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$$\Rightarrow 4\alpha \left[\int_{-1}^0 e^{-\alpha|x|} dx + \int_0^2 e^{-\alpha|x|} dx \right] = 5$$

$$\Rightarrow 4\alpha \left[\int_{-1}^0 e^{\alpha x} dx + \int_0^2 e^{-\alpha x} dx \right] = 5$$

$$\Rightarrow 4\alpha \left[\left(\frac{1 - e^{-\alpha}}{\alpha} \right) + \left(\frac{e^{-2\alpha} - 1}{-\alpha} \right) \right] = 5$$

$$\Rightarrow 4[1 - e^{-2\alpha} - e^{-\alpha} + 1] = 5$$

Let $e^{-\alpha} = t$

$$\Rightarrow 4t^2 + 4t - 3 = 0$$

$$\Rightarrow t = \frac{1}{2} = e^{-\alpha} \Rightarrow \alpha = \log_e 2$$

7. If the sum of the first 40 terms of the series, $3 + 4 + 8 + 9 + 13 + 14 + 18 + 19 + \dots$ is $(102)m$, then m is equal to :

- a. 10
c. 5

- b. 25
d. 20

Answer: (d)

Solution:

$$S = \underline{3+4} + \underline{8+9} + 13 + 14 + \dots \dots 40 \text{ terms}$$

$$S = 7 + 17 + 27 + 37 + \dots \dots 20 \text{ terms}$$

$$S = \frac{20}{2} [14 + (19)10] = 20 \times 102$$

$$\therefore m = 20$$

8. If $\frac{3+i \sin \theta}{4-i \cos \theta}$, $\theta \in [0, 2\pi]$, is a real number, then the argument of $\sin \theta + i \cos \theta$ is :

a. $\pi - \tan^{-1} \left(\frac{4}{3} \right)$

b. $-\tan^{-1} \left(\frac{3}{4} \right)$

c. $\pi - \tan^{-1} \left(\frac{4}{3} \right)$

d. $\tan^{-1} \left(\frac{4}{3} \right)$

Answer: (a)

Solution:

$$\begin{aligned} \text{Let } z &= \frac{3+i \sin \theta}{4-i \cos \theta} \times \frac{4+i \cos \theta}{4+i \cos \theta} \\ &= \frac{12 - \sin \theta \cos \theta + i(4 \sin \theta + 3 \cos \theta)}{16 + \cos^2 \theta} \end{aligned}$$

z is real.

$$\therefore 4 \sin \theta + 3 \cos \theta = 0$$

$$\Rightarrow \tan \theta = -\frac{3}{4} \quad [\theta \text{ lies in } 2^{\text{nd}} \text{ quadrant}]$$

$$\arg(\sin \theta + i \cos \theta) = \pi + \tan^{-1} \left(\frac{\cos \theta}{\sin \theta} \right) = \pi - \tan^{-1} \left(\frac{4}{3} \right)$$

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9. Let $A = [a_{ij}]$ and $B = [b_{ij}]$ be two 3×3 real matrices such that $b_{ij} = (3)^{(i+j-2)}a_{ji}$, where $i, j = 1, 2, 3$. If the determinant of B is 81, then the determinant of A is :

- a. $\frac{1}{9}$ b. $\frac{1}{81}$
 c. $\frac{1}{3}$ d. 3

Answer: (c)

Solution:

$$b_{ij} = (3)^{(i+j-2)}a_{ji}$$

$$B = \begin{bmatrix} 3^0 a_{11} & 3a_{21} & 3^2 a_{31} \\ 3a_{12} & 3^2 a_{22} & 3^3 a_{32} \\ 3^2 a_{13} & 3^3 a_{23} & 3^4 a_{33} \end{bmatrix}$$

$$|B| = \begin{vmatrix} 3^0 a_{11} & 3a_{21} & 3^2 a_{31} \\ 3a_{12} & 3^2 a_{22} & 3^3 a_{32} \\ 3^2 a_{13} & 3^3 a_{23} & 3^4 a_{33} \end{vmatrix}$$

Taking 3^2 common each from C_3 and R_3

$$|B| = 81 \begin{vmatrix} a_{11} & 3a_{21} & a_{31} \\ 3a_{12} & 3^2 a_{22} & 3a_{32} \\ a_{13} & 3a_{23} & a_{33} \end{vmatrix}$$

Taking 3 common each from C_2 and R_2

$$|B| = 81(9) \begin{vmatrix} a_{11} & a_{21} & a_{31} \\ a_{12} & a_{22} & a_{32} \\ a_{13} & a_{23} & a_{33} \end{vmatrix}$$

Given $|B| = 81$

$$\Rightarrow 81 = 81(9)|A| \Rightarrow |A| = \frac{1}{9}$$

10. Let $f(x)$ be a polynomial of degree 5 such that $x = \pm 1$ are its critical points. If $\lim_{x \rightarrow 0} \left(2 + \frac{f(x)}{x^3} \right) = 4$, then which one of the following is not true?

