$  is an isosceles triangle.

Therefore,  $PS = PT$ .

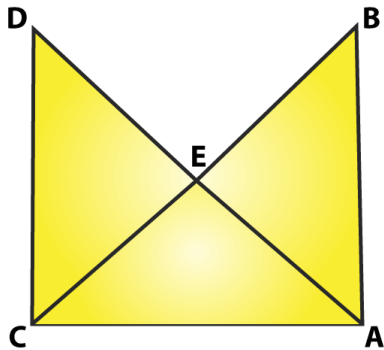
Hence proved.



Exercise 10.4

Page No: 10.47

**Question 1:** In figure, It is given that  $AB = CD$  and  $AD = BC$ . Prove that  $\triangle ADC \cong \triangle CBA$ .



**Solution:**

From figure,  $AB = CD$  and  $AD = BC$ .

To prove:  $\triangle ADC \cong \triangle CBA$

Consider  $\triangle ADC$  and  $\triangle CBA$ .

$AB = CD$  [Given]

$BC = AD$  [Given]

And  $AC = AC$  [Common side]

So, by SSS congruence criterion, we have

$\triangle ADC \cong \triangle CBA$

Hence proved.

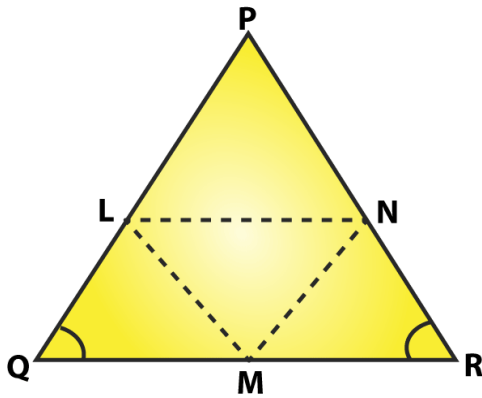
**Question 2:** In a  $\triangle PQR$ , if  $PQ = QR$  and  $L, M$  and  $N$  are the mid-points of the sides  $PQ, QR$  and  $RP$  respectively. Prove that  $LN = MN$ .

**Solution:**

Given: In  $\triangle PQR$ ,  $PQ = QR$  and  $L, M$  and  $N$  are the mid-points of the sides  $PQ, QR$  and  $RP$  respectively

To prove:  $LN = MN$





Join L and M, M and N, N and L

We have  $PL = LQ$ ,  $QM = MR$  and  $RN = NP$

[Since, L, M and N are mid-points of PQ, QR and RP respectively]

And also  $PQ = QR$

$PL = LQ = QM = MR = PN = NR$  .....(i)  
[ Using mid-point theorem]

$MN \parallel PQ$  and  $MN = PQ/2$

$MN = PL = LQ$  .....(ii)

Similarly, we have

$LN \parallel QR$  and  $LN = (1/2)QR$

$LN = QM = MR$  .....(iii)

From equation (i), (ii) and (iii), we have

$PL = LQ = QM = MR = MN = LN$

This implies,  $LN = MN$

Hence Proved.

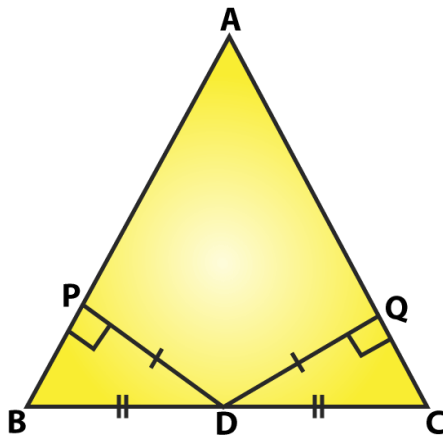
Exercise 10.5

**Question 1:** ABC is a triangle and D is the mid-point of BC. The perpendiculars from D to AB and AC are equal. Prove that the triangle is isosceles.

