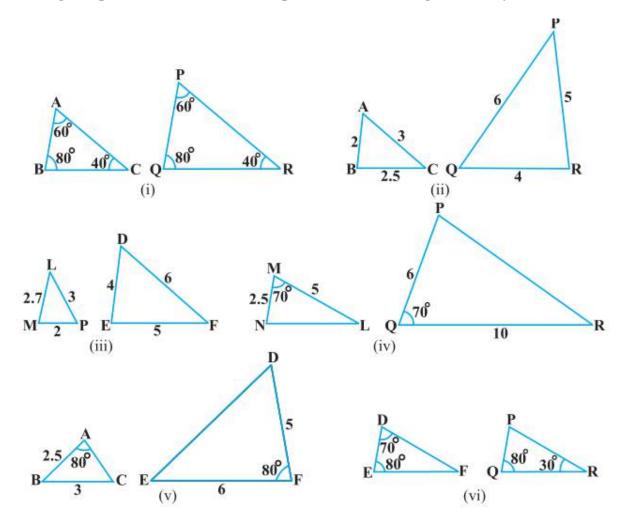


Exercise 6.3

Page: 138

1. State which pairs of triangles in Figure, are similar. Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



Solution:

(i) Given, in $\triangle ABC$ and $\triangle PQR$, $\angle A = \angle P = 60^{\circ}$ $\angle B = \angle Q = 80^{\circ}$ $\angle C = \angle R = 40^{\circ}$ Therefore by AAA similarity criterion, $\therefore \triangle ABC \sim \triangle PQR$

(ii) Given, in $\triangle ABC$ and $\triangle PQR$,



AB/QR = BC/RP = CA/PQ

By SSS similarity criterion, $\Delta ABC \sim \Delta QRP$

(iii) Given, in Δ LMP and Δ DEF,

LM = 2.7, MP = 2, LP = 3, EF = 5, DE = 4, DF = 6 MP/DE = 2/4 = 1/2PL/DF = 3/6 = 1/2LM/EF = 2.7/5 = 27/50Here , MP/DE = PL/DF \neq LM/EF

Therefore, Δ LMP and Δ DEF are not similar.

(iv) In Δ MNL and Δ QPR, it is given, MN/QP = ML/QR = 1/2 \angle M = \angle Q = 70° Therefore, by SAS similarity criterion $\therefore \Delta$ MNL $\sim \Delta$ QPR

(v) In $\triangle ABC$ and $\triangle DEF$, given that, AB = 2.5, BC = 3, $\angle A = 80^{\circ}$, EF = 6, DF = 5, $\angle F = 80^{\circ}$ Here, AB/DF = 2.5/5 = 1/2And, BC/EF = 3/6 = 1/2 $\Rightarrow \angle B \neq \angle F$ Hence, $\triangle ABC$ and $\triangle DEF$ are not similar.

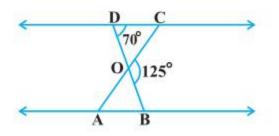
(vi) In $\triangle DEF$, by sum of angles of triangles, we know that, $\angle D + \angle E + \angle F = 180^{\circ}$ $\Rightarrow 70^{\circ} + 80^{\circ} + \angle F = 180^{\circ}$ $\Rightarrow \angle F = 180^{\circ} - 70^{\circ} - 80^{\circ}$ $\Rightarrow \angle F = 30^{\circ}$

Similarly, In $\triangle PQR$, $\angle P + \angle Q + \angle R = 180$ (Sum of angles of \triangle) $\Rightarrow \angle P + 80^{\circ} + 30^{\circ} = 180^{\circ}$ $\Rightarrow \angle P = 180^{\circ} - 80^{\circ} - 30^{\circ}$ $\Rightarrow \angle P = 70^{\circ}$

Now, comparing both the triangles, ΔDEF and ΔPQR , we have $\angle D = \angle P = 70^{\circ}$ $\angle F = \angle Q = 80^{\circ}$ $\angle F = \angle R = 30^{\circ}$ Therefore, by AAA similarity criterion, Hence, $\Delta DEF \sim \Delta PQR$



2. In the figure, $\triangle ODC \propto \frac{1}{4} \triangle OBA$, $\angle BOC = 125^{\circ}$ and $\angle CDO = 70^{\circ}$. Find $\angle DOC$, $\angle DCO$ and $\angle OAB$.