- a. $f(1) - 4f(-1) = 4$
 b. $x = 1$ is a point of maxima and $x = -1$ is a point of minimum of f .
 c. f is an odd function.
 d. $x = 1$ is a point of minima and $x = -1$ is a point of maxima of f .

Answer: (d)

Solution:

Given $\lim_{x \rightarrow 0} \left(2 + \frac{f(x)}{x^3} \right) = 4$

$$\lim_{x \rightarrow 0} \frac{f(x)}{x^3} = 2$$

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$\lim_{x \rightarrow 0} \frac{f(x)}{x^3}$ Limit exists and it is finite

$$\therefore f(x) = ax^5 + bx^4 + cx^3$$

$$\Rightarrow \lim_{x \rightarrow 0} (ax^2 + bx + c) = 2$$

$$c = 2$$

$$\text{Also } f'(x) = 5ax^4 + 4bx^3 + 6x^2$$

$$f'(1) = 5a + 4b + 6 = 0$$

$$f'(-1) = 5a - 4b + 6 = 0$$

$$b = 0, \quad a = -\frac{6}{5}$$

$$f(x) = -\frac{6}{5}x^5 + 2x^3 \Rightarrow f(x) \text{ is odd}$$

$$f'(x) = -6x^4 + 6x^2$$

$$f''(x) = -24x^3 + 12x$$

$$(f''(1) < 0) \qquad (f''(-1) > 0)$$

At $x = -1$ there is local minima and at $x = 1$ there is local maxima.

$$\text{And } f(1) - 4f(-1) = 4$$

11. The number of ordered pairs (r, k) for which $6 \cdot {}^{35}C_r = (k^2 - 3) \cdot {}^{36}C_{r+1}$, where k is an integer, is:

- a. 4
c. 2

- b. 6
d. 3

Answer: (a)

Solution:

$$\text{Using } {}^{36}C_{r+1} = \frac{36}{r+1} \times {}^{35}C_r$$

$$\frac{36}{r+1} \times {}^{35}C_r \times (k^2 - 3) = {}^{35}C_r \times 6$$

$$k^2 - 3 = \frac{r+1}{6}$$

$$k^2 = \frac{r+1}{6} + 3$$

$$k \in \mathbb{I}$$

$$r \rightarrow \text{Non-negative integer } 0 \leq r \leq 35$$

$$r = 5 \Rightarrow k = \pm 2$$

$$r = 35 \Rightarrow k = \pm 3$$

$$\text{No. of ordered pairs } (r, k) = 4$$

12. Let a_1, a_2, a_3, \dots be a G.P. such that $a_1 < 0$, $a_1 + a_2 = 4$ and $a_3 + a_4 = 16$. If $\sum_{i=1}^9 a_i = 4\lambda$, then λ is equal to:

a. 171

b. $\frac{511}{3}$

c. -171

d. -513

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Answer: (c)

Solution:

$$a_1 + a_2 = 4 \Rightarrow a + ar = 4 \Rightarrow a(1 + r) = 4$$

$$a_3 + a_4 = 16 \Rightarrow ar^2 + ar^3 = 16 \Rightarrow ar^2(1 + r) = 16 \Rightarrow 4r^2 = 16$$

$$\Rightarrow r = \pm 2$$

If $r = 2, a = \frac{4}{3}$ which is not possible as $a_1 < 0$

If $r = -2, a = -4$

$$\sum_{i=1}^9 a_i = \frac{a(r^9 - 1)}{r - 1} = \frac{(-4)[(-2)^9 - 1]}{-3} = \frac{4}{3}(-512 - 1) = 4(-171)$$

$$\lambda = -171$$

13. Let \vec{a}, \vec{b} and \vec{c} be three unit vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$. If $\lambda = \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ and $\vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$, then the ordered pair (λ, \vec{d}) is equal to :

a. $(\frac{3}{2}, 3\vec{a} \times \vec{c})$

b. $(-\frac{3}{2}, 3\vec{c} \times \vec{b})$

c. $(-\frac{3}{2}, 3\vec{a} \times \vec{b})$

d. $(\frac{3}{2}, 3\vec{b} \times \vec{c})$

Answer: (c)

