

EXERCISE 3.1

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**1. Find the radian measures corresponding to the following degree measures:**(i)  $25^\circ$  (ii)  $-47^\circ 30'$  (iii)  $240^\circ$  (iv)  $520^\circ$ **Solution:**(i)  $25^\circ$ Here  $180^\circ = \pi$  radian

It can be written as

$$25^\circ = \frac{\pi}{180} \times 25 \text{ radian}$$

So we get

$$= \frac{5\pi}{36} \text{ radian}$$

(ii)  $-47^\circ 30'$ Here  $1^\circ = 60'$ 

It can be written as

$$-47^\circ 30' = -47\frac{1}{2} \text{ degree}$$

So we get

$$= \frac{-95}{2} \text{ degree}$$

Here  $180^\circ = \pi$  radian

$$\frac{-95}{2} \text{ degree} = \frac{\pi}{180} \times \left(\frac{-95}{2}\right) \text{ radian}$$

It can be written as

$$= \left(\frac{-19}{36 \times 2}\right) \pi \text{ radian} = \frac{-19}{72} \pi \text{ radian}$$

We get

$$-47^\circ 30' = \frac{-19}{72} \pi \text{ radian}$$

(iii)  $240^\circ$ Here  $180^\circ = \pi$  radian

It can be written as

$$240^\circ = \frac{\pi}{180} \times 240 \text{ radian}$$

So we get

$$= \frac{4}{3} \pi \text{ radian}$$

(iv)  $520^\circ$

Here  $180^\circ = \pi$  radian

It can be written as

$$520^\circ = \frac{\pi}{180} \times 520 \text{ radian}$$

So we get

$$= \frac{26\pi}{9} \text{ radian}$$

**2. Find the degree measures corresponding to the following radian measures (Use  $\pi = 22/7$ )**

(i)  $11/16$

(ii)  $-4$

(iii)  $5\pi/3$

(iv)  $7\pi/6$

**Solution:**

(i)  $11/16$

Here  $\pi$  radian =  $180^\circ$

$$\frac{11}{16} \text{ radian} = \frac{180}{\pi} \times \frac{11}{16} \text{ deg ree}$$

We can write it as

$$= \frac{45 \times 11}{\pi \times 4} \text{ deg ree}$$

So we get

$$= \frac{45 \times 11 \times 7}{22 \times 4} \text{ deg ree}$$

$$= \frac{315}{8} \text{ deg ree}$$

$$= 39\frac{3}{8} \text{ deg ree}$$

Take  $1^\circ = 60'$

$$= 39^\circ + \frac{3 \times 60}{8} \text{ min utes}$$

We get

$$= 39^\circ + 22' + \frac{1}{2} \text{ min utes}$$

Consider  $1' = 60''$

$$= 39^\circ 22' 30''$$

(ii)  $-4$

Here  $\pi$  radian =  $180^\circ$

$$-4 \text{ radian} = \frac{180}{\pi} \times (-4) \text{ deg ree}$$

We can write it as

$$= \frac{180 \times 7(-4)}{22} \text{ deg ree}$$

By further calculation

$$= \frac{-2520}{11} \text{ deg ree} = -229 \frac{1}{11} \text{ deg ree}$$

Take  $1^\circ = 60'$

$$= -229^\circ + \frac{1 \times 60}{11} \text{ min utes}$$

So we get

$$= -229^\circ + 5' + \frac{5}{11} \text{ min utes}$$

Again  $1' = 60''$

$$= -229^\circ 5' 27''$$

(iii)  $5\pi/3$

Here  $\pi \text{ radian} = 180^\circ$

$$\frac{5\pi}{3} \text{ radian} = \frac{180}{\pi} \times \frac{5\pi}{3} \text{ deg ree}$$

We get

$$= 300^\circ$$

(iv)  $7\pi/6$

Here  $\pi \text{ radian} = 180^\circ$

$$\frac{7\pi}{6} \text{ radian} = \frac{180}{\pi} \times \frac{7\pi}{6}$$

We get

$$= 210^\circ$$

**3. A wheel makes 360 revolutions in one minute. Through how many radians does it turn in one second?**

**Solution:**

It is given that

No. of revolutions made by the wheel in

$$1 \text{ minute} = 360$$

$$1 \text{ second} = 360/6 = 60$$

We know that

The wheel turns an angle of  $2\pi$  radian in one complete revolution.

