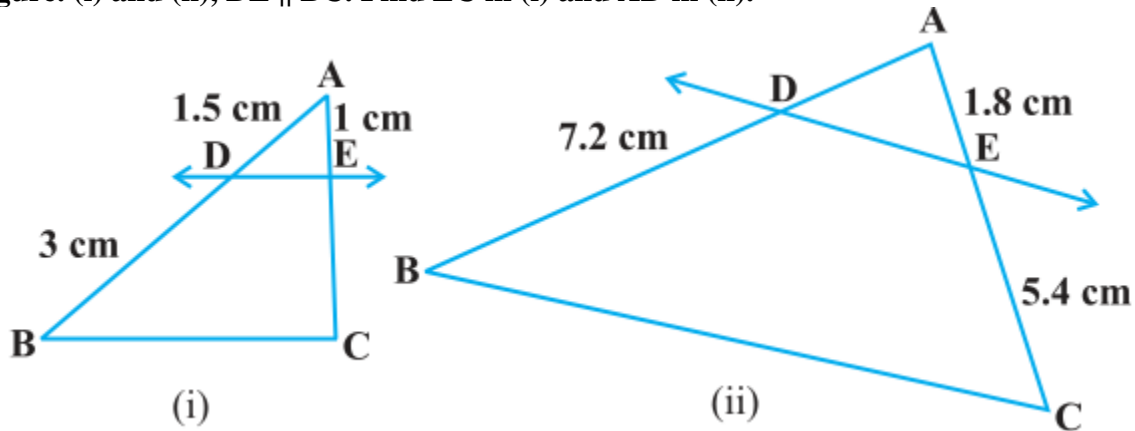


Exercise 6.2

1. In figure. (i) and (ii),  $DE \parallel BC$ . Find EC in (i) and AD in (ii).



**Solution:**

(i) Given, in  $\triangle ABC$ ,  $DE \parallel BC$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} \text{ [Using Basic proportionality theorem]}$$

$$\Rightarrow \frac{1.5}{3} = \frac{1}{EC}$$

$$\Rightarrow EC = \frac{3}{1.5}$$

$$EC = 3 \times \frac{10}{15} = 2 \text{ cm}$$

Hence,  $EC = 2 \text{ cm}$ .

(ii) Given, in  $\triangle ABC$ ,  $DE \parallel BC$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} \text{ [Using Basic proportionality theorem]}$$

$$\Rightarrow \frac{AD}{7.2} = \frac{1.8}{5.4}$$

$$\Rightarrow AD = 1.8 \times \frac{7.2}{5.4} = \frac{18}{10} \times \frac{72}{10} \times \frac{10}{54} = \frac{24}{10}$$

$$\Rightarrow AD = 2.4$$

Hence,  $AD = 2.4 \text{ cm}$ .

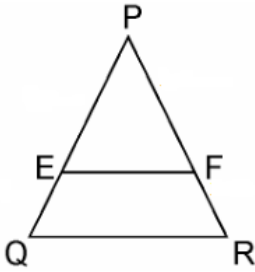
2. E and F are points on the sides PQ and PR respectively of a  $\triangle PQR$ . For each of the following cases, state whether  $EF \parallel QR$ .

(i)  $PE = 3.9 \text{ cm}$ ,  $EQ = 3 \text{ cm}$ ,  $PF = 3.6 \text{ cm}$  and  $FR = 2.4 \text{ cm}$

(ii)  $PE = 4 \text{ cm}$ ,  $QE = 4.5 \text{ cm}$ ,  $PF = 8 \text{ cm}$  and  $RF = 9 \text{ cm}$

(iii)  $PQ = 1.28 \text{ cm}$ ,  $PR = 2.56 \text{ cm}$ ,  $PE = 0.18 \text{ cm}$  and  $PF = 0.63 \text{ cm}$

**Solution:** Given, in  $\triangle PQR$ , E and F are two points on side PQ and PR respectively. See the figure below;



(i) Given, PE = 3.9 cm, EQ = 3 cm, PF = 3.6 cm and FR = 2.4 cm

Therefore, by using Basic proportionality theorem, we get,

$$\frac{PE}{EQ} = \frac{3.9}{3} = \frac{39}{30} = \frac{13}{10} = 1.3$$

And,  $\frac{PF}{FR} = \frac{3.6}{2.4} = \frac{36}{24} = \frac{3}{2} = 1.5$

So, we get,  $\frac{PE}{EQ} \neq \frac{PF}{FR}$

Hence, EF is not parallel to QR.