Solution:

$$\text{Given } \vec{a} + \vec{b} + \vec{c} = \vec{0} \quad \lambda = \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$$

$$\Rightarrow |\vec{a} + \vec{b} + \vec{c}|^2 = |\vec{0}|^2$$

$$|\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) = 0$$

$$\lambda = -\frac{3}{2}$$

$$\text{Also } \vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$$

$$\Rightarrow \vec{d} = \vec{a} \times \vec{b} + \vec{b} \times (-\vec{a} - \vec{b}) + (-\vec{a} - \vec{b}) \times \vec{a}$$

$$\Rightarrow \vec{d} = \vec{a} \times \vec{b} + \vec{a} \times \vec{b} + \vec{a} \times \vec{b}$$

$$\Rightarrow \vec{d} = 3(\vec{a} \times \vec{b}) = 3\vec{a} \times \vec{b}$$

14. Let $y = y(x)$ be the solution curve of the differential equation, $(y^2 - x) \frac{dy}{dx} = 1$, satisfying $y(0) = 1$

This curve intersects the x - axis at a point whose abscissa is :

a. $2 + e$

b. 2

c. $2 - e$

d. $-e$

Answer: (c)

Solution:

$$(y^2 - x) \frac{dy}{dx} = 1$$

$$\frac{dx}{dy} + x = y^2$$

$$xe^y = \int y^2 e^y dy$$

$$x = y^2 - 2y + 2 + ce^{-y}$$

$$\text{Given } y(0) = 1$$

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$$\Rightarrow c = -e$$

$$\therefore \text{Solution is } x = y^2 - 2y + 2 - e^{-y+1}$$

\therefore The value of x where the curve cuts the x - axis will be at $x = 2 - e$

15. If θ_1 and θ_2 be respectively the smallest and the largest values of θ in $(0, 2\pi) - \{\pi\}$ which satisfy the equation, $2 \cot^2 \theta - \frac{5}{\sin \theta} + 4 = 0$, then $\int_{\theta_1}^{\theta_2} \cos^2 3\theta \, d\theta$ is equal to :

a. $\frac{2\pi}{3}$

b. $\frac{\pi}{3}$

c. $\frac{\pi}{3} + \frac{1}{6}$

d. $\frac{\pi}{9}$

Answer: (b)

Solution:

$$2 \cot^2 \theta - \frac{5}{\sin \theta} + 4 = 0, \theta \in [0, 2\pi)$$

$$\Rightarrow 2 \operatorname{cosec}^2 \theta - 2 - 5 \operatorname{cosec} \theta + 4 = 0$$

$$\Rightarrow 2 \operatorname{cosec}^2 \theta - 4 \operatorname{cosec} \theta - \operatorname{cosec} \theta + 2 = 0$$

$$\Rightarrow \operatorname{cosec} \theta = 2 \text{ or } \frac{1}{2} \text{ (Not possible)}$$

As $\theta \in [0, 2\pi)$,

$$\theta_1 = \frac{\pi}{6}, \theta_2 = \frac{5\pi}{6}$$

$$\Rightarrow \int_{\theta_1}^{\theta_2} \cos^2 3\theta \, d\theta = \int_{\frac{\pi}{6}}^{\frac{5\pi}{6}} \frac{(1 + \cos 6\theta)}{2} \, d\theta$$

$$= \frac{1}{2} \left(\frac{5\pi}{6} - \frac{\pi}{6} \right) + \frac{\sin 6\theta}{12} \Big|_{\frac{\pi}{6}}^{\frac{5\pi}{6}}$$

$$= \frac{\pi}{3}$$

16. Let α and β are the roots of the equation $x^2 - x - 1 = 0$. If $p_k = (\alpha)^k + (\beta)^k, k \geq 1$ then which one of the following statements is not true?

a. $(p_1 + p_2 + p_3 + p_4 + p_5) = 26$

b. $p_5 = 11$

c. $p_5 = p_2 \cdot p_3$

d. $p_3 = p_5 - p_4$

Answer: (c)

Solution:

