



- a. zero
 b. antiparallel to $\frac{i+j}{\sqrt{2}}$
 c. parallel to $\frac{i+j}{\sqrt{2}}$
 d. parallel to \hat{k}

Solution: (b)

Force due to electric field is in direction $-\frac{i+j}{\sqrt{2}}$

Because at $t = 0, E = -\frac{(i+j)}{\sqrt{2}} E_0$

Force due to magnetic field is in direction $q(\vec{v} \times \vec{B})$ and $\vec{v} \parallel \hat{k}$

\therefore It is parallel to \vec{E}

\therefore Net force is antiparallel to $\frac{(i+j)}{\sqrt{2}}$.

16. A thin lens made of glass (refractive index = 1.5) of focal length $f = 16 \text{ cm}$ is immersed in a liquid of refractive index 1.42. If its focal length in liquid is f_l , then the ratio f_l/f is closest to the integer

- a. 9
 b. 17
 c. 1
 d. 5

Solution:

(a)

$$\frac{1}{f_a} = \left(\frac{\mu_g}{\mu_a} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$\frac{1}{f_l} = \left(\frac{\mu_g}{\mu_m} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$\Rightarrow \frac{f_a}{f_l} = \frac{\left(\frac{\mu_g}{\mu_l} - 1\right)}{\left(\frac{\mu_g}{\mu_a} - 1\right)} = \frac{\left(\frac{1.50}{1.42} - 1\right)}{\left(\frac{1.50}{1} - 1\right)} = \frac{0.08}{(1.42)(0.5)}$$

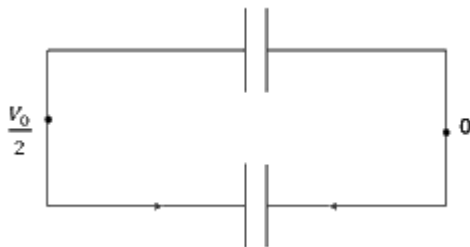
$$\frac{f_l}{f_a} = \frac{(1.42)(0.5)}{0.08} = 8.875 = 9$$

17. An elevator in a building can carry a maximum of 10 persons, with the average mass of each person being 68 kg . The mass of the elevator itself is 920 kg and it moves with a constant speed of 3 m/s . The frictional force opposing the motion is 6000 N . If the elevator is moving up with its full capacity, the power delivered by the motor to the elevator ($g = 10 \text{ m/s}^2$) must be at least

- a. 66000 W
 b. 63360 W
 c. 48000 W
 d. 56300 W

Solution: (a)

Net force on motor will be



$$V_0 = 20 \text{ V}$$

$$\text{Initial potential energy } U_i = \frac{1}{2} CV_0^2$$

After connecting identical capacitor in parallel, voltage across each capacitor will be $\frac{V_0}{2}$. Then, final potential energy $U_f = 2 \left[\frac{1}{2} C \left(\frac{V_0}{2} \right)^2 \right]$

$$\text{Heat loss} = U_i - U_f$$

$$= \frac{CV_0^2}{2} - \frac{CV_0^2}{4} = \frac{CV_0^2}{4} = \frac{60 \times 10^{-12} \times 20^2}{4} = 6 \times 10^{-9} = 6 \text{ nJ}$$

22. M grams of steam at 100°C is mixed with 200 g of ice at its melting point in a thermally insulated container. If it produces liquid water at 40°C [heat of vaporization of water is 540 cal/g and heat of fusion of ice is 80 cal/g], the value of M is _____.

Solution: (40)

$$\text{Here, heat absorbed by ice} = m_{ice} L_f + m_{ice} C_w(40 - 0)$$

$$\text{Heat released by steam} = m_{steam} L_v + m_{steam} C_w(100 - 40)$$

Heat absorbed = heat released

$$m_{ice} L_f + m_{ice} C_w(40 - 0) = m_{steam} L_v + m_{steam} C_w(100 - 40)$$

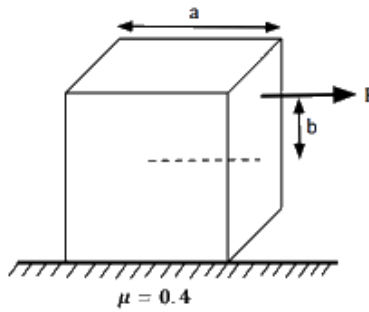
$$\Rightarrow 200 \times 80 \text{ cal/g} + 200 \times 1 \text{ cal/g/}^\circ\text{C} \times (40 - 0)$$

$$= m \times 540 \text{ cal/g} + 540 \times 1 \text{ cal/g/}^\circ\text{C} \times (100 - 40)$$

$$\Rightarrow 200 [80 + (40)1] = m[540 + (60)1]$$

$$m = 40 \text{ g}$$

23. Consider a uniform cubical box of side a on a rough floor that is to be moved by applying minimum possible force F at a point b above its centre of mass (see figure). If the coefficient of friction is $\mu = 0.4$, the maximum value of $100 \times \frac{b}{a}$ for the box not to topple before moving is _____.



Solution: (50)

F balances kinetic friction so that the block can move

So, $F = \mu mg$

For no toppling, the net torque about bottom right edge should be zero

i.e.

$$F \left(\frac{a}{2} + b \right) \leq mg \frac{a}{2}$$

$$\mu mg \left(\frac{a}{2} + b \right) \leq mg \frac{a}{2}$$

$$\mu \frac{a}{2} + \mu b \leq \frac{a}{2}$$

$$0.2a + 0.4b \leq 0.5a$$

$$0.4b \leq 0.3a$$

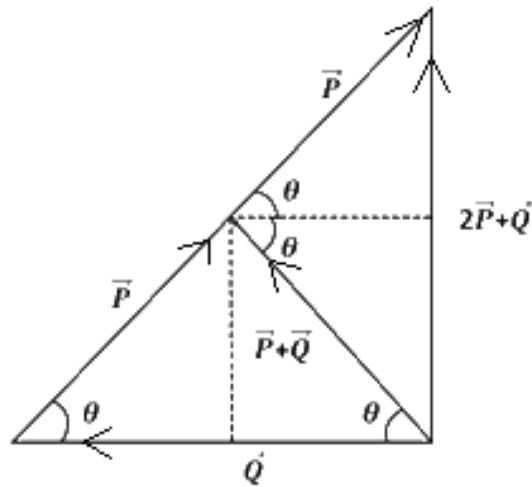
$$b \leq \frac{3}{4} a$$

But, maximum value of b can only be $0.5a$

\therefore Maximum value of $100 \frac{b}{a}$ is 50.

24. The sum of two forces \vec{P} and \vec{Q} is \vec{R} such that $|\vec{R}| = |\vec{P}|$. The angle θ (in degrees) that the resultant of $2\vec{P}$ and \vec{Q} will make with \vec{Q} is _____

Solution: (90°)



25. The balancing length for a cell is 560 cm in a potentiometer experiment. When an external resistance of $10\ \Omega$ is connected in parallel to the cell, the balancing length changes by 60 cm . If the internal resistance of the cell is $\frac{N}{10}\ \Omega$, the value of N is _____

Solution : (12)

Let the emf of cell is ε internal resistance is ' r ' and potential gradient is x .

$$\varepsilon = 560x \quad (1)$$

After connecting the resistor

$$\frac{\varepsilon \times 10}{10 + r} = 500x \quad (2)$$

From (1) and (2)

$$\frac{560 \times 10}{10 + r} = 500x$$

$$56 = 540 + 5r$$

$$r = \frac{6}{5} = 1.2\ \Omega$$

$$n = 12$$

