

**EXERCISE 14A**

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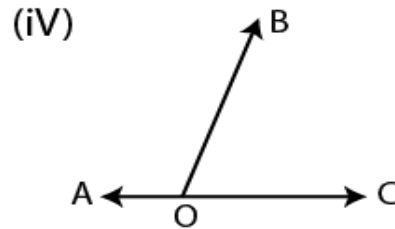
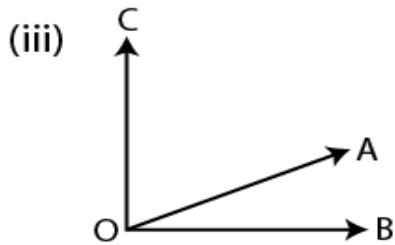
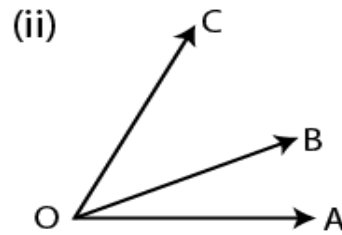
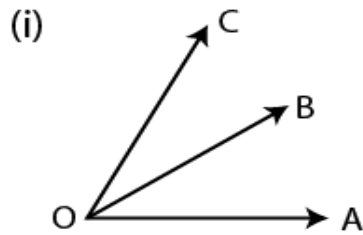
**1. State, true or false:**

- (i) A line segment 4 cm long can have only 2000 points in it.
- (ii) A ray has one end point and a line segment has two end-points.
- (iii) A line segment is the shortest distance between any two given points.
- (iv) An infinite number of straight lines can be drawn through a given point.
- (v) Write the number of end points in
  - (a) a line segment AB (b) a ray AB (c) a line AB
- (vi) Out of  $\overleftrightarrow{AB}$ ,  $\overrightarrow{AB}$ ,  $\overleftarrow{AB}$  and  $\overline{AB}$  which one has a fixed length?
- (vii) How many rays can be drawn through a fixed point O?
- (viii) How many lines can be drawn through three
  - (a) collinear points?
  - (b) non-collinear points?
- (ix) Is  $40^\circ$  the complement of  $60^\circ$ ?
- (x) Is  $45^\circ$  the supplement of  $45^\circ$ ?

**Solution:**

- (i) False.  
It contains infinite number of points.
- (ii) True.
- (iii) True.
- (iv) True.
- (v) (a) 2 (b) 1 (c) 0
- (vi) AB has fixed length.
- (vii) Infinite rays can be drawn through a fixed point O.
- (viii) (a) 1 line can be drawn through three collinear points.  
(b) 3 lines can be drawn through three non-collinear points.
- (ix) False.  
 $40^\circ$  is the complement of  $50^\circ$  as  $40^\circ + 50^\circ = 90^\circ$
- (x) False.  
 $45^\circ$  is the supplement of  $135^\circ$  not  $45^\circ$ .

**2. In which of the following figures, are  $\angle AOB$  and  $\angle AOC$  adjacent angles? Give, in each case, reason for your answer.**



**Solution:**

If  $\angle AOB$  and  $\angle AOC$  are adjacent angle, they have OA as their common arm.

(i) From the figure

OB is the common arm

$\angle AOB$  and  $\angle AOC$  are not adjacent angles.

(ii) From the figure

OC is the common arm

$\angle AOB$  and  $\angle AOC$  are not adjacent angles.

(iii) From the figure

OA is the common arm

$\angle AOB$  and  $\angle AOC$  are adjacent angles.

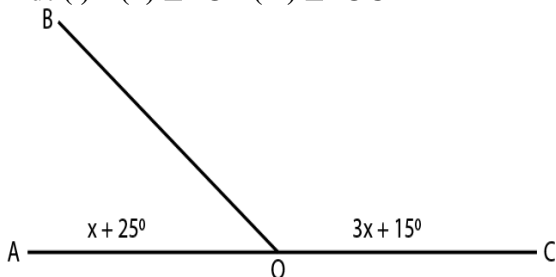
(iv) From the figure

OB is the common arm

$\angle AOB$  and  $\angle AOC$  are not adjacent angles.