Solution:

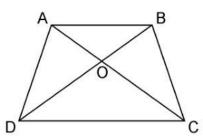
As we can see from the figure, DOB is a straight line. Therefore, $\angle DOC + \angle COB = 180^{\circ}$ $\Rightarrow \angle DOC = 180^{\circ} - 125^{\circ}$ (Given, $\angle BOC = 125^{\circ}$) $= 55^{\circ}$

In $\triangle DOC$, Sum of the measures of the angles of a triangle is 180° Therefore, $\angle DCO + \angle CDO + \angle DOC = 180^{\circ}$ $\Rightarrow \angle DCO + 70^{\circ} + 55^{\circ} = 180^{\circ}$ (Given, $\angle CDO = 70^{\circ}$) $\Rightarrow \angle DCO = 55^{\circ}$

It is given that, $\triangle ODC \propto \frac{1}{4} \triangle OBA$, Therefore, $\triangle ODC \sim \triangle OBA$. Hence, Corresponding angles are equal in similar triangles $\angle OAB = \angle OCD$ $\Rightarrow \angle OAB = 55^{\circ}$ $\angle OAB = \angle OCD$ $\Rightarrow \angle OAB = 55^{\circ}$

3. Diagonals AC and BD of a trapezium ABCD with AB || DC intersect each other at the point O. Using a similarity criterion for two triangles, show that AO/OC = OB/OD

Solution:



In $\triangle DOC$ and $\triangle BOA$, AB || CD, thus alternate interior angles will be equal,



 $\therefore \angle CDO = \angle ABO$ Similarly, $\angle DCO = \angle BAO$ Also, for the two triangles $\triangle DOC$ and $\triangle BOA$, vertically opposite angles will be equal; $\therefore \angle DOC = \angle BOA$

Hence, by AAA similarity criterion, $\Delta DOC \sim \Delta BOA$ Thus, the corresponding sides are proportional. DO/BO = OC/OA $\Rightarrow OA/OC = OB/OD$

Hence, proved.

4. In the fig.6.36, QR/QS = QT/PR and $\angle 1 = \angle 2$. Show that $\triangle PQS \sim \triangle TQR$.

Q 1 2 R

Solution:

In $\triangle PQR$, $\angle PQR = \angle PRQ$ $\therefore PQ = PR$ (i) Given, QR/QS = QT/PRUsing equation (i), we get QR/QS = QT/QP....(ii)

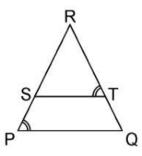
In $\triangle PQS$ and $\triangle TQR$, by equation (ii), QR/QS = QT/QP $\angle Q = \angle Q$ $\therefore \triangle PQS \sim \triangle TQR$ [By SAS similarity criterion]

5. S and T are point on sides PR and QR of \triangle PQR such that \angle P = \angle RTS. Show that \triangle RPQ ~ \triangle RTS.

Solution:



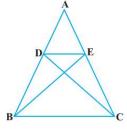
Given, S and T are point on sides PR and QR of \triangle PQR And \angle P = \angle RTS.



In $\triangle RPQ$ and $\triangle RTS$, $\angle RTS = \angle QPS$ (Given) $\angle R = \angle R$ (Common angle) $\therefore \triangle RPQ \sim \triangle RTS$ (AA similarity criterion)



6. In the figure, if $\triangle ABE \cong \triangle ACD$, show that $\triangle ADE \sim \triangle ABC$.



Solution:

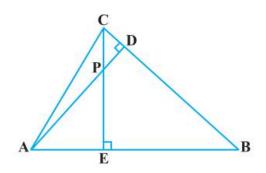
Given, $\triangle ABE \cong \triangle ACD$. $\therefore AB = AC [By CPCT]$(i) And, AD = AE [By CPCT].....(ii)

In $\triangle ADE$ and $\triangle ABC$, dividing eq.(ii) by eq(i), AD/AB = AE/AC $\angle A = \angle A$ [Common angle]

 $\therefore \Delta ADE \sim \Delta ABC \text{ [SAS similarity criterion]}$

7. In the figure, altitudes AD and CE of ΔABC intersect each other at the point P. Show that:

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(i) $\triangle AEP \sim \triangle CDP$ (ii) $\triangle ABD \sim \triangle CBE$ (iii) $\triangle AEP \sim \triangle ADB$ (iv) $\triangle PDC \sim \triangle BEC$

Solution:

Given, altitudes AD and CE of \triangle ABC intersect each other at the point P.