Given α, β are the roots of $x^2 - x - 1 = 0$

$$\Rightarrow \alpha + \beta = 1 \text{ \& } \alpha\beta = -1$$

$$\Rightarrow \alpha^2 = \alpha + 1 \text{ \& } \beta^2 = \beta + 1$$

$$p_k = \alpha^{k-2} \alpha^2 + \beta^{k-2} \beta^2$$

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$$\begin{aligned}p_k &= \alpha^{k-2}(\alpha + 1) + \beta^{k-2}(\beta + 1) \\p_k &= \alpha^{k-1} + \beta^{k-1} + \alpha^{k-2} + \beta^{k-2} \\&\Rightarrow p_k = p_{k-1} + p_{k-2} \\&\Rightarrow p_3 = p_2 + p_1 = 4 \\p_4 &= p_3 + p_2 = 7 \\p_5 &= p_4 + p_3 = 11 \\&\therefore p_5 \neq p_2 \cdot p_3 \text{ \& } p_1 + p_2 + p_3 + p_4 + p_5 = 26 \\&\text{\& } p_3 = p_5 - p_4\end{aligned}$$

17. The area (in sq. units) of the region $\{(x, y) \in \mathbb{R} \mid 4x^2 \leq y \leq 8x + 12\}$ is :

a. $\frac{125}{3}$

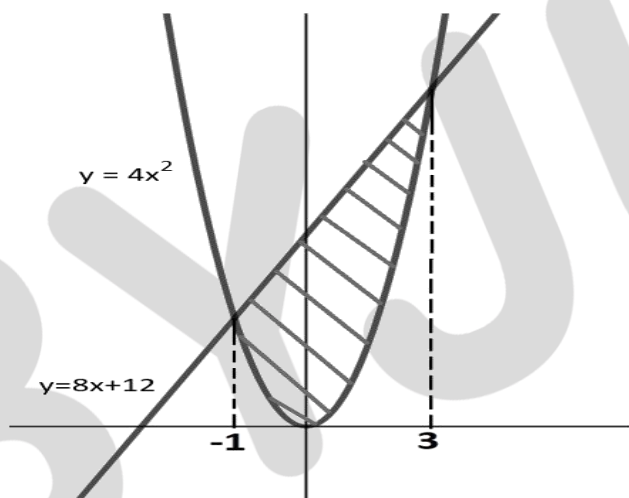
b. $\frac{128}{3}$

c. $\frac{124}{3}$

d. $\frac{127}{3}$

Answer: (b)

Solution:



For point of intersection,

$$4x^2 = 8x + 12$$

$$\Rightarrow x^2 - 2x - 3 = 0$$

$$\Rightarrow x = 3, -1$$

Area bounded is given by

$$A = \int_{-1}^3 (8x + 12 - 4x^2) dx$$

$$A = \left[\frac{8x^2}{2} + 12x - \frac{4x^3}{3} \right]_{-1}^3$$

$$A = (36 + 36 - 36) - \left(4 - 12 + \frac{4}{3} \right)$$

$$A = 44 - \frac{4}{3} = \frac{128}{3}$$

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18. The value of c in Lagrange's mean value theorem for the function $f(x) = x^3 - 4x^2 + 8x + 11$, where $x \in [0,1]$ is :

a. $\frac{4-\sqrt{7}}{3}$

b. $\frac{2}{3}$

c. $\frac{\sqrt{7}-2}{3}$

d. $\frac{4-\sqrt{5}}{3}$

Answer: (a)

Solution:

LMVT is applicable on $f(x)$ in $[0,1]$, therefore it is continuous and differentiable in $[0,1]$

Now, $f(0) = 11, f(1) = 16$

$f'(x) = 3x^2 - 8x + 8$

$\therefore f'(c) = \frac{f(1)-f(0)}{1-0} = \frac{16-11}{1}$

$\Rightarrow 3c^2 - 8c + 8 = 5$

$\Rightarrow 3c^2 - 8c + 3 = 0$

$\Rightarrow c = \frac{8 \pm 2\sqrt{7}}{6} = \frac{4 \pm \sqrt{7}}{3}$

As $c \in (0,1)$

We get, $c = \frac{4-\sqrt{7}}{3}$

19. Let $y = y(x)$ be a function of x satisfying $y\sqrt{1-x^2} = k - x\sqrt{1-y^2}$ where k is a constant and $y\left(\frac{1}{2}\right) = -\frac{1}{4}$. Then $\frac{dy}{dx}$ at $x = \frac{1}{2}$, is equal to :

a. $-\frac{\sqrt{5}}{2}$

b. $\frac{\sqrt{5}}{2}$

c. $-\frac{\sqrt{5}}{4}$

d. $\frac{2}{\sqrt{5}}$

Answer: (a)