**Solution:**

Given: D is the midpoint of BC and  $PD = DQ$  in a triangle ABC.

To prove: ABC is isosceles triangle.



In  $\triangle BDP$  and  $\triangle CDQ$   
 $PD = QD$  (Given)  
 $BD = DC$  (D is mid-point)  
 $\angle BPD = \angle CQD = 90^\circ$

By RHS Criterion:  $\triangle BDP \cong \triangle CDQ$

$BP = CQ$  ... (i) (By CPCT)

In  $\triangle APD$  and  $\triangle AQD$

$PD = QD$  (given)  
 $AD = AD$  (common)  
 $\angle APD = \angle AQD = 90^\circ$

By RHS Criterion:  $\triangle APD \cong \triangle AQD$   
 So,  $PA = QA$  ... (ii) (By CPCT)

Adding (i) and (ii)

$$BP + PA = CQ + QA$$

$$AB = AC$$

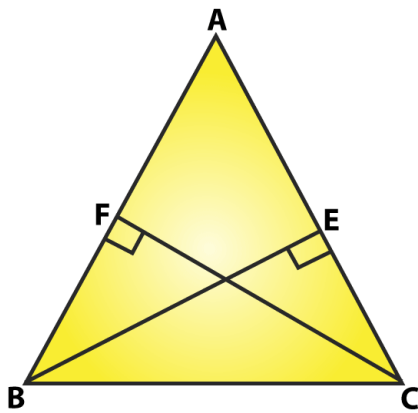
Two sides of the triangle are equal, so ABC is an isosceles.

**Question 2:** ABC is a triangle in which BE and CF are, respectively, the perpendiculars to the sides AC and AB. If  $BE = CF$ , prove that  $\Delta ABC$  is isosceles

**Solution:**

ABC is a triangle in which BE and CF are perpendicular to the sides AC and AS respectively s.t.  $BE = CF$ .

To prove:  $\Delta ABC$  is isosceles



In  $\Delta BCF$  and  $\Delta CBE$ ,  
 $\angle BFC = \angle CEB = 90^\circ$  [Given]

$BC = CB$  [Common side]

And  $CF = BE$  [Given]

By RHS congruence criterion:  $\Delta BFC \cong \Delta CEB$

So,  $\angle FBC = \angle ECB$  [By CPCT]

$\Rightarrow \angle ABC = \angle ACB$

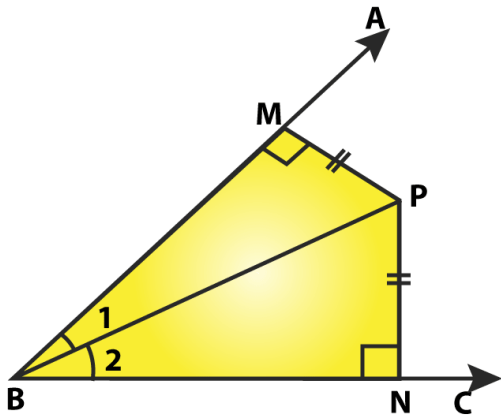
$AC = AB$  [Opposite sides to equal angles are equal in a triangle]

Two sides of triangle ABC are equal.

Therefore,  $\Delta ABC$  is isosceles. Hence Proved.

**Question 3:** If perpendiculars from any point within an angle on its arms are congruent. Prove that it lies on the bisector of that angle.

**Solution:**



Consider an angle ABC and BP be one of the arm within the angle.

Draw perpendiculars PN and PM on the arms BC and BA.

In  $\triangle BPM$  and  $\triangle BPN$ ,

$$\angle BMP = \angle BNP = 90^\circ \text{ [given]}$$

$$BP = BP \quad \text{[Common side]}$$

$$MP = NP \quad \text{[given]}$$

By RHS congruence criterion:  $\triangle BPM \cong \triangle BPN$

So,  $\angle MBP = \angle NBP$  [ By CPCT ]

BP is the angular bisector of  $\angle ABC$ .

