

EXERCISE 19.2

P&GE NO: 19.11

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1. Find:
(i) 10<sup>th</sup> term of the A.P. 1, 4, 7, 10, .....
(ii) 18<sup>th</sup> term of the A.P. \sqrt{2}, 3\sqrt{2}, 5\sqrt{2}, ...
(iii) nth term of the A.P 13, 8, 3, -2, ....
Solution:
(i) 10<sup>th</sup> term of the A.P. 1, 4, 7, 10, .....
Arithmetic Progression (AP) whose common difference is = a_n - a_{n-1} where n > 0
Let us consider, a = a_1 = 1, a_2 = 4...
So, Common difference, d = a_2 - a_1 = 4 - 1 = 3
To find the 10^{th} term of A.P., firstly find a_n
By using the formula,
a_n = a + (n-1) d
   = 1 + (n-1) 3
   = 1 + 3n - 3
   = 3n - 2
When n = 10:
a_{10} = 3(10) - 2
    = 30 - 2
    = 28
Hence, 10<sup>th</sup> term is 28.
(ii) 18<sup>th</sup> term of the A.P. \sqrt{2}, 3\sqrt{2}, 5\sqrt{2}, ...
Arithmetic Progression (AP) whose common difference is = a_n - a_{n-1} where n > 0
Let us consider, a = a_1 = \sqrt{2}, a_2 = 3\sqrt{2}...
So, Common difference, d = a_2 - a_1 = 3\sqrt{2} - \sqrt{2} = 2\sqrt{2}
To find the 18^{th} term of A.P, firstly find a_n
By using the formula,
a_n = a + (n-1) d
   =\sqrt{2} + (n - 1) 2\sqrt{2}
   =\sqrt{2}+2\sqrt{2n}-2\sqrt{2}
   = 2\sqrt{2n} - \sqrt{2}
When n = 18:
a_{18} = 2\sqrt{2(18)} - \sqrt{2}
    = 36\sqrt{2} - \sqrt{2}
    = 35\sqrt{2}
Hence, 10^{\text{th}} term is 35\sqrt{2}
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(iii) nth term of the A.P 13, 8, 3, -2, Arithmetic Progression (AP) whose common difference is $= a_n - a_{n-1}$ where n > 0Let us consider, $a = a_1 = 13$, $a_2 = 8$... So, Common difference, $d = a_2 - a_1 = 8 - 13 = -5$ To find the nth term of A.P, firstly find a_n By using the formula, $a_n = a + (n-1) d$ = 13 + (n-1) (-5)= 13 - 5n + 5= 18 - 5nHence, nth term is 18 - 5n

2. In an A.P., show that $a_{m+n} + a_{m-n} = 2a_m$. Solution:

We know the first term is 'a' and the common difference of an A.P is d. Given: $a_{m+n} + a_{m-n} = 2a_m$ By using the formula, $a_n = a + (n - 1)d$ Now, let us take LHS: $a_{m+n} + a_{m-n}$ $a_{m+n} + a_{m-n} = a + (m + n - 1)d + a + (m - n - 1)d$ = a + md + nd - d + a + md - nd - d = 2a + 2md - 2d = 2(a + md - d) $= 2[a + d(m - 1)] {:: a_n = a + (n - 1)d}$ $a_{m+n} + a_{m-n} = 2a_m$ Hence Proved.

3. (i) Which term of the A.P. 3, 8, 13,... is 248 ? (ii) Which term of the A.P. 84, 80, 76,... is 0 ? (iii) Which term of the A.P. 4, 9, 14,... is 254 ? Solution: (i) Which term of the A.P. 3, 8, 13,... is 248 ? Given A.P is 3, 8, 13,... Here, $a_1 = a = 3$, $a_2 = 8$ Common difference, $d = a_2 - a_1 = 8 - 3 = 5$ We know, $a_n = a + (n - 1)d$ $a_n = 3 + (n - 1)5$ = 3 + 5n - 5



