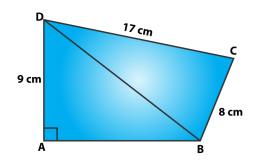


## Exercise 15.3

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Question 1: In figure, compute the area of quadrilateral ABCD.



### Solution:

A quadrilateral ABCD with DC = 17 cm, AD = 9 cm and BC = 8 cm (Given)

In right ΔABD, Using Pythagorean Theorem,

 $AB^2 + AD^2 = BD^2$ 

 $15^2 = AB^2 + 9^2$ 

AB<sup>2</sup> = 225-81=144

AB = 12

Area of  $\triangle ABD = 1/2(12 \times 9) \text{ cm}^2 = 54 \text{ cm}^2$ 

In right ΔBCD: Using Pythagorean Theorem,

 $CD^2 = BD^2 + BC^2$ 

 $17^2 = BD^2 + 8^2$ 

BD<sup>2</sup> = 289 - 64 = 225

or BD = 15

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Area of \Delta BCD = 1/2(8x17) \text{ cm}^2 = 68 \text{ cm}^2
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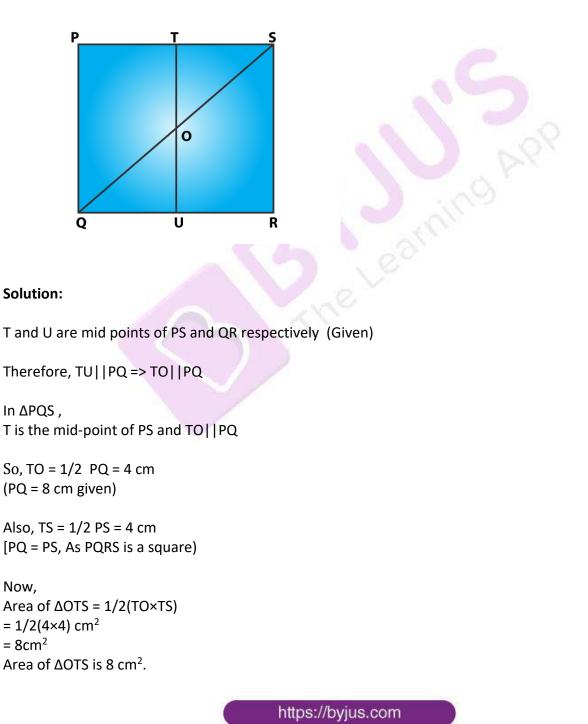


Now, area of quadrilateral ABCD = Area of  $\triangle$ ABD + Area of  $\triangle$ BCD

 $= 54 \text{ cm}^2 + 68 \text{ cm}^2$ 

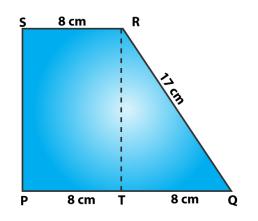
= 112 cm<sup>2</sup>

Question 2: In figure, PQRS is a square and T and U are, respectively, the mid-points of PS and QR . Find the area of  $\Delta$ OTS if PQ = 8 cm.





Question 3: Compute the area of trapezium PQRS in figure.



### Solution:

From figure,

Area of trapezium PQRS = Area of rectangle PSRT + Area of  $\Delta QRT$ 

 $= PT \times RT + 1/2 (QT \times RT)$ 

 $= 8 \times RT + 1/2(8 \times RT)$ 

= 12 RT

In right ΔQRT, Using Pythagorean Theorem,

 $QR^2 = QT^2 + RT^2$ 

 $RT^2 = QR^2 - QT^2$ 

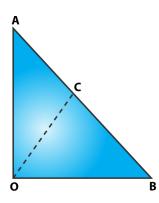
 $RT^2 = 17^2 - 8^2 = 225$ 

or RT = 15

Therefore, Area of trapezium =  $1/2 \times 15$  cm<sup>2</sup> = 180 cm<sup>2</sup>



Question 4: In figure,  $\angle AOB = 90^{\circ}$ , AC = BC, OA = 12 cm and OC = 6.5 cm. Find the area of  $\triangle AOB$ .



### Solution:

Given: A triangle AOB, with  $\angle AOB = 90^{\circ}$ , AC = BC, OA = 12 cm and OC = 6.5 cm

As we know, the midpoint of the hypotenuse of a right triangle is equidistant from the vertices.

So, CB = CA = OC = 6.5 cm

 $AB = 2 CB = 2 \times 6.5 cm = 13 cm$ 

In right ΔΟΑΒ: Using Pythagorean Theorem, we get

 $AB^2 = OB^2 + OA^2$ 

 $13^2 = OB^2 + 12^2$ 

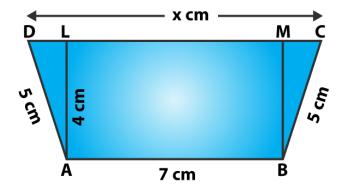
 $OB^2 = 169 - 144 = 25$ 

or OB = 5 cm

Now, Area of  $\triangle AOB = \frac{1}{2}(Base x height) cm^2 = \frac{1}{2}(12 x 5) cm^2 = 30 cm^2$ 

Question 5: In figure, ABCD is a trapezium in which AB = 7 cm, AD = BC = 5 cm, DC = x cm, and distance between AB and DC is 4 cm. Find the value of x and area of trapezium ABCD.





### Solution:

Given: ABCD is a trapezium, where AB = 7 cm, AD = BC = 5 cm, DC = x cm, and Distance between AB and DC = 4 cm

Consider AL and BM are perpendiculars on DC, then

AL = BM = 4 cm and LM = 7 cm.

