

EXERCISE 6A

1 quintal = 100 kg

We get

Express each of the given ratios in its simplest form:
 (i) 22: 66
 (ii) 1.5: 2.5
 (iii) 6 1/4: 12 1/2
 (iv) 40 kg: 1 quintal
 (v) 10 paise: ₹ 1
 (vi) 200 m: 5 km
 (vii) 3 hours: 1 day
 (viii) 6 months: 1 1/3 years
 (ix) 1 1/3: 2 1/4: 2 1/2
 Solution:

(i) 22: 66 It can be written as = 22/66We know that the HCF of 22 and 66 is 22 Dividing both numerator and denominator by 22 $=(22 \div 22)/(66 \div 22)$ So we get = 1/3 = 1: 3 (ii) 1.5: 2.5 It can be written as = 1.5/2.5Multiplying both numerator and denominator by 10 = 15/25We know that the HCF of 15 and 25 is 5 Dividing both numerator and denominator by 5 $=(15 \div 5)/(25 \div 5)$ So we get = 3/5= 3: 5 (iii) 6 1/4: 12 1/2 It can be written as = 25/4: 25/2 $= 25/4 \times 2/25$ By further calculation = 2/4So we get = 1/2= 1: 2 (iv) 40 kg: 1 quintal We know that

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= 40 kg: 100 kg It can be written as = 40/100We know that the HCF of 40 and 100 is 20 Dividing both numerator and denominator by 20 $= (40 \div 20)/(100 \div 20)$ So we get = 2/5= 2: 5 (v) 10 paise: ₹ 1 We know that 1 Rupee = 100 PaiseWe get = 10 paise: 100 paise It can be written as = 10/100So we get = 1/10= 1: 10 (vi) 200 m: 5 km We know that 1 km = 1000 mWe get = 200 m: 5000 m It can be written as = 200/5000Here the HCF of 200 and 5000 is 200 Dividing both numerator and denominator by 200 $=(200 \div 200)/(5000 \div 200)$ So we get = 1/25= 1: 25 (vii) 3 hours: 1 day We know that 1 day = 24 hoursWe get = 3 hours: 24 hours It can be written as = 3/24So we get = 1/8= 1:8(viii) 6 months: 1 1/3 years We know that 1 year = 12 monthsWe get



= 6 months: $4/3 \times 12$ months It can be written as = 6 months: 16 months = 6/16 Here the HCF of 6 and 16 is 2 Dividing both numerator and denominator by 2 = $(6 \div 2)/(16 \div 2)$ So we get = 3/8= 3:8

(ix) 1 1/3: 2 1/4: 2 1/2 It can be written as = 4/3: 9/4: 5/2 We know that the LCM of 3, 4 and 2 is 12 = (16: 27: 30)/ 12 So we get = 16: 27: 30

2. Divide 64 cm long string into two parts in the ratio 5: 3. Solution:

We know that The sum of ratios = 5 + 3 = 8So the first part = 5/8 of 64 cm = 40 cm Similarly the second part = 3/8 of 64 cm = 24 cm

3. ₹ 720 is divided between x and y in the ratio 4: 5. How many rupees will each get? Solution:

It is given that Total amount = ₹ 720 Ratio between x and y = 4: 5 We know that The sum of ratios = 4 + 5 = 9So x's share = 4/9 of ₹ 720 = ₹ 320 Similarly y's share = 5/9 of ₹ 720 = ₹ 400

4. The angles of a triangle are in the ratio 3: 2: 7. Find each angle. Solution:

It is given that Ratios in angles of a triangle = 3: 2: 7 We know that The sum of ratios = 3 + 2 + 7 = 12In a triangle, the sum of all the angles = 180° So the first angle of the triangle = $3/12 \times 180^{\circ} = 45^{\circ}$ Second angle of the triangle = $2/12 \times 180^{\circ} = 30^{\circ}$ Similarly the third angle of the triangle = $7/12 \times 180^{\circ} = 105^{\circ}$