(ii) Given, PE = 4 cm, QE = 4.5 cm, PF = 8cm and RF = 9cm

Therefore, by using Basic proportionality theorem, we get,

$$\frac{PE}{QE} = \frac{4}{4.5} = \frac{40}{45} = \frac{8}{9}$$

And,  $\frac{PF}{RF} = \frac{8}{9}$

So, we get here,

$$\frac{PE}{QE} = \frac{PF}{RF}$$

Hence, EF is parallel to QR.

(iii) Given, PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm and PF = 0.36 cm

From the figure,

$$EQ = PQ - PE = 1.28 - 0.18 = 1.10 \text{ cm}$$

And,  $FR = PR - PF = 2.56 - 0.36 = 2.20 \text{ cm}$

So,  $\frac{PE}{EQ} = \frac{0.18}{1.10} = \frac{18}{110} = \frac{9}{55}$  ..... (i)

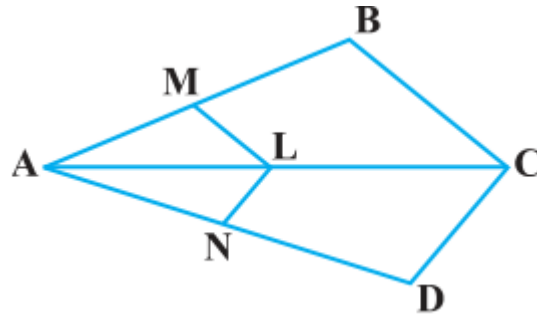
And,  $\frac{PF}{FR} = \frac{0.36}{2.20} = \frac{36}{220} = \frac{9}{55}$  ..... (ii)

So, we get here,

$$\frac{PE}{EQ} = \frac{PF}{FR}$$

Hence, EF is parallel to QR.

3. In the figure, if LM || CB and LN || CD, prove that AM/MB = AN/AD



**Solution:** In the given figure, we can see,  $LM \parallel CB$ ,

By using basic proportionality theorem, we get,

$$\frac{AM}{AB} = \frac{AL}{AC} \dots\dots\dots \text{(i)}$$

Similarly, given,  $LN \parallel CD$  and using basic proportionality theorem,

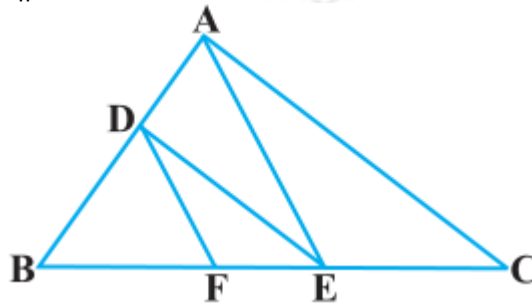
$$\therefore \frac{AN}{AD} = \frac{AL}{AC} \dots\dots\dots \text{(ii)}$$

From equation (i) and (ii), we get,

$$\frac{AM}{AB} = \frac{AN}{AD}$$

Hence, proved.

**4. In the figure,  $DE \parallel AC$  and  $DF \parallel AE$ . Prove that  $BF/FE = BE/EC$**



**Solution:** In  $\triangle ABC$ , given as,  $DE \parallel AC$

Thus, by using Basic Proportionality Theorem, we get,

$$\therefore \frac{BD}{DA} = \frac{BE}{EC} \dots\dots\dots \text{(i)}$$

In  $\triangle ABC$ , given as,  $DF \parallel AE$

Thus, by using Basic Proportionality Theorem, we get,

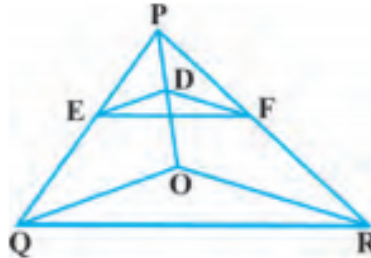
$$\therefore \frac{BD}{DA} = \frac{BF}{FE} \dots\dots\dots \text{(ii)}$$

From equation (i) and (ii), we get

$$\frac{BE}{EC} = \frac{BF}{FE}$$

Hence, proved.