In right ΔBMC : Using Pythagorean Theorem, we get

 $BC^2 = BM^2 + MC^2$ 

 $25 = 16 + MC^2$ 

 $MC^2 = 25 - 16 = 9$ 

or MC = 3

Again, In right ∆ ADL : Using Pythagorean Theorem, we get

 $AD^2 = AL^2 + DL^2$ 

 $25 = 16 + DL^2$ 

 $DL^2 = 25 - 16 = 9$ 

or DL = 3



Therefore, x = DC = DL + LM + MC = 3 + 4 + 3 = 13 => x = 13 cm

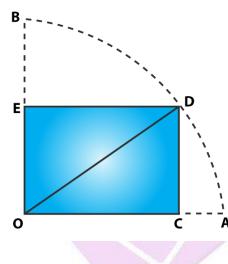
Now,

Area of trapezium ABCD = 1/2(AB + CD) AL

= 1/2(7+13)4 = 40

Area of trapezium ABCD is 40 cm<sup>2</sup>.

Question 6: In figure, OCDE is a rectangle inscribed in a quadrant of a circle of radius 10 cm. If OE = 2V5 cm, find the area of the rectangle.



Solution:

From given: Radius = OD = 10 cm and OE = 2V5 cm

In right ∆DEO, By Pythagoras theorem

 $OD^2 = OE^2 + DE^2$ 

 $(10)^2 = (2\sqrt{5})^2 + DE^2$ 

 $100 - 20 = DE^2$ 

DE = 4√5

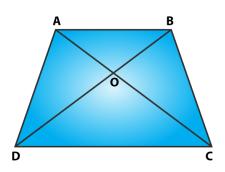


Now,

Area of rectangle OCDE = Length x Breadth = OE x DE =  $2\sqrt{5} \times 4\sqrt{5} = 40$ 

Area of rectangle is 40 cm<sup>2</sup>.

Question 7: In figure, ABCD is a trapezium in which AB || DC. Prove that  $ar(\Delta AOD) = ar(\Delta BOC)$ 



### Solution:

ABCD is a trapezium in which AB || DC (Given)

To Prove:  $ar(\Delta AOD) = ar(\Delta BOC)$ 

Proof:

From figure, we can observe that  $\triangle$ ADC and  $\triangle$ BDC are sharing common base i.e. DC and between same parallels AB and DC.

Then,  $ar(\Delta ADC) = ar(\Delta BDC)$  .....(1)

 $\Delta$ ADC is the combination of triangles,  $\Delta$ AOD and  $\Delta$ DOC. Similarly,  $\Delta$ BDC is the combination of  $\Delta$ BOC and  $\Delta$ DOC triangles.

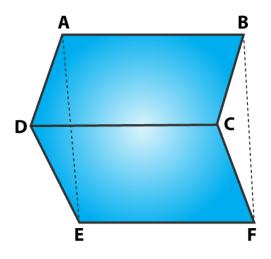
Equation (1) => ar( $\Delta AOD$ ) + ar( $\Delta DOC$ ) = ar( $\Delta BOC$ ) + ar( $\Delta DOC$ )

or  $ar(\Delta AOD) = ar(\Delta BOC)$ 

Hence Proved.

Question 8: In figure, ABCD, ABFE and CDEF are parallelograms. Prove that  $ar(\Delta ADE) = ar(\Delta BCF)$ .





### Solution:

Here, ABCD, CDEF and ABFE are parallelograms:

Which implies: AD = BC DE = CF and AE = BF

Again, from triangles ADE and BCF:

AD = BC, DE = CF and AE = BF

By SSS criterion of congruence, we have

 $\Delta ADE \cong \Delta BCF$ 

Since both the triangles are congruent, then  $ar(\Delta ADE) = ar(\Delta BCF)$ . Hence Proved,

Question 9: Diagonals AC and BD of a quadrilateral ABCD intersect each other at P. Show that: ar( $\Delta$ APB) x ar( $\Delta$ CPD) = ar( $\Delta$ APD) x ar( $\Delta$ BPC).

### Solution:

Consider: BQ and DR are two perpendiculars on AC.

To prove:  $ar(\Delta APB) \times ar(\Delta CPD) = ar(\Delta APD) \times ar(\Delta BPC)$ .



Now, L.H.S. =  $ar(\Delta APB) \times ar(\Delta CDP)$ 

=  $(1/2 \times AP \times BQ) \times (1/2 \times PC \times DR)$ 

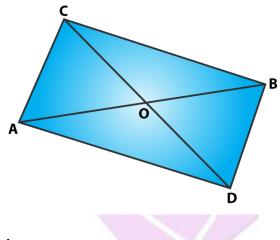
=  $(1/2 \times PC \times BQ) \times (1/2 \times AP \times DR)$ 

=  $ar(\Delta APD) \times ar(\Delta BPC)$ 

= R.H.S.

Hence proved.

Question 10: In figure, ABC and ABD are two triangles on the base AB. If line segment CD is bisected by AB at O, show that  $ar(\Delta ABC) = ar(\Delta ABD)$ .



Solution:

Draw two perpendiculars CP and DQ on AB.

Now,

 $ar(\Delta ABC) = 1/2 \times AB \times CP$  .....(1)

 $ar(\Delta ABD) = 1/2 \times AB \times DQ$  .....(2)

To prove the result,  $ar(\Delta ABC) = ar(\Delta ABD)$ , we have to show that CP = DQ.

In right angled triangles,  $\Delta CPO$  and  $\Delta DQO$ 

∠CPO = ∠DQO = 90°



CO = OD (Given)

 $\angle COP = \angle DOQ$  (Vertically opposite angles)

By AAS condition:  $\triangle CP0 \cong \triangle DQO$ So, CP = DQ .....(3) (By CPCT)

From equations (1), (2) and (3), we have

 $ar(\Delta ABC) = ar(\Delta ABD)$ 

Hence proved.