

RD Sharma Solutions for Class 11 Maths Chapter 23 – The Straight Lines

EXERCISE 23.12

P&GE NO: 23.92

1. Find the equation of a line passing through the point (2, 3) and parallel to the line 3x - 4y + 5 = 0. Solution: Given: The equation is parallel to 3x - 4y + 5 = 0 and pass through (2, 3) The equation of the line parallel to 3x - 4y + 5 = 0 is $3x - 4y + \lambda = 0,$ Where, λ is a constant. It passes through (2, 3). Substitute the values in above equation, we get $3(2) - 4(3) + \lambda = 0$ $6 - 12 + \lambda = 0$ $\lambda = 6$ Now, substitute the value of $\lambda = 6$ in $3x - 4y + \lambda = 0$, we get 3x - 4y + 6 \therefore The required line is 3x - 4y + 6 = 0. 2. Find the equation of a line passing through (3, -2) and perpendicular to the line x

2. Find the equation of a line passing through (3, -2) and perpendicular to the line x - 3y + 5 = 0.

Solution: Given: The equation is perpendicular to x - 3y + 5 = 0 and passes through (3,-2) The equation of the line perpendicular to x - 3y + 5 = 0 is $3x + y + \lambda = 0$, Where, λ is a constant. It passes through (3, -2). Substitute the values in above equation, we get $3 (3) + (-2) + \lambda = 0$ $9 - 2 + \lambda = 0$ $\lambda = -7$ Now, substitute the value of $\lambda = -7$ in $3x + y + \lambda = 0$, we get 3x + y - 7 = 0 \therefore The required line is 3x + y - 7 = 0.

3. Find the equation of the perpendicular bisector of the line joining the points (1, 3) and (3, 1).

Solution:



Given:

A (1, 3) and B (3, 1) be the points joining the perpendicular bisector Let C be the midpoint of AB. So, coordinates of C = [(1+3)/2, (3+1)/2] = (2, 2)Slope of AB = [(1-3) / (3-1)] = -1Slope of the perpendicular bisector of AB = 1 Thus, the equation of the perpendicular bisector of AB is given as, y - 2 = 1(x - 2) y = x x - y = 0 \therefore The required equation is y = x.

4. Find the equations of the altitudes of a \triangle ABC whose vertices are A (1, 4), B (-3, 2) and C (-5, -3).

Solution:

Given:

The vertices of $\triangle ABC$ are A (1, 4), B (-3, 2) and C (-5, -3). Now let us find the slopes of $\triangle ABC$.



Slope of AB =
$$[(2 - 4) / (-3 - 1)]$$

= $\frac{1}{2}$

Slope of BC =
$$[(-3 - 2) / (-5+3)]$$

= $5/2$

Slope of CA = [(4 + 3) / (1 + 5)]= 7/6 Thus, we have:



Slope of CF = -2Slope of AD = -2/5Slope of BE = -6/7Hence, Equation of CF is: y + 3 = -2(x + 5)y + 3 = -2x - 102x + y + 13 = 0

Equation of AD is: y - 4 = (-2/5) (x - 1)5y - 20 = -2x + 22x + 5y - 22 = 0

Equation of BE is: y - 2 = (-6/7) (x + 3)7y - 14 = -6x - 186x + 7y + 4 = 0

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: The required equations are 2x + y + 13 = 0, 2x + 5y - 22 = 0, 6x + 7y + 4 = 0.

5. Find the equation of a line which is perpendicular to the line $\sqrt{3x} - y + 5 = 0$ and which cuts off an intercept of 4 units with the negative direction of y-axis. Solution:

Given:

The equation is perpendicular to $\sqrt{3x} - y + 5 = 0$ equation and cuts off an intercept of 4 units with the negative direction of y-axis.

The line perpendicular to $\sqrt{3x - y} + 5 = 0$ is $x + \sqrt{3y} + \lambda = 0$

It is given that the line $x + \sqrt{3}y + \lambda = 0$ cuts off an intercept of 4 units with the negative direction of the y-axis.

This means that the line passes through (0,-4). So.

Let us substitute the values in the equation $x + \sqrt{3}y + \lambda = 0$, we get 0

$$0 - \sqrt{3}(4) + \lambda =$$

$$\lambda = 4\sqrt{3}$$

Now, substitute the value of λ back, we get

 $\mathbf{x} + \sqrt{3}\mathbf{y} + 4\sqrt{3} = 0$

: The required equation of line is $x + \sqrt{3}y + 4\sqrt{3} = 0$.

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