Hence proved

## Exercise 10.6

Page No: 10.66

**Question 1:** In  $\Delta ABC$ , if  $\angle A = 40^\circ$  and  $\angle B = 60^\circ$ . Determine the longest and shortest sides of the triangle.

**Solution:** In  $\Delta ABC$ ,  $\angle A = 40^\circ$  and  $\angle B = 60^\circ$   
We know, sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$40^\circ + 60^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 100^\circ = 80^\circ$$

$$\angle C = 80^\circ$$

Now,  $40^\circ < 60^\circ < 80^\circ$   
 $\Rightarrow \angle A < \angle B < \angle C$

$\Rightarrow \angle C$  is greater angle and  $\angle A$  is smaller angle.

Now,  $\angle A < \angle B < \angle C$

We know, side opposite to greater angle is larger and side opposite to smaller angle is smaller.

Therefore,  $BC < AC < AB$

AB is longest and BC is shortest side.

**Question 2:** In a  $\Delta ABC$ , if  $\angle B = \angle C = 45^\circ$ , which is the longest side?

**Solution:** In  $\Delta ABC$ ,  $\angle B = \angle C = 45^\circ$

Sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 45^\circ + 45^\circ = 180^\circ$$

$$\angle A = 180^\circ - (45^\circ + 45^\circ) = 180^\circ - 90^\circ = 90^\circ$$

$$\angle A = 90^\circ$$

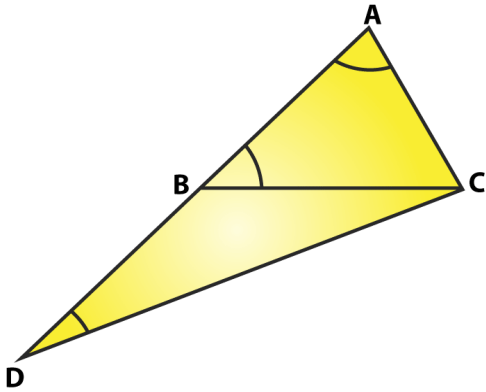
$$\Rightarrow \angle B = \angle C < \angle A$$

Therefore, BC is the longest side.

**Question 3:** In  $\Delta ABC$ , side  $AB$  is produced to  $D$  so that  $BD = BC$ . If  $\angle B = 60^\circ$  and  $\angle A = 70^\circ$ .  
Prove that: (i)  $AD > CD$  (ii)  $AD > AC$

**Solution:** In  $\Delta ABC$ , side  $AB$  is produced to  $D$  so that  $BD = BC$ .

$\angle B = 60^\circ$ , and  $\angle A = 70^\circ$



To prove: (i)  $AD > CD$  (ii)  $AD > AC$

Construction: Join  $C$  and  $D$

We know, sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$70^\circ + 60^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - (130^\circ) = 50^\circ$$

$$\angle C = 50^\circ$$

$$\angle ACB = 50^\circ \quad \dots\dots(i)$$

And also in  $\Delta BDC$

$$\angle DBC = 180^\circ - \angle ABC = 180 - 60^\circ = 120^\circ$$

[ $\angle DBA$  is a straight line]

and  $BD = BC$  [given]

$\angle BCD = \angle BDC$  [Angles opposite to equal sides are equal]

Sum of angles in a triangle =  $180^\circ$

$\angle DBC + \angle BCD + \angle BDC = 180^\circ$

$120^\circ + \angle BCD + \angle BCD = 180^\circ$

$120^\circ + 2\angle BCD = 180^\circ$

$2\angle BCD = 180^\circ - 120^\circ = 60^\circ$

$\angle BCD = 30^\circ$

$\angle BCD = \angle BDC = 30^\circ$  ....(ii)

Now, consider  $\Delta ADC$ .