= 5n - 2

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Now, to find which term of A.P is 248
Put a_n = 248
:.5n - 2 = 248
= 248 + 2
= 250
= 250/5
= 50
Hence, 50<sup>th</sup> term of given A.P is 248.
(ii) Which term of the A.P. 84, 80, 76,... is 0?
Given A.P is 84, 80, 76,...
Here, a_1 = a = 84, a_2 = 88
Common difference, d = a_2 - a_1 = 80 - 84 = -4
We know, a_n = a + (n - 1)d
a_n = 84 + (n-1)-4
  = 84 - 4n + 4
  = 88 - 4n
Now, to find which term of A.P is 0
Put a_n = 0
88 - 4n = 0
-4n = -88
n = 88/4
  = 22
Hence, 22<sup>nd</sup> term of given A.P is 0.
(iii) Which term of the A.P. 4, 9, 14,... is 254?
Given A.P is 4, 9, 14,...
Here, a_1 = a = 4, a_2 = 9
Common difference, d = a_2 - a_1 = 9 - 4 = 5
We know, a_n = a + (n-1)d
a_n = 4 + (n-1)5
  = 4 + 5n - 5
  = 5n - 1
Now, to find which term of A.P is 254
Put a_n = 254
5n - 1 = 254
5n = 254 + 1
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5n = 255n = 255/5= 51 Hence, 51st term of given A.P is 254. 4. (i) Is 68 a term of the A.P. 7, 10, 13,...? (ii) Is 302 a term of the A.P. 3, 8, 13,...? Solution: (i) Is 68 a term of the A.P. 7, 10, 13,...? Given A.P is 7, 10, 13,... Here, $a_1 = a = 7$, $a_2 = 10$ Common difference, $d = a_2 - a_1 = 10 - 7 = 3$ We know, $a_n = a + (n - 1)d$ [where, a is first term or a_1 and d is common difference and n is any natural number] $a_n = 7 + (n-1)3$ = 7 + 3n - 3= 3n + 4Now, to find whether 68 is a term of this A.P. or not Put $a_n = 68$ 3n + 4 = 683n = 68 - 43n = 64n = 64/364/3 is not a natural number Hence, 68 is not a term of given A.P. (ii) Is 302 a term of the A.P. 3, 8, 13,...? Given A.P is 3, 8, 13,... Here, $a_1 = a = 3$, $a_2 = 8$ Common difference, $d = a_2 - a_1 = 8 - 3 = 5$ We know, $a_n = a + (n-1)d$ $a_n = 3 + (n-1)5$ = 3 + 5n - 5= 5n - 2To find whether 302 is a term of this A.P. or not Put $a_n = 302$ 5n - 2 = 3025n = 302 + 25n = 304



n = 304/5 304/5 is not a natural number Hence, 304 is not a term of given A.P.

5. (i) Which term of the sequence 24, 23 ¹/₄, 22 ¹/₂, 21 ³/₄ is the first negative term? Solution:

Given: AP: 24, 23 ¹/₄, 22 ¹/₂, 21 ³/₄, ... = 24, 93/4, 45/2, 87/4, ... Here, $a_1 = a = 24$, $a_2 = 93/4$ Common difference, $d = a_2 - a_1 = 93/4 - 24$ =(93 - 96)/4= - 3/4We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number] We know, $a_n = a + (n - 1) d$ $a_n = 24 + (n - 1)(-3/4)$ $= 24 - 3/4n + \frac{3}{4}$ = (96+3)/4 - 3/4n= 99/4 - 3/4nNow we need to find, first negative term. Put $a_n < 0$ $a_n = 99/4 - 3/4n < 0$ 99/4 < 3/4n3n > 99n > 99/3n > 33Hence, 34th term is the first negative term of given AP.