Solution:

$y\sqrt{1-x^2} = k - x\sqrt{1-y^2}$

Differentiating w.r.t. x on both the sides, we get:

$y'\sqrt{1-x^2} + y \times \frac{1}{2\sqrt{1-x^2}} \times (-2x) = -\sqrt{1-y^2} - x \times \frac{1}{2\sqrt{1-y^2}} \times (-2y)y'$

$\Rightarrow y'\sqrt{1-x^2} - \frac{xy}{\sqrt{1-x^2}} + \sqrt{1-y^2} - \frac{xy}{\sqrt{1-y^2}}y' = 0$

$\Rightarrow y' \left[\sqrt{1-x^2} - \frac{xy}{\sqrt{1-y^2}} \right] = \frac{xy}{\sqrt{1-x^2}} - \sqrt{1-y^2}$

Putting $x = \frac{1}{2}, y = -\frac{1}{4}$

$\Rightarrow y' \left[\frac{\sqrt{3}}{2} + \frac{\frac{1}{8}}{\frac{\sqrt{15}}{4}} \right] = -\frac{\frac{1}{8}}{\frac{\sqrt{3}}{2}} - \frac{\sqrt{15}}{4}$

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$$\Rightarrow y' \left[\frac{\sqrt{3}}{2} + \frac{1}{2\sqrt{15}} \right] = -\frac{1}{4\sqrt{3}} - \frac{\sqrt{15}}{4}$$

$$\Rightarrow y' \left[\frac{\sqrt{45}+1}{2\sqrt{15}} \right] = -\frac{1+\sqrt{45}}{4\sqrt{3}}$$

$$\Rightarrow y' = -\frac{\sqrt{5}}{2}$$

20. Let the tangents drawn from the origin to the circle, $x^2 + y^2 - 8x - 4y + 16 = 0$ touch it at the points A and B . The $(AB)^2$ is equal to :

a. $\frac{32}{5}$

b. $\frac{64}{5}$

c. $\frac{52}{5}$

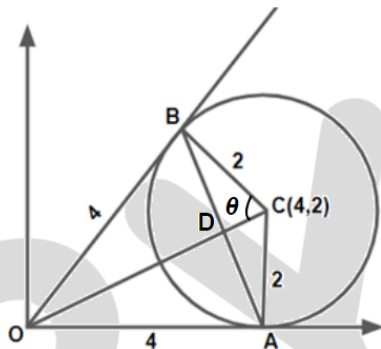
d. $\frac{56}{5}$

Answer: (b)

Solution:

$$x^2 + y^2 - 8x - 4y + 16 = 0$$

$$(x - 4)^2 + (y - 2)^2 = 4 \Rightarrow \text{Centre } (4, 2), \text{ radius} = 2$$



$$OA = 4 = OB$$

In $\triangle OBC$

$$\tan \theta = \frac{4}{2} = 2 \Rightarrow \sin \theta = \frac{2}{\sqrt{5}}$$

In $\triangle BDC$

$$\sin \theta = \frac{BD}{2} \Rightarrow BD = \frac{4}{\sqrt{5}}$$

$$\text{Length of chord of contact } (AB) = \frac{8}{\sqrt{5}}$$

Alternative

(l) length of tangent = 4 and (r) radius = 2

$$\Rightarrow \text{Length of chord of contact} = \frac{2lr}{\sqrt{l^2 + r^2}}$$

$$\text{Square of length of chord of contact} = \frac{64}{5}$$

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21. If system of linear equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$3x + 2y + \lambda z = \mu$$

has more than two solutions, then $\mu - \lambda^2$ is equal to _____.

Answer: (13)

Solution:

The system of equations has more than 2 solutions

$$\therefore D = D_3 = 0$$

$$\Rightarrow \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 3 & 2 & \lambda \end{vmatrix} = 0 \Rightarrow 2\lambda - 6 - \lambda + 9 + 2 - 6 = 0$$

$$\Rightarrow \lambda = 1$$

$$\begin{vmatrix} 1 & 1 & 6 \\ 1 & 2 & 10 \\ 3 & 2 & \mu \end{vmatrix} = 0 \Rightarrow 2\mu - 20 - \mu + 30 - 24 = 0$$

$$\Rightarrow \mu = 14$$

$$\text{So, } \mu - \lambda^2 = 13$$

22. If the foot of perpendicular drawn from the point $(1, 0, 3)$ on a line passing through $(\alpha, 7, 1)$ is

$\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3}\right)$, then α is equal to _____.