(i) In $\triangle AEP$ and $\triangle CDP$, $\angle AEP = \angle CDP$ (90° each) $\angle APE = \angle CPD$ (Vertically opposite angles) Hence, by AA similarity criterion, $\triangle AEP \sim \triangle CDP$

(ii) In $\triangle ABD$ and $\triangle CBE$, $\angle ADB = \angle CEB$ (90° each) $\angle ABD = \angle CBE$ (Common Angles) Hence, by AA similarity criterion, $\triangle ABD \sim \triangle CBE$

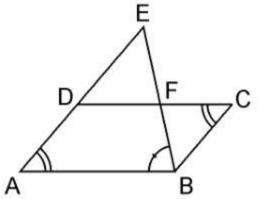
(iii) In $\triangle AEP$ and $\triangle ADB$, $\angle AEP = \angle ADB$ (90° each) $\angle PAE = \angle DAB$ (Common Angles) Hence, by AA similarity criterion, $\triangle AEP \sim \triangle ADB$ (iv) In $\triangle PDC$ and $\triangle BEC$, $\angle PDC = \angle BEC$ (90° each) $\angle PCD = \angle BCE$ (Common angles) Hence, by AA similarity criterion, $\triangle PDC \sim \triangle BEC$

8. E is a point on the side AD produced of a parallelogram ABCD and BE intersects CD at F. Show that $\triangle ABE \sim \triangle CFB$.

Solution:

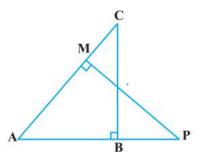


Given, E is a point on the side AD produced of a parallelogram ABCD and BE intersects CD at F. Consider the figure below,



In $\triangle ABE$ and $\triangle CFB$, $\angle A = \angle C$ (Opposite angles of a parallelogram) $\angle AEB = \angle CBF$ (Alternate interior angles as $AE \parallel BC$) $\therefore \triangle ABE \sim \triangle CFB$ (AA similarity criterion)

9. In the figure, ABC and AMP are two right triangles, right angled at B and M respectively, prove that:



(i) $\triangle ABC \sim \triangle AMP$ (ii) CA/PA = BC/MP

Solution:

Given, ABC and AMP are two right triangles, right angled at B and M respectively.

(i) In $\triangle ABC$ and $\triangle AMP$, we have, $\angle CAB = \angle MAP$ (common angles) $\angle ABC = \angle AMP = 90^{\circ}$ (each 90°) $\therefore \triangle ABC \sim \triangle AMP$ (AA similarity criterion)

(ii) As, $\triangle ABC \sim \triangle AMP$ (AA similarity criterion) If two triangles are similar then the corresponding sides are always equal, Hence, CA/PA = BC/MP

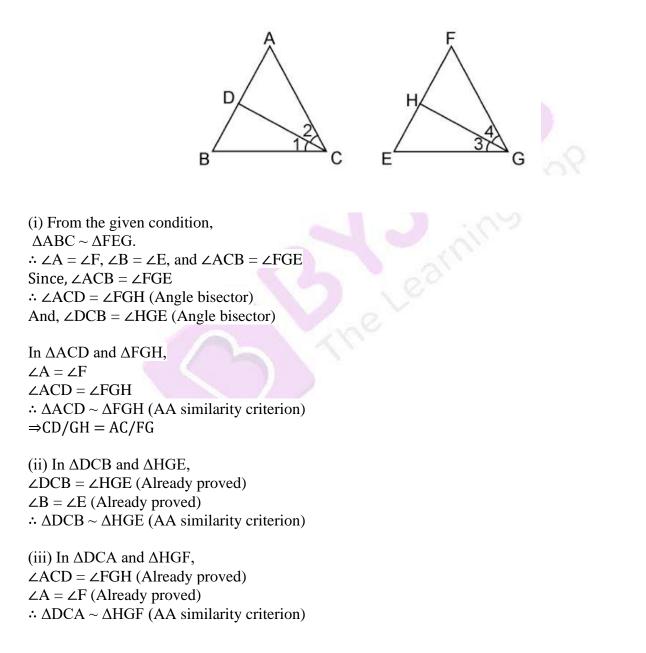
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10. CD and GH are respectively the bisectors of ∠ACB and ∠EGF such that D and H lie on sides AB and FE of ΔABC and ΔEFG respectively. If ΔABC ~ ΔFEG, Show that: (i) CD/GH = AC/FG