5. A rectangular field is 100 m by 80 m. Find the ratio of:
(i) length to its breadth
(ii) breadth to its perimeter.
Solution:

It is given that Length of the rectangular field = 100 m Breadth of the rectangular field = 80 m So the perimeter = 2 (length + breadth) = 2 (100 + 80) m By further calculation = 2×180 = 360 m (i) Ratio of length to its breadth

= 100: 80 Here the HCF of 100 and 80 is 20 Dividing both numerator and denominator by 20 = $(100 \div 20)/(80 \div 20)$ So we get = 5/4= 5: 4

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(ii) Ratio of breadth to its perimeter
= 80: 360
Here the HCF of 80 and 360 is 40
Dividing both numerator and denominator by 40
= (80 \div 40)/(360 \div 40)
So we get
= 2/9
= 2: 9
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6. The sum of three numbers, whose ratios are 3 1/3: 4 1/5: 6 1/8 is 4917. Find the numbers. Solution:

It is given that Sum of three numbers = 4917Ratio between the three numbers = $3 \ 1/3$: $4 \ 1/5$: $6 \ 1/8$ It can be written as = 10/3: 21/5: 49/8We know that the LCM of 3, 5 and 8 is 120= (400: 504: 735)/120So we get = 400: 504: 735

Here the sum of ratio = 400 + 504 + 735 = 1639So the first number = 400/1639 of 4917 = 1200Second number = 504/1639 of 4917 = 1512Similarly the third number = 735/1639 of 4917 = 2205



7. The ratio between two quantities is 3: 4. If the first is ₹ 810, find the second. Solution:

It is given that The ratio between two quantities = 3: 4 So the sum of ratio = 3 + 4 = 7Here the second quantity = $(810 \times 4)/3$ We get = 270×4 = ₹ 1080

8. Two numbers are in the ratio **5**: **7**. Their difference is **10**. Find the numbers. Solution:

It is given that The ratio between two numbers = 5: 7 The difference between two numbers = 7 - 5 = 2Here if 2 is the difference, the first number is 5 Similarly if 10 if the difference, the first number = $5/2 \times 10 = 25$ Second number = $7/2 \times 10 = 35$

9. Two numbers are in the ratio 10: 11. Their sum is 168. Find the numbers. Solution:

It is given that The ratio between two numbers = 10: 11 Sum of ratio between two numbers = 10 + 11 = 21Sum of two numbers = 168So the first number = $168/21 \times 10 = 80$ Similarly the second number = $168/21 \times 11 = 88$

10. A line is divided into two parts in the ratio 2.5: 1.3. If the smaller one is 35.1 cm, find the length of the line. Solution:

It is given that Ratio between two parts of a line = 2.5: 1.3 Multiplying by 10 = 25: 13 Here the sum of ratios = 25 + 13 = 38Length of smaller one = 35.1 cm So the length of the line = $38/13 \times 35.1$ We get = 38×2.7 cm = 102.6 cm

11. In a class, the ratio of boys to the girls is 7:8. What part of the whole class are girls? Solution:

It is given that



Ratio of boys to the girls = 7: 8 Here the sum of ratios = 7 + 8 = 15So the part of the whole class are girls = 8/15

Hence, 8/15 part of the whole class are girls.

12. The population of a town is 180,000, out of which males are 1/3 of the whole population. Find the number of females. Also, find the ratio of the number of females to the whole population. Solution:

It is given that Total population = 180000So the population of males = 1/3 of 180000 = 60,000Similarly the population of females = 180000 - 60000 = 120000Here the ratio of females to whole population = 120000: 180000 = 2: 3

13. Ten gram of an alloy of metals A and B contains 7.5 gm of metal A and the rest is metal B. Find the ratio between:

(i) the weights of metals A and B in the alloy.(ii) the weight of metal B and the weight of the alloy.Solution:

We know that Total weight of A and B metals = 10 gm A weight - 7.5 gm B weight So we get = 10 - 7.5 = 2.5 gm (i) Ratio between the weight of A and B in the alloy = 7.5: 2.5 It can be written as = 75/10: 25/10 So we get = 3: 1 (ii) Ratio between the weight of metal B and the weight of the alloy = 2.5: 10 It can be written as

= 25/10: 10 So we get = 25: 100 = 1: 4

14. The ages of two boys A and B are 6 years and 8 months and 7 years and 4 months respectively. Divide ₹ 3,150 in the ratio of their ages. Solution:

It is given that Age of A = 6 years 8 months It can be written as = $6 \times 12 + 8$ = 72 + 8



= 80 months Age of B = 7 years 4 months It can be written as = $7 \times 12 + 4$ = 84 + 4= 88 months So the ratio between them = 80: 88 = 10: 11Amount = ₹ 3150We know that Sum of ratio between them = 10 + 11 = 21Here A share = $(3150 \times 10)/21 = ₹ 1500$ Similarly B share = $(3150 \times 11)/21 = ₹ 1650$

15. Three persons start a business and spend ₹ 25,000, ₹ 15,000 and ₹ 40,000 respectively. Find the share of each out of a profit of ₹ 14,400 in a year. Solution:

It is given that Investment of $A = \overline{2} 25000$ Investment of $B = \overline{2} 15000$ Investment of $C = \overline{2} 40000$ Here the ratio between their investment = 25000: 15000: 40000 = 5: 3: 8 So the sum of ratios = 5 + 3 + 8 = 16Total profit = $\overline{2} 14400$ Share of $A = 14400/16 \times 5 = \overline{2} 4500$ Share of $B = 14400/16 \times 3 = \overline{2} 2700$ Share of $C = 14400/16 \times 8 = \overline{2} 7200$

16. A plot of land, 600 sq m in area, is divided between two persons such that the first person gets threefifths of what the second gets. Find the share of each. Solution:

It is given that Area of plot of land = 600 sq m Consider second share = x So first share = 3/5 xHere the ratio between them = 3/5x: x We get = 3/5: 1 = 3: 5 Sum of the ratio between them = 3 + 5 = 8So the share of first person = $600/8 \times 3 = 225$ sq m Similarly the share of second person = $600/8 \times 5 = 375$ sq m

17. Two poles of different heights are standing vertically on a horizontal field. At a particular time, the ratio between the lengths of their shadows is 2: 3. If the height of the smaller pole is 7.5 m, find the height of the other pole. Solution:

It is given that



Ratio between the shadows of two poles = 2: 3 We know that the height of smaller pole = 7.5 m So the height of taller pole = $(7.5 \times 3)/2$ On further calculation = 22.5/2 = 11.25 m

18. Two numbers are in the ratio **4**: **7**. If their L.C.M. is **168**, find the numbers. Solution:

It is given that Ratio between two numbers = 4: 7 LCM of two numbers = 168 Consider first number = 4x Second number = 7x Now the LCM of 4x and $7x = 4 \times 7 \times x = 28x$ By equating both the values 28x = 168So we get x = 168/28 = 6So the required numbers $4x = 4 \times 6 = 24$ $7x = 7 \times 6 = 42$

19. ₹ 300 is divided between A and B in such a way that A gets half of B. Find:
(i) the ratio between the shares of A and B.
(ii) the share of A and the share of B.
Solution:

Amount divided between A and B = 300

(i) We know that A gets half of B So the ratio between the shares of A and $B = \frac{1}{2} = 1:2$

(ii) We know that Sum of the ratios = 1 + 2 = 3Share of A = $(300 \times 1)/3 = ₹100$ Share of B = $(300 \times 2)/3 = ₹200$

20. The ratio between two numbers is **5**: **9**. Find the numbers, if their H.C.F. is **16**. Solution:

Consider first number = 5xSecond number = 9xWe know that HCF of 5x and 9x = LCM of 5x and 9x = xSo HCF = 16Here x = 16We get the required numbers $5x = 5 \times 16 = 80$