(ii) Which term of the sequence 12 + 8i, 11 + 6i, 10 + 4i, ... is (a) purely real (b) purely imaginary ? Solution:

Given: AP: 12 + 8i, 11 + 6i, 10 + 4i, ... Here, $a_1 = a = 12 + 8i$, $a_2 = 11 + 6i$ Common difference, $d = a_2 - a_1$ = 11 + 6i - (12 + 8i) = 11 - 12 + 6i - 8i= -1 - 2i

We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n

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is any natural number] $a_n = 12 + 8i + (n - 1) - 1 - 2i$ = 12 + 8i - n - 2ni + 1 + 2i= 13 + 10i - n - 2ni= (13 - n) + (10 - 2n) iTo find purely real term of this A.P., imaginary part have to be zero 10 - 2n = 02n = 10n = 10/2= 5 Hence, 5th term is purely real. To find purely imaginary term of this A.P., real part have to be zero $\therefore 13 - n = 0$ n = 13 Hence, 13th term is purely imaginary. 6. (i) How many terms are in A.P. 7, 10, 13,...43? Solution: Given:

AP: 7, 10, 13,... Here, $a_1 = a = 7$, $a_2 = 10$ Common difference, $d = a_2 - a_1 = 10 - 7 = 3$ We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number] $a_n = 7 + (n - 1)3$ = 7 + 3n - 3 = 3n + 4To find total terms of the A.P., put $a_n = 43$ as 43 is last term of A.P. 3n + 4 = 43 3n = 43 - 4 3n = 39 n = 39/3= 13

Hence, total 13 terms exists in the given A.P.

(ii) How many terms are there in the A.P. -1, -5/6, -2/3, -1/2, ..., 10/3 ? Solution:

Given: AP: -1, -5/6, -2/3, -1/2, ...

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Here, $a_1 = a = -1$, $a_2 = -5/6$ Common difference, $d = a_2 - a_1$ = -5/6 - (-1)= -5/6 + 1=(-5+6)/6= 1/6We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number] $a_n = -1 + (n-1) 1/6$ = -1 + 1/6n - 1/6= (-6-1)/6 + 1/6n= -7/6 + 1/6nTo find total terms of the AP, Put $a_n = 10/3$ [Since, 10/3 is the last term of AP] $a_n = -7/6 + 1/6n = 10/3$ 1/6n = 10/3 + 7/61/6n = (20+7)/61/6n = 27/6n = 27Hence, total 27 terms exists in the given A.P.

7. The first term of an A.P. is 5, the common difference is 3, and the last term is 80; find the number of terms.

Solution:

Given:

First term, a = 5; last term, $l = a_n = 80$

Common difference, d = 3

We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number]

 $a_n = 5 + (n-1)3$ = 5 + 3n - 3

$$= 3n + 2$$

To find total terms of the A.P., put $a_n = 80$ as 80 is last term of A.P.

3n + 2 = 803n = 80 - 2

3n = 78

n = 78/3

Hence, total 26 terms exists in the given A.P.



8. The 6th and 17th terms of an A.P. are 19 and 41 respectively. Find the 40th term. Solution:

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Given:
6<sup>th</sup> term of an A.P is 19 and 17<sup>th</sup> terms of an A.P. is 41
So, a_6 = 19 and a_{17} = 41
We know, a_n = a + (n - 1) d [where a is first term or a_1 and d is common difference and n
is any natural number]
When n = 6:
a_6 = a + (6 - 1) d
  = a + 5d
Similarly, When n = 17:
a_{17} = a + (17 - 1)d
   = a + 16d
According to question:
a_6 = 19 and a_{17} = 41
a + 5d = 19 .....(i)
And a + 16d = 41.....(ii)
Let us subtract equation (i) from (ii) we get,
a + 16d - (a + 5d) = 41 - 19
a + 16d - a - 5d = 22
11d = 22
d = 22/11
  = 2
put the value of d in equation (i):
a + 5(2) = 19
a + 10 = 19
a = 19 - 10
  = 9
As, a_n = a + (n - 1)d
a_{40} = a + (40 - 1)d
   = a + 39d
Now put the value of a = 9 and d = 2 in a_{40} we get,
a_{40} = 9 + 39(2)
   = 9 + 78
   = 87
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Hence, 40th term of the given A.P. is 87.