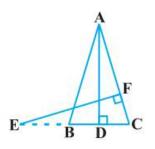
(ii) ΔDCB ~ ΔHGE(iii) ΔDCA ~ ΔHGF

Solution: Given, CD and GH are respectively the bisectors of $\angle ACB$ and $\angle EGF$ such that D and H lie on sides AB and FE of $\triangle ABC$ and $\triangle EFG$ respectively.



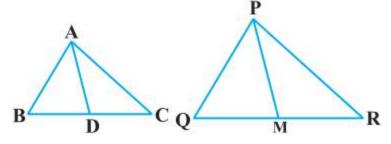
11. In the following figure, E is a point on side CB produced of an isosceles triangle ABC with AB = AC. If AD \perp BC and EF \perp AC, prove that \triangle ABD ~ \triangle ECF.

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Solution: Given, ABC is an isosceles triangle. \therefore AB = AC $\Rightarrow \angle$ ABD = \angle ECF In \triangle ABD and \triangle ECF, \angle ADB = \angle EFC (Each 90°) \angle BAD = \angle CEF (Already proved) $\therefore \triangle$ ABD ~ \triangle ECF (using AA similarity criterion)

12. Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of Δ PQR (see Fig 6.41). Show that Δ ABC ~ Δ PQR.



Solution: Given, $\triangle ABC$ and $\triangle PQR$, AB, BC and median AD of $\triangle ABC$ are proportional to sides PQ, QR and median PM of $\triangle PQR$

i.e. AB/PQ = BC/QR = AD/PM

We have to prove: $\triangle ABC \sim \triangle PQR$

As we know here, AB/PQ = BC/QR = AD/PM

 $\frac{AB}{PQ} = \frac{\frac{1}{2}BC}{\frac{1}{2}QR} = \frac{AD}{PM}.$ (i)

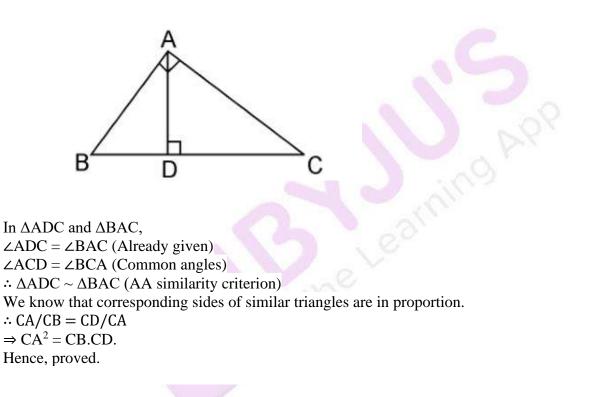
 $\Rightarrow AB/PQ = BC/QR = AD/PM \text{ (D is the midpoint of BC. M is the midpoint of QR)}$ $\Rightarrow \Delta ABD \sim \Delta PQM \text{ [SSS similarity criterion]}$ $\therefore \angle ABD = \angle PQM \text{ [Corresponding angles of two similar triangles are equal]}$ $\Rightarrow \angle ABC = \angle PQR$



In $\triangle ABC$ and $\triangle PQR$ AB/PQ = BC/QR(i) $\angle ABC = \angle PQR$ (ii) From equation (i) and (ii), we get, $\triangle ABC \sim \triangle PQR$ [SAS similarity criterion]

13. D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$. Show that $CA^2 = CB.CD$

Solution: Given, D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$.



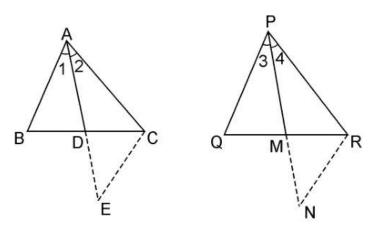
14. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR. Show that \triangle ABC ~ \triangle PQR.