 $9x = 9 \times 16 = 144$

21. A bag contains ₹ 1,600 in the form of ₹ 10 and ₹ 20 notes. If the ratio between the numbers of ₹ 10 and ₹ 20 notes is 2: 3; find the total number of notes in all. Solution:

Amount in the bag = $\gtrless 1,600$ The bag has notes in the denomination of \gtrless 10 and \gtrless 20 So the ratio between the number of $\gtrless 10$ and $\gtrless 20$ notes = 2: 3 Consider the number of $\gtrless 10$ notes = x Number of \gtrless 20 notes = y Using the condition $10x + 20y = 1600 \dots (1)$ $x = 2/3 y \dots (2)$ By substituting the value of x in equation (1) $10 \times 2/3$ y + 20y = 1600 On further calculation 20/3y + 30y = 1600By taking LCM (20 + 60)/3 y = 1600We get 80/3 y = 1600We can write it as $v = (1600 \times 3)/80$ y = 60Substituting the value of y in equation (2) $x = 2/3 \times 60 = 40$ So the total number of notes in all = x + y= 60 + 40= 100 notes

22. The ratio between the prices of a scooter and a refrigerator is 4: 1. If the scooter costs ₹ 45,000 more than the refrigerator, find the price of the refrigerator. Solution:

It is given that Ratio between the prices of a scooter and a refrigerator = 4: 1 Cost of scooter = ₹ 45,000 Consider the cost of scooter = 4x Cost of refrigerator = 1x Using the condition Cost of scooter > Cost of refrigerator 4x - 1x = 45000On further calculation 3x = 45000So we get x = 45000/3 = ₹ 15000So the price of refrigerator = ₹ 15000



EXERCISE 6B

Check whether the following quantities form a proportion or not:
 (i) 3x, 7x, 24 and 56
 (ii) 0.8, 3, 2.4 and 9
 (iii) 1 ¹/₂, 3 ¹/₄, 4 1/2 and 9 ³/₄
 (iv) 0.4, 0.5, 2.9 and 3.5
 (v) 2 ¹/₂, 5 ¹/₂, 3.0 and 6.0
 Solution:

(i) 3x, 7x, 24 and 56 If the quantities are in proportion $3x \times 56 = 7x \times 24$ By further calculation 168x = 168x which is true Therefore, 3x, 7x, 24 and 56 are in proportion.

(ii) 0.8, 3, 2.4 and 9 If the quantities are in proportion $0.8 \times 9 = 3 \times 2.4$ By further calculation 7.2 = 7.2 which is true Therefore, 0.8, 3, 2.4 and 9 are in proportion.

(iii) $1 \frac{1}{2}$, $3 \frac{1}{4}$, $4 \frac{1}{2}$ and $9 \frac{3}{4}$ If the quantities are in proportion $1 \frac{1}{2} \times 9 \frac{3}{4} = 3 \frac{1}{4} \times 4 \frac{1}{2}$ By further calculation $3/2 \times 39/4 = 13/4 \times 9/2$ 117/8 = 117/8 which is true Therefore, $1 \frac{1}{2}$, $3 \frac{1}{4}$, $4 \frac{1}{2}$ and $9 \frac{3}{4}$ are in proportion.

(iv) 0.4, 0.5, 2.9 and 3.5 If the quantities are in proportion $0.4 \times 3.5 = 0.5 \times 2.9$ By further calculation 1.40 = 1.45 which is not true Therefore, 0.4, 0.5, 2.9 and 3.5 are not in proportion.

(v) $2\frac{1}{2}$, $5\frac{1}{2}$, 3.0 and 6.0If the quantities are in proportion $2\frac{1}{2} \times 6.0 = 5\frac{1}{2} \times 3.0$ By further calculation $5/2 \times 6.0 = 11/2 \times 3.0$ 30/2 = 33/2 which is not true Therefore, $2\frac{1}{2}$, $5\frac{1}{2}$, 3.0 and 6.0 are not in proportion.