**3. In the given figure, BAC is a straight line.**

**Find:** (i)  $x$  (ii)  $\angle AOB$  (iii)  $\angle BOC$



**Solution:**

We know that

$\angle AOB$  and  $\angle COB$  are linear pairs

It can be written as

$$\angle AOB + \angle COB = 180^\circ$$

Substituting the values

$$x + 25^\circ + 3x + 15^\circ = 180^\circ$$

By further calculation

$$4x + 40^\circ = 180^\circ$$

So we get

$$4x = 180 - 40 = 140^\circ$$

$$(i) x = 140/4 = 35^\circ$$

$$(ii) \angle AOB = x + 25$$

Substituting the value of x

$$\angle AOB = 25 + 35 = 60^\circ$$

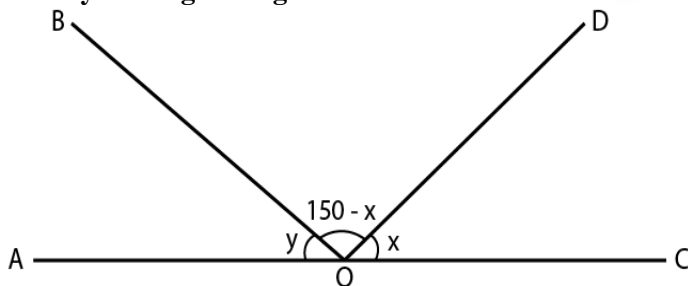
$$(iii) \angle BOC = 3x + 15^\circ$$

Substituting the value of x

$$\angle BOC = (3 \times 35) + 15$$

$$\angle BOC = 120^\circ$$

4. Find y in the given figure.



**Solution:**

Here AOC is a straight line

We can write it as

$$\angle AOB + \angle BOD + \angle DOC = 180^\circ$$

Substituting the values

$$y + 150 - x + x = 180$$

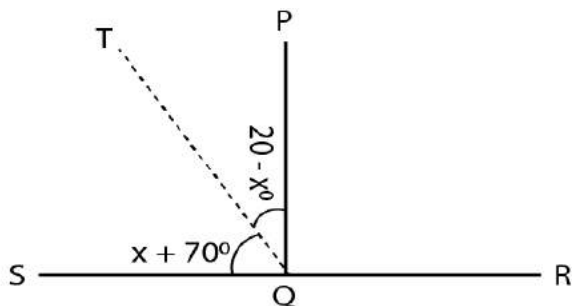
By further calculation

$$y + 150 = 180$$

So we get

$$y = 180 - 150 = 30^\circ$$

5. In the given figure, find  $\angle PQR$ .



**Solution:**

Here SQR is a straight line

We can write it as

$$\angle SQT + \angle TQP + \angle PQR = 180^\circ$$

Substituting the values

$$x + 70 + 20 - x + \angle PQR = 180^\circ$$

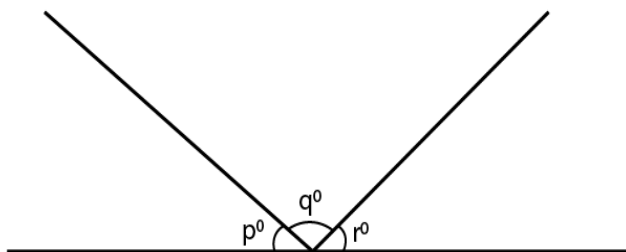
By further calculation

$$90^\circ + \angle PQR = 180^\circ$$

So we get

$$\angle PQR = 180^\circ - 90^\circ = 90^\circ$$

**6. In the given figure,  $p^\circ = q^\circ = r^\circ$ , find each.**



**Solution:**

We know that

$$p^\circ + q^\circ + r^\circ = 180^\circ \text{ is a straight angle}$$

It is given that

$$p^\circ = q^\circ = r^\circ$$

We can write it as

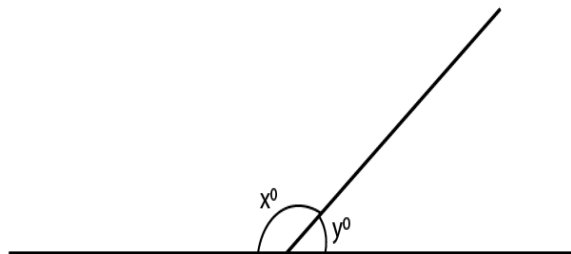
$$p^\circ + p^\circ + p^\circ = 180^\circ$$