Answer: (4)

Solution:

Given points $P(1, 0, 3)$ and $Q\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3}\right)$

Direction ratios of line $L: \left(\alpha - \frac{5}{3}, 7 - \frac{7}{3}, 1 - \frac{17}{3}\right)$

$$= \left(\frac{3\alpha - 5}{3}, \frac{14}{3}, -\frac{14}{3}\right)$$

Direction ratios of $PQ: \left(-\frac{2}{3}, -\frac{7}{3}, -\frac{8}{3}\right)$

As line L is perpendicular to PQ

$$\text{So, } \left(\frac{3\alpha - 5}{3}\right)\left(-\frac{2}{3}\right) + \left(\frac{14}{3}\right)\left(-\frac{7}{3}\right) + \left(-\frac{14}{3}\right)\left(-\frac{8}{3}\right) = 0$$

$$\Rightarrow -6\alpha + 10 - 98 + 112 = 0 \Rightarrow 6\alpha = 24 \Rightarrow \alpha = 4$$

23. If the function f defined on $\left(-\frac{1}{3}, \frac{1}{3}\right)$ by

$$f(x) = \begin{cases} \left(\frac{1}{x}\right) \log_e \left(\frac{1+3x}{1-2x}\right) & \text{when } x \neq 0 \\ k & \text{when } x = 0 \end{cases}$$

is continuous, the k is equal to _____.

Answer: (5)

Solution:

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As $f(x)$ is continuous

$$\Rightarrow \lim_{x \rightarrow 0} f(x) = f(0) = k$$

$$\Rightarrow \lim_{x \rightarrow 0} \left(\frac{1}{x}\right) \log_e \left(\frac{1+3x}{1-2x}\right) = k$$

$$\Rightarrow \lim_{x \rightarrow 0} \frac{3 \log(1+3x)}{3x} + \lim_{x \rightarrow 0} \frac{(-2) \log(1-2x)}{(-2x)} = k$$

$$\Rightarrow 3 + 2 = k \Rightarrow k = 5$$

24. If the mean and variance of eight numbers 3, 7, 9, 12, 13, 20, x and y be 10 and 25 respectively then xy is equal to _____.

Answer: (54)

Solution:

$$\text{Mean} = 10 \Rightarrow \frac{64+x+y}{8} = 10$$

$$\Rightarrow x + y = 16$$

$$\text{Variance} = \frac{\sum x_i^2}{n} - (\bar{x})^2$$

$$\Rightarrow 25 = \frac{3^2+7^2+9^2+12^2+13^2+20^2+x^2+y^2}{8} - 100$$

$$\Rightarrow 1000 = 852 + x^2 + y^2$$

$$\Rightarrow x^2 + y^2 = 148$$

$$\Rightarrow (x + y)^2 - 2xy = 148$$

$$\Rightarrow 256 - 2xy = 148$$

$$\text{So, } xy = 54$$

25. Let $X = \{n \in \mathbf{N} : 1 \leq n \leq 50\}$. If $A = \{n \in X : n \text{ is a multiple of } 2\}$ and $B = \{n \in X : n \text{ is a multiple of } 7\}$, then the number of elements in the smallest subset of X containing both A and B is _____.

Answer: (29)

Solution:

$$A = \{x : x \text{ is multiple of } 2\} = \{2, 4, 6, 8, \dots\}$$

$$B = \{x : x \text{ is multiple of } 7\} = \{7, 14, 21, \dots\}$$

$$X = \{x : 1 \leq x \leq 50, x \in \mathbf{N}\}$$

Smallest subset of X which contains elements of both A and B is a set with multiples of 2 or 7 less than 50.

$$P = \{x : x \text{ is a multiple of } 2 \text{ less than or equal to } 50\}$$

$$Q = \{x : x \text{ is a multiple of } 7 \text{ less than or equal to } 50\}$$

$$n(P \cup Q) = n(P) + n(Q) - n(P \cap Q)$$

$$= 25 + 7 - 3$$

$$= 29$$