

RD Sharma Solutions for Class 11 Maths Chapter 30 – Derivatives

EXERCISE 30.3

P&GE NO: 30.33

Differentiate the following with respect to x:

1. $x^4 - 2\sin x + 3\cos x$ **Solution:** Given: $f(x) = x^4 - 2\sin x + 3\cos x$ Differentiate on both the sides with respect to x, we get $\frac{\mathrm{d}}{\mathrm{dx}}\{\mathrm{f}(\mathrm{x})\} = \frac{\mathrm{d}}{\mathrm{dx}}\left(\mathrm{x}^4 - 2\sin\mathrm{x} + 3\cos\mathrm{x}\right)$ By using algebra of derivatives, $f' = \frac{d}{dx}(x^4) - 2\frac{d}{dx}(\sin x) + 3\frac{d}{dx}(\cos x)$ We know that, $\frac{d}{dx}(x^n) = nx^{n-1}$ $\frac{d}{dx}(\sin x) = \cos x$ $\frac{d}{dx}(\cos x) = -\sin x$ So. $=4x^{4-1}-2\cos x+3(-\sin x)$ $=4x^{3}-2\cos x-3\sin x$ \therefore Derivative of f (x) is $4x^3 - 2\cos x - 3\sin x$ 2. $3^{x} + x^{3} + 3^{3}$ **Solution:** Given: $f(x) = 3^x + x^3 + 3^3$ Differentiate on both the sides with respect to x, we get

$$\frac{\mathrm{d}}{\mathrm{dx}}\{\mathrm{f}(\mathrm{x})\} = \frac{\mathrm{d}}{\mathrm{dx}}\left(3^{\mathrm{x}} + \mathrm{x}^{3} + 3^{3}\right)$$

By using algebra of derivatives,

 $f' = \frac{d}{dx}(3^{x}) + \frac{d}{dx}(x^{3}) + \frac{d}{dx}(3^{3})$ We know that, $\frac{d}{dx}(x^{n}) = nx^{n-1}$

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 $\frac{d}{dx}(a^x) = a^x \log a$ $\frac{d}{dx}(\text{constant}) = 0$ $f' = 3^x \log_e 3 + 3x^{3-1} + 0$ $= 3^{x} \log_{e} 3 + 3x^{2}$

 \therefore Derivative of f (x) is $3^x \log_e 3 + 3x^2$

$$3.\,\frac{x^3}{3} - 2\sqrt{x} + \frac{5}{x^2}$$

Solution:

Given:

$$f(x) = \frac{x^3}{3} - 2\sqrt{x} + \frac{5}{x^2}$$

Differentiate on both the sides with respect to x, we get

$$\frac{d}{dx}\{f(x)\} = \frac{d}{dx}\left(\frac{x^{3}}{3} - 2\sqrt{x} + \frac{5}{x^{2}}\right)$$

By using algebra of derivatives,

$$f' = \frac{d}{dx} \left(\frac{x^3}{3} \right) - 2 \frac{d}{dx} (\sqrt{x}) + 5 \frac{d}{dx} \left(\frac{1}{x^2} \right)$$
$$= \frac{1}{3} \frac{d}{dx} (x^3) - 2 \frac{d}{dx} (x^{\frac{1}{2}}) + 5 \frac{d}{dx} (x^{-2})$$

We know that,

$$\frac{d}{dx}(x^{n}) = nx^{n-1}$$

$$f' = \frac{1}{3}(3x^{3-1}) - 2 \times \frac{1}{2}x^{\frac{1}{2}-1} + 5(-2)x^{-2-1}$$

$$= \frac{3 \times \frac{1}{3}x^{2} - x^{-\frac{1}{2}} - 10x^{-3}}{= x^{2} - x^{(-1/2)} - 10x^{-3}}$$

$$\therefore \text{ Derivative of } f(x) \text{ is } x^{2} - x^{(-1/2)} - 10x^{-3}$$

4.
$$e^{x \log a} + e^{a \log x} + e^{a \log a}$$

Solution:
Given:
 $f(x) = e^{x \log a} + e^{a \log x} + e^{a \log a}$
We know that,
 $e^{\log f(x)} = f(x)$
So,
 $f(x) = a^x + x^a + a^a$

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Differentiate on both the sides with respect to x, we get

 $\frac{d}{dx}{f(x)} = \frac{d}{dx}(a^x + x^a + a^a)$ By using algebra of derivatives, $f' = \frac{d}{dx}(a^x) + \frac{d}{dx}(x^a) + \frac{d}{dx}(a^a)$ We know that, $\frac{d}{dx}(x^n) = nx^{n-1}$ $\frac{d}{dx}(a^x) = a^x \log a$ $\int \frac{d}{dx}(\text{constant}) = 0$ $f' = a^x \log_a a - ax^{a-1} + 0$ $= a^x \log a - ax^{a-1}$ \therefore Derivative of f(x) is $a^x \log a - ax^{a-1}$ 5. $(2x^2 + 1)(3x + 2)$ Solution: Given: $f(x) = (2x^2 + 1)(3x + 2)$ $= 6x^3 + 4x^2 + 3x + 2$ Differentiate on both the sides with respect to x, we get $\frac{d}{dx}{f(x)} = \frac{d}{dx}(6x^3 + 4x^2 + 3x + 2)$ By using algebra of derivatives, $f'_{f'} = 6 \frac{d}{dx}(x^3) + 4 \frac{d}{dx}(x^2) + 3 \frac{d}{dx}(x) + \frac{d}{dx}(2)$ We know that, $\frac{d}{dx}(x^n) = nx^{n-1}$ $\frac{d}{dw}(\text{constant}) = 0$ $f' = 6(3x^{3-1}) + 4(2x^{2-1}) + 3(x^{1-1}) + 0$ $= 18x^2 + 8x + 3 + 0$ $= 18x^2 + 8x + 3$ \therefore Derivative of f(x) is $18x^2 + 8x + 3$