$$3p = 180$$

$$p = 180/3 = 60^\circ$$

Therefore,  $p^\circ = q^\circ = r^\circ = 60^\circ$

**7. In the given figure, if  $x = 2y$ , find  $x$  and  $y$ .**



**Solution:**

It is given that

$$x = 2y$$

For a straight angle

$$x^\circ + y^\circ = 180^\circ$$

Substituting the values

$$2y + y = 180$$

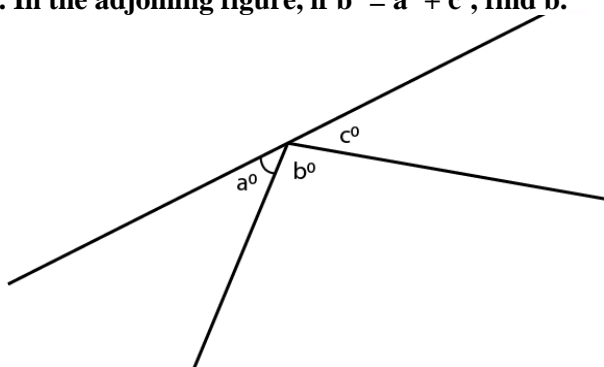
By further calculation

$$3y = 180$$

$$y = 180/3 = 60^\circ$$

$$x = 2y = 2 \times 60^\circ = 120^\circ$$

**8. In the adjoining figure, if  $b^\circ = a^\circ + c^\circ$ , find  $b$ .**



**Solution:**

It is given that

$$b^\circ = a^\circ + c^\circ$$

For a straight angle

$$a^\circ + b^\circ + c^\circ = 180^\circ$$

Substituting the values

$$b^\circ + b^\circ = 180^\circ$$

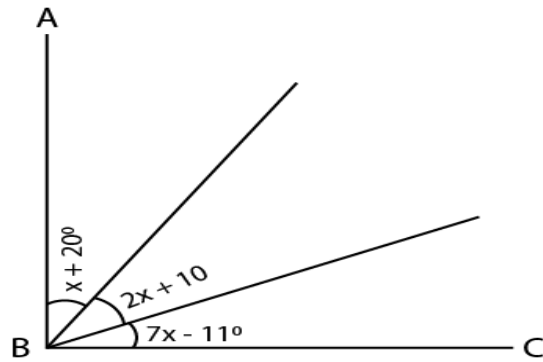
$$2b^\circ = 180^\circ$$

$$b^\circ = 180/2 = 90^\circ$$

**9. In the given figure, AB is perpendicular to BC at B.**

**Find : (i) the value of  $x$ .**

**(ii) the complement of angle  $x$ .**



**Solution:**

(i) From the figure

$AB \perp BC$  at B

Here  $\angle ABC = 90^\circ$

Substituting the values

$$x + 20 + 2x + 10 + 7x - 11 = 90$$

By further calculation

$$10x + 10 = 90$$

$$10x = 90 - 10 = 80$$

$$x = 80/10 = 8^\circ$$

(ii) The complement of angle  $x = 90 - x$

So we get

$$= 90 - 8 = 82^\circ$$

**10. Write the complement of:**

(i)  $25^\circ$

(ii)  $90^\circ$

(iii)  $a^\circ$

(iv)  $(x + 5)^\circ$

(v)  $(30 - a)^\circ$

(vi)  $\frac{1}{2}$  of a right angle

(vii)  $\frac{1}{3}$  of  $180^\circ$

(viii)  $21^\circ 17'$

**Solution:**

(i) The complement of  $25^\circ = 90^\circ - 25^\circ = 65^\circ$

(ii) The complement of  $90^\circ = 90^\circ - 90^\circ = 0$

(iii) The complement of  $a^\circ = 90^\circ - a^\circ$

(iv) The complement of  $(x + 5)^\circ = 90^\circ - (x + 5)^\circ$

By further calculation

$$= 90^\circ - x - 5^\circ$$

$$= 85^\circ - x$$

(v) The complement of  $(30 - a)^\circ = 90^\circ - (30 - a)^\circ$

By further calculation

$$= 90^\circ - 30^\circ + a^\circ$$

$$= 60^\circ + a^\circ$$

(vi) The complement of  $\frac{1}{2}$  of a right angle  $= 90^\circ - \frac{1}{2}$  of a right angle

So we get

$$= 90^\circ - \frac{1}{2} \times 90^\circ$$

$$= 90^\circ - 45^\circ$$

$$= 45^\circ$$

(vii) The complement of  $\frac{1}{3}$  of  $180^\circ = 90^\circ - \frac{1}{3}$  of  $180^\circ$

By further calculation

$$= 90^\circ - 60^\circ$$

$$= 30^\circ$$

(viii) The complement of  $21^\circ 17' = 90^\circ - 21^\circ 17'$

So we get

$$= 68^\circ 43'$$

**11. Write the supplement of:**

(i)  $100^\circ$

(ii)  $0^\circ$

(iii)  $x^\circ$

(iv)  $(x + 35)^\circ$

(v)  $(90 + a + b)^\circ$

(vi)  $(110 - x - 2y)^\circ$

(vii)  $\frac{1}{5}$  of a right angle

(viii)  $80^\circ 49' 25''$

**Solution:**

(i) The supplement of  $100^\circ = 180 - 100 = 80^\circ$

(ii) The supplement of  $0^\circ = 180 - 0 = 180^\circ$

(iii) The supplement of  $x^\circ = 180^\circ - x^\circ$

(iv) The supplement of  $(x + 35)^\circ = 180^\circ - (x + 35)^\circ$

We can write it as

$$= 180 - x - 35$$

$$= 145^\circ - x^\circ$$

(v) The supplement of  $(90 + a + b)^\circ = 180^\circ - (90 + a + b)^\circ$

We can write it as

$$= 180 - 90 - a - b$$

So we get

$$= 90^\circ - a^\circ - b^\circ$$

$$= (90 - a - b)^\circ$$

(vi) The supplement of  $(110 - x - 2y)^\circ = 180^\circ - (110 - x - 2y)^\circ$

We can write it as

$$= 180 - 110 + x + 2y$$
$$= 70^\circ + x^\circ + 2y^\circ$$

(vii) The supplement of  $1/5$  of a right angle  $= 180^\circ - 1/5$  of a right angle

We can write it as

$$= 180^\circ - 1/5 \times 90^\circ$$

So we get

$$= 180^\circ - 18^\circ$$

$$= 162^\circ$$

(viii) The supplement of  $80^\circ 49' 25'' = 180^\circ - 80^\circ 49' 25''$

We know that  $1^\circ = 60'$  and  $1' = 60''$

So we get

$$= 99^\circ 10' 35''$$

**12. Are the following pairs of angles complementary?**

(i)  $10^\circ$  and  $80^\circ$

(ii)  $37^\circ 28'$  and  $52^\circ 33'$

(iii)  $(x + 16)^\circ$  and  $(74 - x)^\circ$

(iv)  $54^\circ$  and  $2/5$  of a right angle.

**Solution:**

(i)  $10^\circ$  and  $80^\circ$

Yes, they are complementary angles as their sum  $= 10^\circ + 80^\circ = 90^\circ$

(ii)  $37^\circ 28'$  and  $52^\circ 33'$

No, they are not complementary angles as their sum is not equal to  $90^\circ$

$$37^\circ 28' + 52^\circ 33' = 90^\circ 1'$$

(iii)  $(x + 16)^\circ$  and  $(74 - x)^\circ$

Yes, they are complementary angles as their sum  $= x + 16 + 74 - x = 90^\circ$

(iv)  $54^\circ$  and  $2/5$  of a right angle

We can write it as

$$= 54^\circ \text{ and } 2/5 \times 90^\circ$$

$$= 54^\circ \text{ and } 36^\circ$$

Yes, they are complementary angles as their sum  $= 54 + 36 = 90^\circ$

**13. Are the following pairs of angles supplementary?**

(i)  $139^\circ$  and  $39^\circ$

(ii)  $26^\circ 59'$  and  $153^\circ 1'$

(iii)  $3/10$  of a right angle and  $4/15$  of two right angles

(iv)  $2x^\circ + 65^\circ$  and  $115^\circ - 2x^\circ$

**Solution:**

(i)  $139^\circ$  and  $39^\circ$

No, they are not supplementary angles as their sum is not equal to  $180^\circ$

$$139^\circ + 39^\circ = 178^\circ$$

(ii)  $26^\circ 59'$  and  $153^\circ 1'$



Yes, they are supplementary angles as their sum =  $26^{\circ}59' + 153^{\circ}1' = 180^{\circ}$

(iii)  $3/10$  of a right angle and  $4/15$  of two right angles

We can write it as

$$= 3/10 \text{ of } 90^{\circ} \text{ and } 4/15 \text{ of } 180^{\circ}$$

$$= 27^{\circ} \text{ and } 48^{\circ}$$

No, they are not supplementary angles as their sum is not equal to  $180^{\circ}$

$$27^{\circ} + 48^{\circ} = 75^{\circ}$$

(iv)  $2x^{\circ} + 65^{\circ}$  and  $115^{\circ} - 2x^{\circ}$

Yes they are supplementary angles as their sum =  $2x + 65 + 115 - 2x = 180^{\circ}$