2. Find the fourth proportional of:
(i) 3, 12 and 4
(ii) 5, 9 and 45

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(iii) 2.1, 1.5 and 8.4
(iv) 1/3, 2/5 and 8.4
(v) 4 hours 40 minutes, 1 hour 10 minutes and 16 hours Solution:

(i) 3, 12 and 4 Here the 4^{th} proportional = $(12 \times 4)/3 = 16$

(ii) 5, 9 and 45 Here the 4^{th} proportional = $(9 \times 45)/5 = 81$

(iii) 2.1, 1.5 and 8.4 Here the 4th proportional = $(1.5 \times 8.4)/2.1 = 1.5 \times 4 = 6.0$

(iv) 1/3, 2/5 and 8.4 Here the 4th proportional = $(2/5 \times 8.4)/1/3$ By further calculation = $2/5 \times 8.4 \times 3/1$ So we get = $(2 \times 84 \times 3)/(5 \times 10 \times 1)$ = 252/25= 10.08

(v) 4 hours 40 minutes, 1 hour 10 minutes and 16 hours It can be written as 4 hours 40 minutes = $4 \times 60 + 40 = 240 + 40 = 280$ minutes 1 hour 10 minutes = $1 \times 60 + 10 = 60 + 10 = 70$ minutes 16 hours = $16 \times 60 = 960$ minutes So the fourth proportional = $(70 \times 960)/280 = 240$ minutes We get = 240/60= 4 hours

3. Find the third proportional of:
(i) 27 and 9
(ii) 2 m 40 cm and 40 cm
(iii) 1.8 and 0.6
(iv) 1/7 and 3/14
(v) 1.6 and 0.8
Solution:

(i) 27 and 9 Here the 3^{rd} proportional = $(9 \times 9)/27 = 3$

(ii) 2 m 40 cm and 40 cm It can be written as 240 cm and 40 cm Here the 3^{rd} proportional = $(40 \times 40)/240 = 20/3 = 62/3$ cm

(iii) 1.8 and 0.6



Here the 3^{rd} proportional = (0.6 × 0.6)/ 1.8 = 0.36/ 1.8 Multiplying by 100 = 36/ 180 So we get = 1/5= 0.2(iv) 1/7 and 3/14 Here the 3^{rd} proportional = $(3/14 \times 3/14)/1/7$ By further calculation $= 9/196 \times 7/1$ So we get = 9/28(v) 1.6 and 0.8 Here the 3^{rd} proportional = $(0.8 \times 0.8)/1.6 = 0.64/1.6$ By further calculation = 64/160= 2/5= 0.44. Find the mean proportional between:

(i) 16 and 4 (ii) 3 and 27 (iii) 0.9 and 2.5 (iv) 0.6 and 9.6

(v) ¼ and 1/16 Solution:

(i) 16 and 4 Here the mean proportional between them = $\sqrt{(16 \times 4)}$ By multiplication = $\sqrt{64}$ = 8

(ii) 3 and 27 Here the mean proportional between them = $\sqrt{(3 \times 27)}$ By multiplication = $\sqrt{81}$ = 9

(iii) 0.9 and 2.5 Here the mean proportional between them = $\sqrt{(0.9 \times 2.5)}$ Multiplying and dividing by 10 = $\sqrt{(9/10 \times 25/10)}$ So we get = $\sqrt{225/100}$



= 15/10= 1.5

(iv) 0.6 and 9.6 Here the mean proportional between them $= \sqrt{(0.6 \times 9.6)}$ Multiplying and dividing by 10 $= \sqrt{6/10 \times 96/10}$ So we get $= \sqrt{576/100}$ = 24/10= 2.4(v) ¹/₄ and 1/16 Here the mean proportional between them