Solution: Given: Two triangles $\triangle ABC$ and $\triangle PQR$ in which AD and PM are medians such that; AB/PQ = AC/PR = AD/PM

We have to prove, $\triangle ABC \sim \triangle PQR$

Let us construct first: Produce AD to E so that AD = DE. Join CE, Similarly produce PM to N such that PM = MN, also Join RN.





In $\triangle ABD$ and $\triangle CDE$, we have AD = DE [By Construction.] BD = DC [Since, AP is the median] and, $\angle ADB = \angle CDE$ [Vertically opposite angles] $\therefore \triangle ABD \cong \triangle CDE$ [SAS criterion of congruence] $\Rightarrow AB = CE$ [By CPCT](i)

Also, in ΔPQM and ΔMNR , PM = MN [By Construction.] QM = MR [Since, PM is the median] and, $\angle PMQ = \angle NMR$ [Vertically opposite angles] $\therefore \Delta PQM = \Delta MNR$ [SAS criterion of congruence] $\Rightarrow PQ = RN$ [CPCT](ii)

Now, AB/PQ = AC/PR = AD/PM From equation (i) and (ii), \Rightarrow CE/RN = AC/PR = AD/PM \Rightarrow CE/RN = AC/PR = 2AD/2PM \Rightarrow CE/RN = AC/PR = AE/PN [Since 2AD = AE and 2PM = PN] $\therefore \Delta ACE \sim \Delta PRN$ [SSS similarity criterion] Therefore, $\angle 2 = \angle 4$ Similarly, $\angle 1 = \angle 3$ $\therefore \angle 1 + \angle 2 = \angle 3 + \angle 4$ $\Rightarrow \angle A = \angle P$(iii)

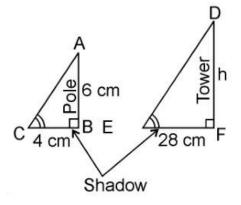
Now, In $\triangle ABC$ and $\triangle PQR$, we have AB/PQ = AC/PR (Already given) From equation (iii), $\angle A = \angle P$ $\therefore \triangle ABC \sim \triangle PQR$ [SAS similarity criterion]



15. A vertical pole of a length 6 m casts a shadow 4m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.

Solution:

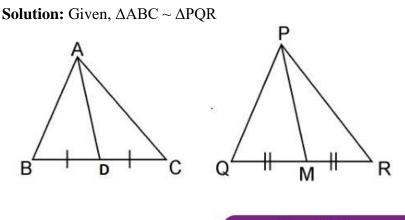
Given, Length of the vertical pole = 6mShadow of the pole = 4mLet Height of tower = hmLength of shadow of the tower = 28m



In $\triangle ABC$ and $\triangle DEF$, $\angle C = \angle E$ (angular elevation of sum) $\angle B = \angle F = 90^{\circ}$ $\therefore \triangle ABC \sim \triangle DEF$ (AA similarity criterion) $\therefore AB/DF = BC/EF$ (If two triangles are similar corresponding sides are proportional)

 $\therefore 6/h = 4/28$ $\Rightarrow h = (6 \times 28)/4$ $\Rightarrow h = 6 \times 7$ $\Rightarrow h = 42 m$ Hence, the height of the tower is 42 m.

16. If AD and PM are medians of triangles ABC and PQR, respectively where $\triangle ABC \sim \triangle PQR$ prove that AB/PQ = AD/PM.



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We know that the corresponding sides of similar triangles are in proportion.

 $\therefore AB/PQ = AC/PR = BC/QR....(i)$ $Also, <math>\angle A = \angle P, \angle B = \angle Q, \angle C = \angle R$ (ii) Since AD and PM are medians, they will divide their opposite sides. $\therefore BD = BC/2 \text{ and } QM = QR/2 \dots (iii)$ From equations (i) and (iii), we get $AB/PQ = BD/QM \dots (iv)$

In $\triangle ABD$ and $\triangle PQM$, From equation (ii), we have $\angle B = \angle Q$ From equation (iv), we have, AB/PQ = BD/QM

 $\therefore \Delta ABD \sim \Delta PQM \text{ (SAS similarity criterion)} \\\Rightarrow AB/PQ = BD/QM = AD/PM$