**14. If  $3x + 18^{\circ}$  and  $2x + 25^{\circ}$  are supplementary, find the value of x.**

**Solution:**

It is given that  $3x + 18^{\circ}$  and  $2x + 25^{\circ}$  are supplementary

We can write it as

$$3x + 18^{\circ} + 2x + 25^{\circ} = 180^{\circ}$$

By further calculation

$$5x + 43^{\circ} = 180^{\circ}$$

So we get

$$5x = 180 - 43 = 137^{\circ}$$

$$x = 137/5 = 27.4^{\circ} \text{ or } 27^{\circ} 24'$$

**15. If two complementary angles are in the ratio 1:5, find them.**

**Solution:**

It is given that two complementary angles are in the ratio 1:5

Consider x and 5x as the angles

We can write it as

$$x + 5x = 90^{\circ}$$

$$6x = 90^{\circ}$$

So we get

$$x = 90/6 = 15^{\circ}$$

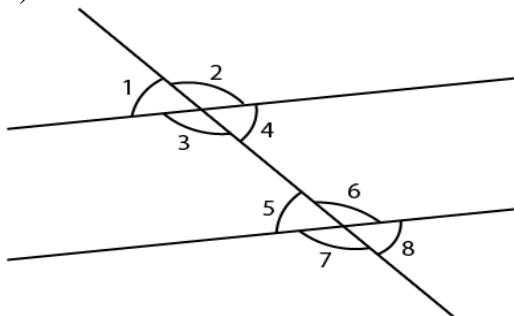
Here the angles will be  $15^{\circ}$  and  $15 \times 5 = 75^{\circ}$

**EXERCISE 14B**

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1. In questions 1 and 2, given below, identify the given pairs of angles as corresponding angles, interior alternate angles, exterior alternate angles, adjacent angles, vertically opposite angles or allied angles:

- (i)  $\angle 3$  and  $\angle 6$
- (ii)  $\angle 2$  and  $\angle 4$
- (iii)  $\angle 3$  and  $\angle 7$
- (iv)  $\angle 2$  and  $\angle 7$
- (v)  $\angle 4$  and  $\angle 6$
- (vi)  $\angle 1$  and  $\angle 8$
- (vii)  $\angle 1$  and  $\angle 5$
- (viii)  $\angle 1$  and  $\angle 4$
- (ix)  $\angle 5$  and  $\angle 7$

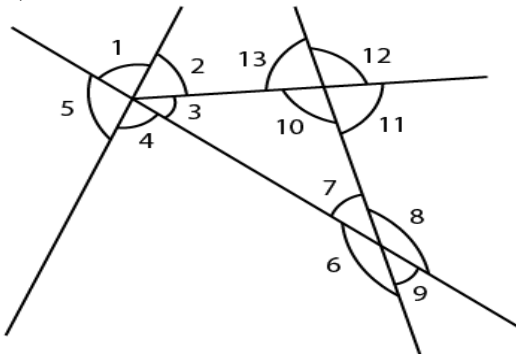


**Solution:**

- (i)  $\angle 3$  and  $\angle 6$  are interior alternate angles.
- (ii)  $\angle 2$  and  $\angle 4$  are adjacent angles.
- (iii)  $\angle 3$  and  $\angle 7$  are corresponding angles.
- (iv)  $\angle 2$  and  $\angle 7$  are exterior alternate angles.
- (v)  $\angle 4$  and  $\angle 6$  are allied or co-interior angles.
- (vi)  $\angle 1$  and  $\angle 8$  are exterior alternate angles.
- (vii)  $\angle 1$  and  $\angle 5$  are corresponding angles.
- (viii)  $\angle 1$  and  $\angle 4$  are vertically opposite angles.
- (ix)  $\angle 5$  and  $\angle 7$  are adjacent angles.

2. (i)  $\angle 1$  and  $\angle 4$   
 (ii)  $\angle 4$  and  $\angle 7$   
 (iii)  $\angle 10$  and  $\angle 12$   
 (iv)  $\angle 7$  and  $\angle 13$   
 (v)  $\angle 6$  and  $\angle 8$   
 (vi)  $\angle 11$  and  $\angle 8$   
 (vii)  $\angle 7$  and  $\angle 9$   
 (viii)  $\angle 4$  and  $\angle 5$

- (ix)  $\angle 4$  and  $\angle 6$   
(x)  $\angle 6$  and  $\angle 7$   
(xi)  $\angle 2$  and  $\angle 13$

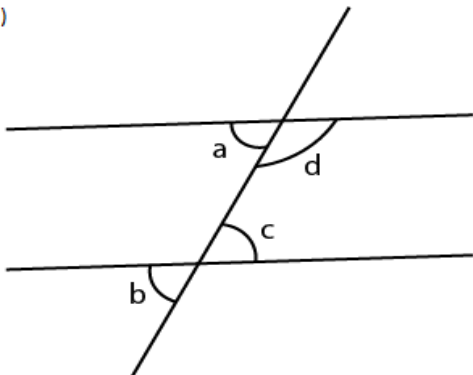


**Solution:**

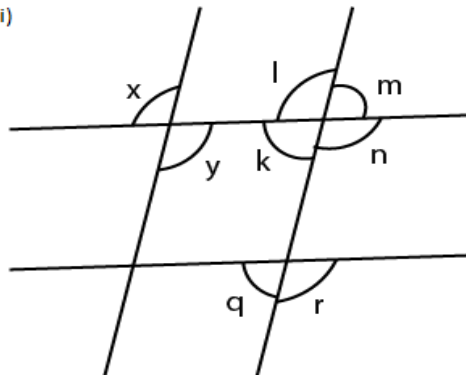
- (i)  $\angle 1$  and  $\angle 4$  are vertically opposite angles.  
(ii)  $\angle 4$  and  $\angle 7$  are interior alternate angles.  
(iii)  $\angle 10$  and  $\angle 12$  are vertically opposite angles.  
(iv)  $\angle 7$  and  $\angle 13$  are corresponding angles.  
(v)  $\angle 6$  and  $\angle 8$  are vertically opposite angles.  
(vi)  $\angle 11$  and  $\angle 8$  are allied or co-interior angles.  
(vii)  $\angle 7$  and  $\angle 9$  are vertically opposite angles.  
(viii)  $\angle 4$  and  $\angle 5$  are adjacent angles.  
(ix)  $\angle 4$  and  $\angle 6$  are allied or co-interior angles.  
(x)  $\angle 6$  and  $\angle 7$  are adjacent angles.  
(xi)  $\angle 2$  and  $\angle 13$  are allied or co-interior angles.