5. In the figure,  $DE \parallel OQ$  and  $DF \parallel OR$ , show that  $EF \parallel QR$ .



**Solution: Given,**

In  $\triangle PQO$ ,  $DE \parallel OQ$

So by using Basic Proportionality Theorem,

$$\frac{PD}{DO} = \frac{PE}{EQ} \dots\dots\dots(\mathbf{i})$$

Again given, in  $\triangle PQR$ ,  $DF \parallel OR$ ,

So by using Basic Proportionality Theorem,

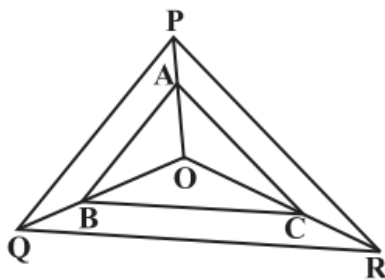
$$\frac{PD}{DO} = \frac{PF}{FR} \dots\dots\dots(\mathbf{ii})$$

From equation (i) and (ii), we get,

$$\frac{PE}{EQ} = \frac{PF}{FR}$$

Therefore, by converse of Basic Proportionality Theorem,  
 $EF \parallel QR$ , in  $\triangle PQR$ .

6. In the figure, A, B and C are points on OP, OQ and OR respectively such that  $AB \parallel PQ$  and  $AC \parallel PR$ . Show that  $BC \parallel QR$ .



**Solution: Given here,**

In  $\triangle OPQ$ ,  $AB \parallel PQ$

By using Basic Proportionality Theorem,

$$\frac{OA}{AP} = \frac{OB}{BQ} \dots\dots\dots\text{(i)}$$

Also given,

In  $\triangle OPR$ ,  $AC \parallel PR$

By using Basic Proportionality Theorem

$$\therefore \frac{OA}{AP} = \frac{OC}{CR} \dots\dots\dots\text{(ii)}$$

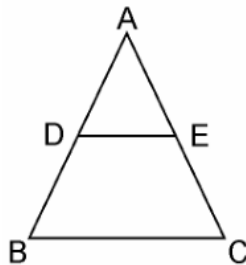
From equation (i) and (ii), we get,

$$\frac{OB}{BQ} = \frac{OC}{CR}$$

Therefore, by converse of Basic Proportionality Theorem,

In  $\triangle OQR$ ,  $BC \parallel QR$ .

**7. Using Basic proportionality theorem, prove that a line drawn through the mid-points of one side of a triangle parallel to another side bisects the third side. (Recall that you have proved it in Class IX).**



Solution: Given, in  $\triangle ABC$ , D is the midpoint of AB such that  $AD=DB$ .  
A line parallel to BC intersects AC at E as shown in above figure such that  $DE \parallel BC$ .

We have to prove that E is the mid point of AC.

Since, D is the mid-point of AB.

$$\therefore AD=DB$$

$$\Rightarrow \frac{AD}{DB} = 1 \dots\dots\dots\text{(i)}$$

In  $\triangle ABC$ ,  $DE \parallel BC$ ,

By using Basic Proportionality Theorem,

Therefore,  $\frac{AD}{DB} = \frac{AE}{EC}$

From equation (i), we can write,

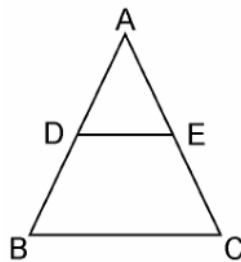
$$\Rightarrow 1 = \frac{AE}{EC}$$

$$\therefore AE = EC$$

Hence, proved, E is the midpoint of AC.