Here the mean proportional between them = $\sqrt{(1/4 \times 1/16)}$ So we get = $\sqrt{1/64}$ = 1/8

5. (i) If A: B = 3: 5 and B: C = 4: 7, find A: B: C. (ii) If A: B = 3: 5 and y: z = 5: 7, find x: y: z. (iii) If m: n = 4: 9 and n: s = 3: 7, find m: s. (iv) If P: Q = $\frac{1}{2}$: 1/3 and Q: R = 1 $\frac{1}{2}$: 1 1/3, find P: R. (v) If a: b = 1.5: 3.5 and b: c = 5: 6, find a: c. (vi) If 1 $\frac{1}{4}$: 2 1/3 = p: q and q: r = 4 $\frac{1}{2}$: 5 $\frac{1}{4}$, find p: r. Solution:

(i) A: B = 3: 5Now divide by 5 = 3/5: 1 Similarly B: C = 4: 7 Now divide by 4 = 1: 7/4 So we get A: B: C = 3/5: 1: 7/4 Multiplying by $5 \times 4 = 20$ A: B: C = 12: 20: 35 (ii) x: y = 2: 3Now divide by 3 = 2/3: 1Similarly y: z = 5: 7 Now divide by 5 = 1: 7/5 So we get x: y: z = 2/3: 1: 7/5 Multiplying by $3 \times 5 = 15$



x: y: z = 10: 15: 21 (iii) m: n = 4: 9We can write it as m/n = 4/9Similarly n: s = 3: 7We can write it as n/s = 3/7So we get $m/n \times n/s = 4/9 \times 3/7$ Here m/s = 4/21m: s = 4: 21 (iv) P: Q = 1/2: 1/3It can be written as $P/Q = 1/2 \times 3/1 = 3/2$ Similarly Q: R = 1 1/2: 1 1/3 = 3/2: 4/3 It can be written as $Q/R = 3/2 \times 3/4 = 9/8$ So we get $P/Q \times Q/R = 3/2 \times 9/8$ P/R = 27/16P: R = 27: 16 (v) a: b = 1.5: 3.5 It can be written as a/b = 1.5/ 3.5 = 15/35 = 3/7 We know that b: c = 5: 6It can be written as b/c = 5/6So we get $a/b \times b/c = 3/7 \times 5/6$ By further calculation a/c = 5/14a: c = 5: 14 (vi) p: $q = 1 \frac{1}{4}: 2 \frac{1}{3}$ We can write it as = 5/4: 7/3 We get $p/q = 5/4 \times 3/7 = 15/28$ Similarly q: r = 4 1/2: 5 1/4 = 9/2: 21/4We can write it as $q/r = 9/2 \times 4/21 = 6/7$ So we get $p/q \times q/r = 15/28 \times 6/7$

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p/r = 45/98 p: r = 45: 98

6. If x: y = 5: 4 and 2: x = 3: 8, find the value of y. Solution:

It is given that x: y = 5: 4 and 2: x = 3: 8 We can write it as x/y = 5/4 (1) 2/x = 3/8 (2) $x = (2 \times 8)/3 = 16/3$ Substituting the value of x in equation (1) x/y = 5/4We get $y = x \times 4/5$ $y = 16/3 \times 4/5 = 64/15 = 44/15$

7. Find the value of x, when 2.5: 4 = x: 7.5. Solution:

It is given that 2.5: 4:: x: 7.5 We can write it as $4 \times x = 2.5 \times 7.5$ $x = (2.5 \times 7.5)/4$ Now multiplying by 100 $x = (25 \times 75)/(4 \times 100)$ By further calculation $x = 75/16 = 4 \ 11/16$

8. Show that 2, 12 and 72 are in continued proportion. Solution:

Consider a, b and c as the three numbers in continued proportion where a: b:: b: c So the numbers are 2, 12 and 72 a/b = 2/12 = 1/6b/c = 12/72 = 1/6We get a/b = b/c

Hence, 2, 12 and 72 are in continued proportion.