**3. In the following figures, the arrows indicate parallel lines. State which angles are equal. Give reasons.**

(i)



(ii)



**Solution:**

(i) From the figure (i)

$a = b$  are corresponding angles

$b = c$  are vertically opposite angles

$a = c$  are alternate angles

So we get

$a = b = c$

(ii) From the figure (ii)

$x = y$  are vertically opposite angles

$y = l$  are alternate angles

$x = l$  are corresponding angles

$l = n$  are vertically opposite angles

$n = r$  are corresponding angles

So we get

$x = y = l = n = r$

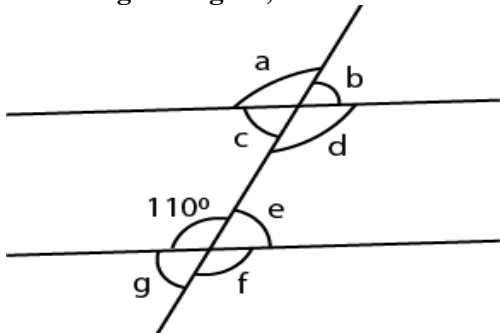
Similarly

$m = k$  are vertically opposite angles

$k = q$  are corresponding angles

Hence,  $m = k = q$ .

**4. In the given figure, find the measure of the unknown angles:**



**Solution:**

From the figure

$a = d$  are vertically opposite angles

$d = f$  are corresponding angles

$f = 110^\circ$  are vertically opposite angles

So we get

$a = d = f = 110^\circ$

We know that

$e + 110^\circ = 180^\circ$  are co-interior angles

$e = 180 - 110 = 70^\circ$

$b = c$  are vertically opposite angles

$b = e$  are corresponding angles

$e = g$  are vertically opposite angles

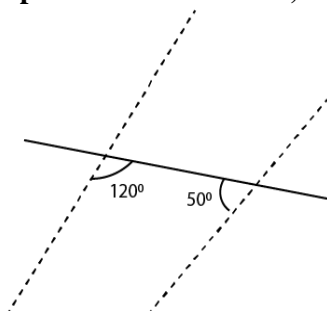
So we get

$b = c = e = g = 70^\circ$

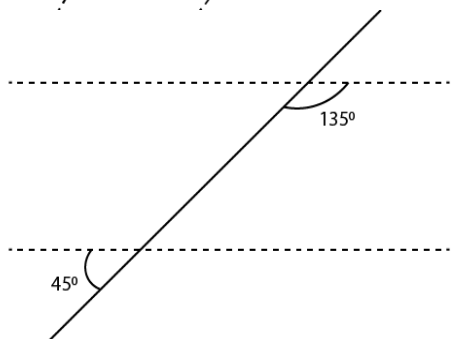
Therefore,  $a = 110^\circ$ ,  $b = 70^\circ$ ,  $c = 70^\circ$ ,  $d = 110^\circ$ ,  $e = 110^\circ$ ,  $f = 110^\circ$  and  $g = 70^\circ$ .

**5. Which pair of the dotted line, segments, in the following figures, are parallel. Give reason:**

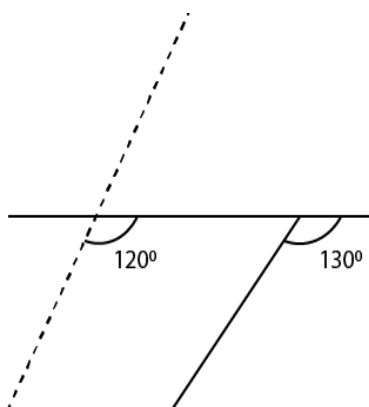
i)



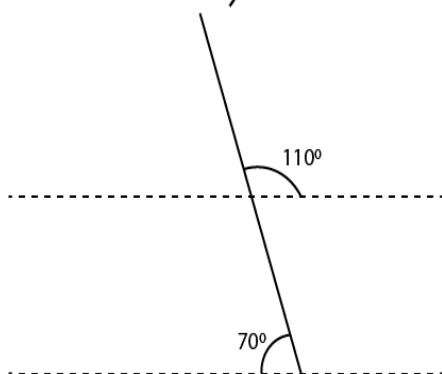
ii)



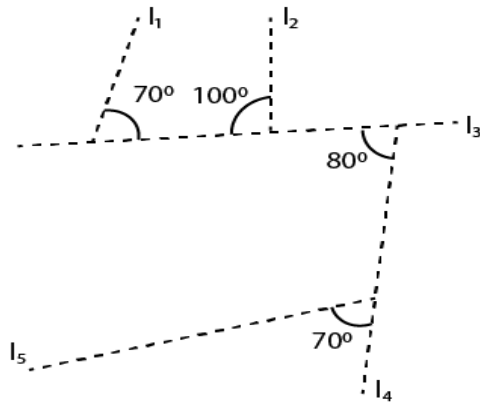
iii)



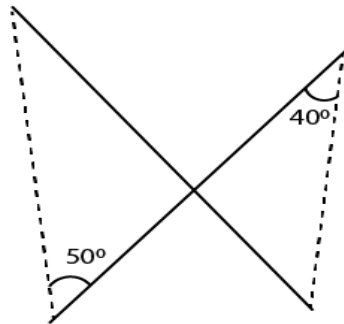
iv)



v)



vi)



**Solution:**

(i) From the figure (i)

If the lines are parallel we get  $120 + 50 = 180^\circ$

There are co-interior angles where  $170^\circ = 180^\circ$

It is not true.