**8. Using Converse of basic proportionality theorem, prove that the line joining the mid-points of any two sides of a triangle is parallel to the third side. (Recall that you have done it in Class IX).**

**Solution:** Given, in  $\triangle ABC$ , D and E are the mid points of AB and AC respectively, such that,  $AD=BD$  and  $AE=EC$ .



We have to prove that:  $DE \parallel BC$ .

Since, D is the midpoint of AB

$$\therefore AD=BD$$

$$\Rightarrow \frac{AD}{BD} = 1 \dots\dots\dots \text{(i)}$$

Also given, E is the mid-point of AC.

$$\therefore AE=EC$$

$$\Rightarrow \frac{AE}{EC} = 1$$

From equation (i) and (ii), we get,

$$\frac{AD}{BD} = \frac{AE}{EC}$$

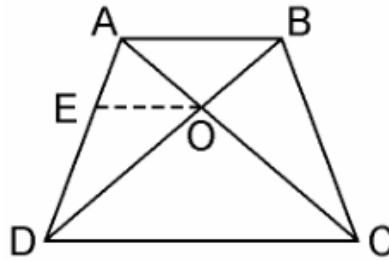
By converse of Basic Proportionality Theorem,

$$DE \parallel BC$$

Hence, proved.

**9. ABCD is a trapezium in which  $AB \parallel DC$  and its diagonals intersect each other at the point O. Show that  $AO/BO = CO/DO$ .**

**Solution:** Given, ABCD is a trapezium where  $AB \parallel DC$  and diagonals AC and BD intersect each other at O.



We have to prove,  $\frac{AO}{BO} = \frac{CO}{DO}$

From the point O, draw a line EO touching AD at E, in such a way that,  
 $EO \parallel DC \parallel AB$

In  $\triangle ADC$ , we have  $OE \parallel DC$

Therefore, By using Basic Proportionality Theorem

$$\frac{AE}{ED} = \frac{AO}{CO} \dots\dots\dots\text{(i)}$$

Now, In  $\triangle ABD$ ,  $OE \parallel AB$

Therefore, By using Basic Proportionality Theorem

$$\frac{DE}{EA} = \frac{DO}{BO} \dots\dots\dots\text{(ii)}$$

From equation (i) and (ii), we get,

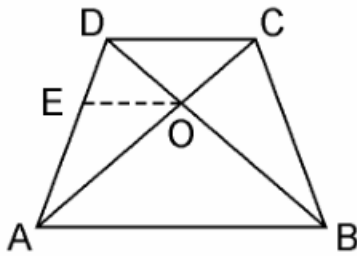
$$\frac{AO}{CO} = \frac{BO}{DO}$$

$$\Rightarrow \frac{AO}{BO} = \frac{CO}{DO}$$

Hence, proved.

**10. The diagonals of a quadrilateral ABCD intersect each other at the point O such that  $AO/BO = CO/DO$ . Show that ABCD is a trapezium.**

**Solution:** Given, Quadrilateral ABCD where AC and BD intersects each other at O such that,  
 $AO/BO = CO/DO$ .



We have to prove here, ABCD is a trapezium

From the point O, draw a line EO touching AD at E, in such a way that,  
EO || DC || AB

In  $\triangle DAB$ , EO || AB

Therefore, By using Basic Proportionality Theorem

$$\frac{DE}{EA} = \frac{DO}{OB} \dots\dots\dots\text{(i)}$$

Also, given,

$$\begin{aligned} \frac{AO}{BO} &= \frac{CO}{DO} \\ \Rightarrow \frac{AO}{CO} &= \frac{BO}{DO} \\ \Rightarrow \frac{DO}{OB} &= \frac{CO}{AO} \dots\dots\dots\text{(ii)} \end{aligned}$$

From equation (i) and (ii), we get

$$\frac{DE}{EA} = \frac{CO}{AO}$$

Therefore, By using converse of Basic Proportionality Theorem,

EO || DC also EO || AB

$\Rightarrow$  AB || DC.

Hence, quadrilateral ABCD is a trapezium with AB || CD.