$\angle DAC = 70^\circ$  [given]

$\angle ADC = 30^\circ$  [From (ii)]

$\angle ACD = \angle ACB + \angle BCD = 50^\circ + 30^\circ = 80^\circ$  [From (i) and (ii)]

Now,  $\angle ADC < \angle DAC < \angle ACD$

$AC < DC < AD$

[Side opposite to greater angle is longer and smaller angle is smaller]

$AD > CD$  and  $AD > AC$

Hence proved.

**Question 4: Is it possible to draw a triangle with sides of length 2 cm, 3 cm and 7 cm?**

**Solution:**

Lengths of sides are 2 cm, 3 cm and 7 cm.

A triangle can be drawn only when the sum of any two sides is greater than the third side.

So, let's check the rule.

$$2 + 3 \neq 7 \text{ or } 2 + 3 < 7$$

$$2 + 7 > 3$$

$$\text{and } 3 + 7 > 2$$

$$\text{Here } 2 + 3 \neq 7$$

So, the triangle does not exist.





Exercise VSAQs

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**Question 1:** In two congruent triangles ABC and DEF, if  $AB = DE$  and  $BC = EF$ . Name the pairs of equal angles.

**Solution:**

In two congruent triangles ABC and DEF, if  $AB = DE$  and  $BC = EF$ , then

$$\angle A = \angle D, \angle B = \angle E \text{ and } \angle C = \angle F$$

**Question 2:** In two triangles ABC and DEF, it is given that  $\angle A = \angle D$ ,  $\angle B = \angle E$  and  $\angle C = \angle F$ . Are the two triangles necessarily congruent?

**Solution:** No.

Reason: Two triangles are not necessarily congruent, because we know only angle-angle-angle (AAA) criterion. This criterion can produce similar but not congruent triangles.

**Question 3:** If ABC and DEF are two triangles such that  $AC = 2.5$  cm,  $BC = 5$  cm,  $C = 75^\circ$ ,  $DE = 2.5$  cm,  $DF = 5$  cm and  $D = 75^\circ$ . Are two triangles congruent?

**Solution:** Yes.

Reason: Given triangles are congruent as  $AC = DE = 2.5$  cm,  $BC = DF = 5$  cm and  $\angle C = \angle D = 75^\circ$ .

By SAS theorem triangle ABC is congruent to triangle EDF.

**Question 4:** In two triangles ABC and ADC, if  $AB = AD$  and  $BC = CD$ . Are they congruent?

**Solution:** Yes.

Reason: Given triangles are congruent as

$$AB = AD$$

$$BC = CD \text{ and}$$

$$AC \text{ [ common side]}$$

By SSS theorem triangle ABC is congruent to triangle ADC.

**Question 5:** In triangles ABC and CDE, if  $AC = CE$ ,  $BC = CD$ ,  $\angle A = 60^\circ$ ,  $\angle C = 30^\circ$  and  $\angle D = 90^\circ$ . Are two triangles congruent?

**Solution:** Yes.

Reason: Given triangles are congruent

$$\text{Here } AC = CE$$

$$BC = CD$$

$$\angle B = \angle D = 90^\circ$$

By SSA criteria triangle ABC is congruent to triangle CDE.

**Question 6:** ABC is an isosceles triangle in which  $AB = AC$ . BE and CF are its two medians. Show that  $BE = CF$ .

**Solution:** ABC is an isosceles triangle (given)

$AB = AC$  (given)

BE and CF are two medians (given)

To prove:  $BE = CF$

In  $\triangle CFB$  and  $\triangle BEC$

$CE = BF$  (Since,  $AC = AB = AC/2 = AB/2 = CE = BF$ )

$BC = BC$  (Common)

$\angle ECB = \angle FBC$  (Angle opposite to equal sides are equal)

By SAS theorem:  $\triangle CFB \cong \triangle BEC$

So,  $BE = CF$  (By c.p.c.t)