Therefore, they are not parallel lines.

(ii) From the figure (ii)

$\angle 1 = 45^\circ$  are vertically opposite angles

We know that the lines are parallel if

$\angle 1 + 135^\circ = 180^\circ$  are co-interior angles

Substituting the values

$$45^\circ + 135^\circ = 180^\circ$$

$$180^\circ = 180^\circ \text{ which is true}$$

Therefore, the lines are parallel.

(iii) From the figure (iii)

The lines are parallel if corresponding angles are equal

$$\text{Here } 120^\circ = 130^\circ \text{ is not correct}$$

Hence, lines are not parallel.

(iv)  $\angle 1 = 110^\circ$  are vertically opposite angles

We know that if lines are parallel

$$\angle 1 + 70^\circ = 180^\circ \text{ are co-interior angles}$$

Substituting the values

$$110^\circ + 70^\circ = 180^\circ$$

$$180^\circ = 180^\circ \text{ which is correct}$$

Therefore, the lines are parallel.

(v)  $\angle 1 + 100^\circ = 180^\circ$

So we get

$\angle 1 = 180^\circ - 100^\circ = 80^\circ$  which is a linear pair

Here the lines 1 and 2 are parallel if  $\angle 1 = 70^\circ$

$80^\circ = 70^\circ$  is not true

So the  $\angle 1$  and  $\angle 2$  are not parallel

$\angle 3$  and  $\angle 5$  will be parallel if  $80^\circ = 70^\circ$  are corresponding angle which is not true.

Hence,  $\angle 3$  and  $\angle 5$  are not parallel.

We know that

$\angle 1 = 80^\circ$  are alternate angles

$80^\circ = 80^\circ$  which is true

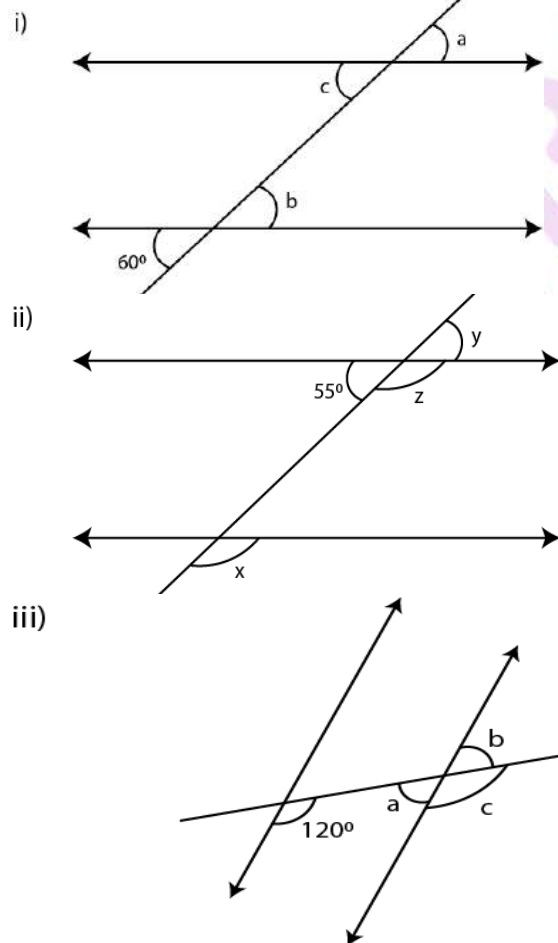
Hence,  $\angle 2$  and  $\angle 4$  are parallel.

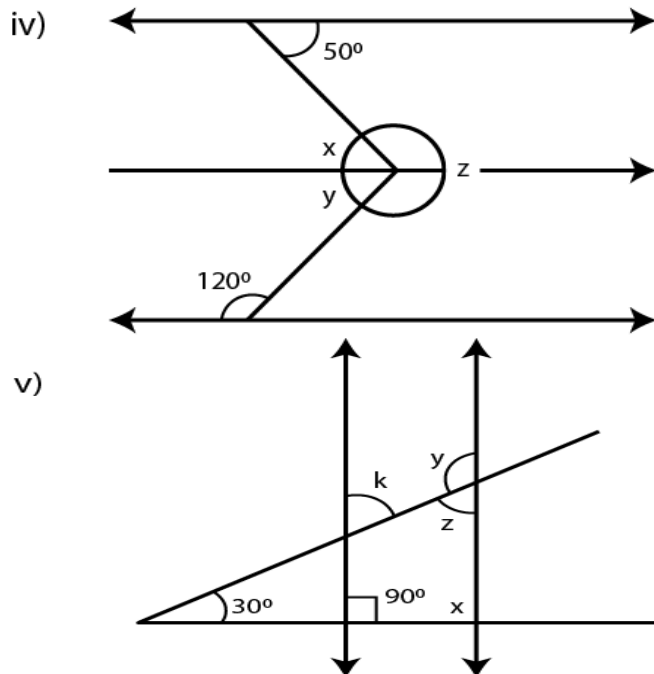
(vi) Two lines are parallel if alternate angles are equal

$50^\circ = 40^\circ$  which is not true

Hence, the lines are not parallel.

**6. In the given figures, the directed lines are parallel to each other. Find the unknown angles.**





**Solution:**

(i) If the lines are parallel

$a = b$  are corresponding angles

$a = c$  are vertically opposite angles

$a = b = c$

Here  $b = 60^\circ$  are vertically opposite angles

Therefore,  $a = b = c = 60^\circ$

(ii) If the lines are parallel

$x = z$  are corresponding angles

$z + y = 180^\circ$  is a linear pair

$y = 55^\circ$  are vertically opposite angles

Substituting the values

$$z + 55^\circ = 180^\circ$$

$$z = 180 - 55 = 125^\circ$$

If  $x = z$  we get  $x = 125^\circ$

Therefore,  $x = 125^\circ$ ,  $y = 55^\circ$  and  $z = 125^\circ$ .

