

# **EXERCISE 18.1**

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Find the maximum and the minimum values, if any, without using derivatives of the following functions:

1. 
$$f(x) = 4x^2 - 4x + 4$$
 on R

# **Solution:**

Given f (x) = 
$$4x^2 - 4x + 4$$
 on R

$$=4x^2-4x+1+3$$

By grouping the above equation we get,

$$=(2x-1)^2+3$$

Since, 
$$(2x - 1)^2 \ge 0$$

$$= (2x - 1)^2 + 3 \ge 3$$

$$= f(x) \ge f(\frac{1}{2})$$

Thus, the minimum value of f(x) is 3 at  $x = \frac{1}{2}$ 

Since, f(x) can be made large. Therefore maximum value does not exist.

2. 
$$f(x) = -(x-1)^2 + 2$$
 on R

## **Solution:**

Given 
$$f(x) = -(x-1)^2 + 2$$

It can be observed that  $(x-1)^2 \ge 0$  for every  $x \in R$ 

Therefore,  $f(x) = -(x-1)^2 + 2 \le 2$  for every  $x \in R$ 

The maximum value of f is attained when (x - 1) = 0

$$(x-1) = 0, x = 1$$

Since, Maximum value of  $f = f(1) = -(1-1)^2 + 2 = 2$ 

Hence, function f does not have minimum value.

3. 
$$f(x) = |x + 2|$$
 on R

#### **Solution:**

Given 
$$f(x) = |x + 2| \ge 0$$
 for  $x \in R$ 

$$= f(x) \ge 0$$
 for all  $x \in R$ 

So the minimum value of f(x) is 0, which attains at x = 2

Hence, f(x) = |x + 2| does not have the maximum value.



4. 
$$f(x) = \sin 2x + 5$$
 on R

# **Solution:**

Given f (x) =  $\sin 2x + 5$  on R We know that  $-1 \le \sin 2x \le 1$ =  $-1 + 5 \le \sin 2x + 5 \le 1 + 5$ =  $4 \le \sin 2x + 5 \le 6$ 

Hence, the maximum and minimum value of h are 4 and 6 respectively.

5. 
$$f(x) = |\sin 4x + 3|$$
 on R

## **Solution:**

Given f (x) =  $|\sin 4x + 3|$  on R We know that  $-1 \le \sin 4x \le 1$ =  $2 \le \sin 4x + 3 \le 4$ =  $2 \le |\sin 4x + 3| \le 4$ 

Hence, the maximum and minimum value of f are 4 and 2 respectively.