In 6 complete revolutions, it will turn an angle of  $6 \times 2\pi \text{ radian} = 12 \pi \text{ radian}$

Therefore, in one second, the wheel turns an angle of  $12\pi$  radian.

4. Find the degree measure of the angle subtended at the centre of a circle of radius 100 cm by an arc of length 22 cm (Use  $\pi = 22/7$ ).

**Solution:**

Consider a circle of radius  $r$  unit with  $l$  unit as the arc length which subtends an angle  $\theta$  radian at the centre

$$\theta = l/r$$

Here  $r = 100$  cm,  $l = 22$  cm

$$\theta = \frac{22}{100} \text{ radian} = \frac{180}{\pi} \times \frac{22}{100} \text{ deg ree}$$

It can be written as

$$= \frac{180 \times 7 \times 22}{22 \times 100} \text{ deg ree}$$

$$= \frac{126}{10} \text{ deg ree}$$

So we get

$$= 12 \frac{3}{5} \text{ deg ree}$$

$$\text{Here } 1^\circ = 60'$$

$$= 12^\circ 36'$$

Therefore, the required angle is  $12^\circ 36'$ .

5. In a circle of diameter 40 cm, the length of a chord is 20 cm. Find the length of minor arc of the chord.

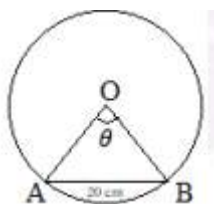
**Solution:**

The dimensions of the circle are

Diameter = 40 cm

Radius =  $40/2 = 20$  cm

Consider AB be as the chord of the circle i.e. length = 20 cm



In  $\triangle OAB$ ,

Radius of circle =  $OA = OB = 20$  cm

Similarly  $AB = 20$  cm

Hence,  $\triangle OAB$  is an equilateral triangle.

$$\theta = 60^\circ = \pi/3 \text{ radian}$$

In a circle of radius  $r$  unit, if an arc of length  $l$  unit subtends an angle  $\theta$  radian at the centre

We get  $\theta = l/r$

$$\frac{\pi}{3} = \frac{\widehat{AB}}{20} \Rightarrow \widehat{AB} = \frac{20\pi}{3} \text{ cm}$$

Therefore, the length of the minor arc of the chord is  $20\pi/3$  cm.

**6. If in two circles, arcs of the same length subtend angles  $60^\circ$  and  $75^\circ$  at the centre, find the ratio of their radii.**

**Solution:**

Consider  $r_1$  and  $r_2$  as the radii of the two circles.

Let an arc of length  $l$  subtend an angle of  $60^\circ$  at the centre of the circle of radius  $r_1$  and an arc of length

$l$  subtend an angle of  $75^\circ$  at the centre of the circle of radius  $r_2$ .

Here  $60^\circ = \pi/3$  radian and  $75^\circ = 5\pi/12$  radian

In a circle of radius  $r$  unit, if an arc of length  $l$  unit subtends an angle  $\theta$  radian at the centre

We get

$$\theta = l/r \text{ or } l = r\theta$$

We know that

$$l = \frac{r_1\pi}{3} \text{ and } l = \frac{r_2 5\pi}{12}$$

By equating both we get

$$\frac{r_1\pi}{3} = \frac{r_2 5\pi}{12}$$

On further calculation

$$r_1 = \frac{r_2 5}{4}$$

So we get

$$\frac{r_1}{r_2} = \frac{5}{4}$$

Therefore, the ratio of the radii is 5: 4.

**7. Find the angle in radian through which a pendulum swings if its length is 75 cm and the tip describes an arc of length**

**(i) 10 cm (ii) 15 cm (iii) 21 cm**

**Solution:**

In a circle of radius  $r$  unit, if an arc of length  $l$  unit subtends an angle  $\theta$  radian at the centre, then  $\theta = l/r$

We know that  $r = 75$  cm

(i)  $l = 10$  cm

So we get

$$\theta = 10/75 \text{ radian}$$

By further simplification

$$\theta = 2/15 \text{ radian}$$

(ii)  $l = 15$  cm

So we get

$$\theta = 15/75 \text{ radian}$$

By further simplification

$$\theta = 1/5 \text{ radian}$$

(iii)  $l = 21$  cm

So we get

$$\theta = 21/75 \text{ radian}$$

By further simplification

$$\theta = 7/25 \text{ radian}$$