(iii) If the lines are parallel

$$c = 120^\circ$$

$a + 120^\circ = 180^\circ$  are co-interior angles

$$a = 180 - 120 = 60^\circ$$

We know that  $a = b$  are vertically opposite angles

So  $b = 60^\circ$

Therefore,  $a = b = 60^\circ$  and  $c = 120^\circ$ .

(iv) If the lines are parallel

$x = 50^\circ$  are alternate angles

$y + 120^\circ = 180^\circ$  are co-interior angles



$$y = 180 - 120 = 60^\circ$$

We know that

$$x + y + z = 360^\circ \text{ are angles at a point}$$

Substituting the values

$$50 + 60 + z = 360$$

By further calculation

$$110 + z = 360$$

$$z = 360 - 110 = 250^\circ$$

Therefore,  $x = 50^\circ$ ,  $y = 60^\circ$  and  $z = 250^\circ$ .

(v) If the lines are parallel

$$x + 90^\circ = 180^\circ \text{ are co-interior angles}$$

$$x = 180^\circ - 90^\circ = 90^\circ$$

$$\angle 2 = x$$

$$\angle 2 = 90^\circ$$

We know that the sum of angles of a triangle

$$\angle 1 + \angle 2 + 30^\circ = 180^\circ$$

Substituting the values

$$\angle 1 + 90^\circ + 30^\circ = 180^\circ$$

By further calculation

$$\angle 1 + 120^\circ = 180^\circ$$

$$\angle 1 = 180 - 120 = 60^\circ$$

Here  $\angle 1 = k$  are vertically opposite angles

$$k = 60^\circ$$

Here  $\angle 1 = z$  are alternate angles

$$z = 60^\circ$$

Here  $k + y = 180^\circ$  are co-interior angles

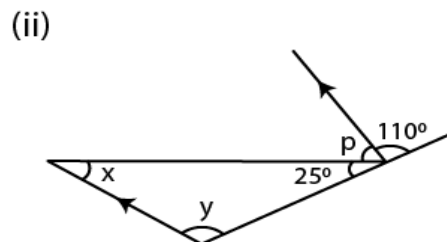
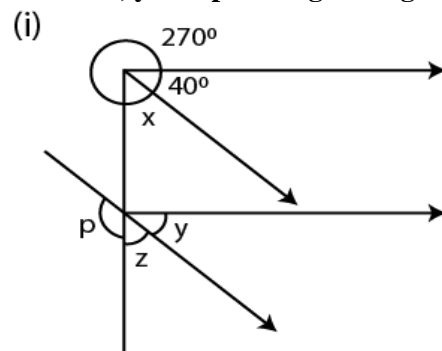
Substituting the values

$$60^\circ + y = 180^\circ$$

$$y = 180 - 60 = 120^\circ$$

Therefore,  $x = 90^\circ$ ,  $y = 120^\circ$ ,  $z = 60^\circ$ ,  $k = 60^\circ$ .

**7. Find  $x$ ,  $y$  and  $p$  in the given figures:**



**Solution:**

(i) From the figure (i)

The lines are parallel

$x = z$  are corresponding angles

$y = 40^\circ$  are corresponding angles

We know that

$x + 40^\circ + 270^\circ = 360^\circ$  are the angles at a point

So we get

$$x + 310^\circ = 360^\circ$$

$$x = 360 - 310 = 50^\circ$$

$$\text{So } z = x = 50^\circ$$

Here  $p + z = 180^\circ$  is a linear pair

By substituting the values

$$p + 50^\circ = 180^\circ$$

$$p = 180 - 50 = 130^\circ$$

Therefore,  $x = 50^\circ$ ,  $y = 40^\circ$ ,  $z = 50^\circ$  and  $p = 130^\circ$ .

(ii) From the figure (ii)