9. If 9th term of an A.P. is Zero, prove that its 29th term is double the 19th term. Solution:

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Given:
9<sup>th</sup> term of an A.P is 0
So, a_9 = 0
We need to prove: a_{29} = 2a_{19}
We know, a_n = a + (n - 1) d [where a is first term or a_1 and d is common difference and n
is any natural number]
When n = 9:
a_9 = a + (9 - 1)d
  = a + 8d
According to question:
a_9 = 0
a + 8d = 0
a = -8d
When n = 19:
a_{19} = a + (19 - 1)d
   = a + 18d
   = -8d + 18d
   = 10d
When n = 29:
a_{29} = a + (29 - 1)d
   = a + 28d
   = -8d + 28d [Since, a = -8d]
   = 20d
   = 2 \times 10d
a_{29} = 2a_{19} [Since, a_{19} = 10d]
Hence Proved.
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10. If 10 times the 10th term of an A.P. is equal to 15 times the 15th term, show that the 25th term of the A.P. is Zero. Solution:

Given: 10 times the 10th term of an A.P. is equal to 15 times the 15th term So, $10a_{10} = 15a_{15}$



We need to prove: $a_{25} = 0$ We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number] When n = 10: $a_{10} = a + (10 - 1)d$ = a + 9dWhen n = 15: $a_{15} = a + (15 - 1)d$ = a + 14dWhen n = 25: $a_{25} = a + (25 - 1)d$ = a + 24d(i) According to question: $10a_{10} = 15a_{15}$ 10(a + 9d) = 15(a + 14d)10a + 90d = 15a + 210d10a - 15a + 90d - 210d = 0-5a - 120d = 0-5(a + 24d) = 0a + 24d = 0 $a_{25} = 0$ [From (i)] Hence Proved.

11. The 10th and 18th term of an A.P. are 41 and 73 respectively, find 26th term. Solution:

Given: 10^{th} term of an A.P is 41, and 18^{th} terms of an A.P. is 73 So, $a_{10} = 41$ and $a_{18} = 73$ We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is the common difference and n is any natural number] When n = 10: $a_{10} = a + (10 - 1)d$ = a + 9dWhen n = 18: $a_{18} = a + (18 - 1)d$ = a + 17d



According to question: $a_{10} = 41$ and $a_{18} = 73$ a + 9d = 41(i) And a + 17d = 73.....(ii) Let us subtract equation (i) from (ii) we get, a + 17d - (a + 9d) = 73 - 41 a + 17d - a - 9d = 32 8d = 32 d = 32/8d = 4

Put the value of d in equation (i) we get, a + 9(4) = 41 a + 36 = 41 a = 41 - 36 a = 5we know, $a_n = a + (n - 1)d$ $a_{26} = a + (26 - 1)d$ = a + 25dNow put the value of a = 5 and d = 4 in a_{26} $a_{26} = 5 + 25(4)$ = 5 + 100 = 105Hence, 26th term of the given A.P. is 105.

12. In a certain A.P. the 24th term is twice the 10th term. Prove that the 72nd term is twice the 34th term. Solution:

Given: 24^{th} term is twice the 10^{th} term So, $a_{24} = 2a_{10}$ We need to prove: $a_{72} = 2a_{34}$ We know, $a_n = a + (n - 1) d$ [where a is first term or a_1 and d is common difference and n is any natural number] When n = 10: $a_{10} = a + (10 - 1)d$ = a + 9d

When n = 24:



 $a_{24} = a + (24 - 1)d$ = a + 23dWhen n = 34: $a_{34} = a + (34 - 1)d$ = a + 33d(i) When n = 72: $a_{72} = a + (72 - 1)d$ = a + 71dAccording to question: $a_{24} = 2a_{10}$ a + 23d = 2(a + 9d)a + 23d = 2a + 18da - 2a + 23d - 18d = 0-a + 5d = 0a = 5dNow, $a_{72} = a + 71d$ $a_{72} = 5d + 71d$ = 76d = 10d + 66d= 2(5d + 33d)= 2(a + 33d) [since, a = 5d] $a_{72} = 2a_{34}$ (From (i)) Hence Proved.