The lines are parallel

$y = 110^\circ$  are corresponding angles

We know that

$$25^\circ + p + 110^\circ = 180^\circ \text{ are angles on a line}$$

$$p + 135^\circ = 180^\circ$$

$$p = 180 - 135 = 45^\circ$$

We know that the sum of angles of a triangle

$$x + y + 25^\circ = 180^\circ$$

$$x + 110^\circ + 25^\circ = 180^\circ$$

By further calculation

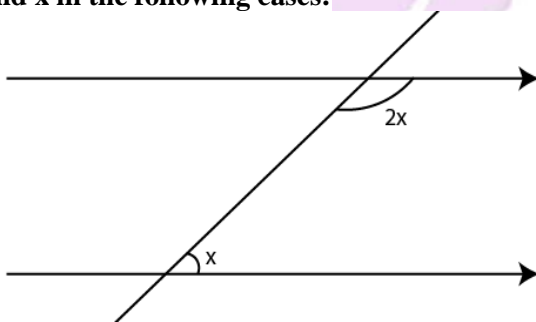
$$x + 135^\circ = 180^\circ$$

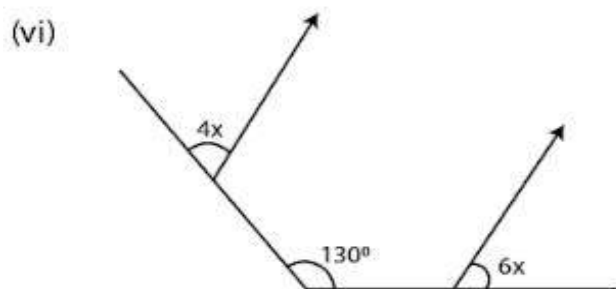
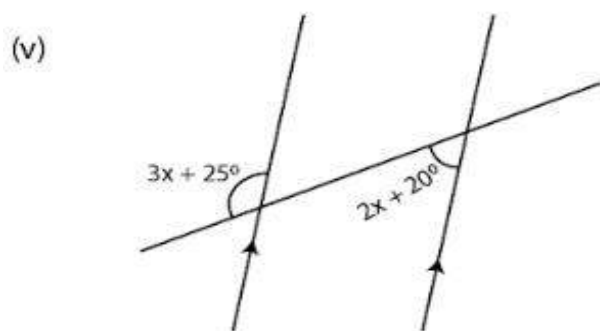
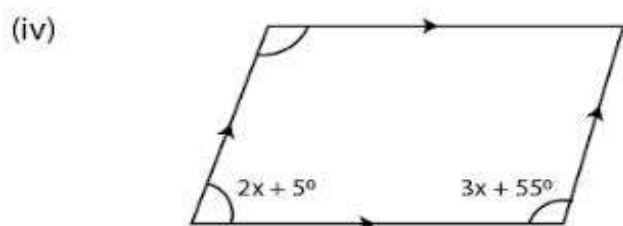
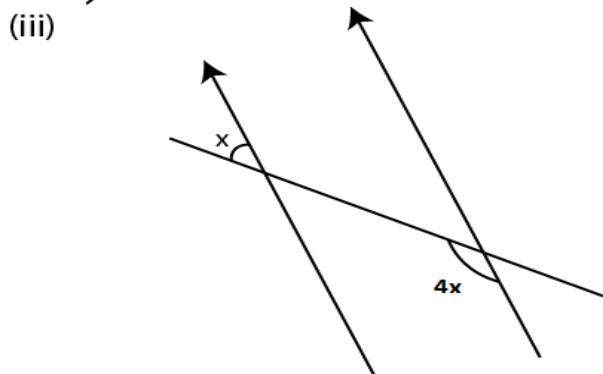
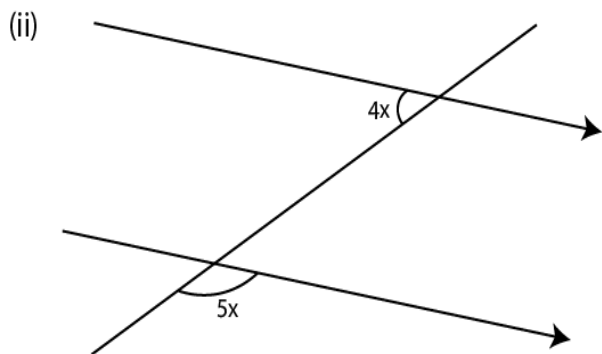
$$x = 180 - 135 = 45^\circ$$

Therefore,  $x = 45^\circ$ ,  $y = 110^\circ$  and  $p = 45^\circ$ .

**8. Find  $x$  in the following cases:**

(i)





**Solution:**

(i) From the figure (i)

The lines are parallel

$2x + x = 180^\circ$  are co-interior angles

$$3x = 180^\circ$$

$$x = 180/3 = 60^\circ$$

(ii) From the figure (ii)

The lines are parallel

$4x + 1 = 180^\circ$  are co-interior angles

$\angle 1 = 5x$  are vertically opposite angles

Substituting the values

$$4x + 5x = 180^\circ$$

So we get

$$9x = 180^\circ$$

$$x = 180/9 = 20^\circ$$

(iii) From the figure (iii)

The lines are parallel

$\angle 1 + 4x = 180^\circ$  are co-interior angles

$\angle 1 = x$  are vertically opposite angles

Substituting the values

$$x + 4x = 180^\circ$$

$$5x = 180^\circ$$

So we get

$$x = 180/5 = 36^\circ$$

(iv) From the figure (iv)

The lines are parallel

$2x + 5 + 3x + 55 = 180^\circ$  are co-interior angles

$$5x + 60^\circ = 180^\circ$$

By further calculation

$$5x = 180 - 60 = 120^\circ$$

So we get

$$x = 120/5 = 24^\circ$$

(v) From the figure (v)

The lines are parallel

$\angle 1 = 2x + 20^\circ$  are alternate angles

$\angle 1 + 3x + 25^\circ = 180^\circ$  is a linear pair

Substituting the values

$$2x + 20^\circ + 3x + 25^\circ = 180^\circ$$

$$5x + 45^\circ = 180^\circ$$

So we get

$$5x = 180 - 45 = 135^\circ$$

$$x = 135/5 = 27^\circ$$

(vi) From the figure (vi)

Construct a line parallel to the given parallel lines

$\angle 1 = 4x$  and  $\angle 2 = 6x$  are corresponding angles

$$\angle 1 + \angle 2 = 130^\circ$$

Substituting the values

$$4x + 6x = 130^\circ$$

$$10x = 130^\circ$$

So we get

$$x = 130/10 = 13^\circ$$



### EXERCISE 14C

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1. Using ruler and compasses, construct the following angles:

(i)  $30^\circ$

(ii)  $15^\circ$

(iii)  $75^\circ$

(iv)  $180^\circ$

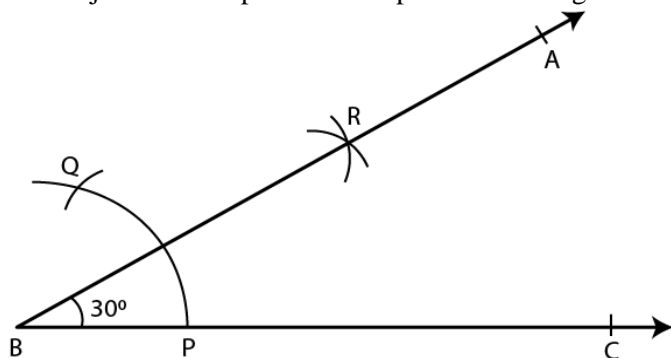
(v)  $165^\circ$

**Solution:**

(i)  $30^\circ$

Steps of Construction:

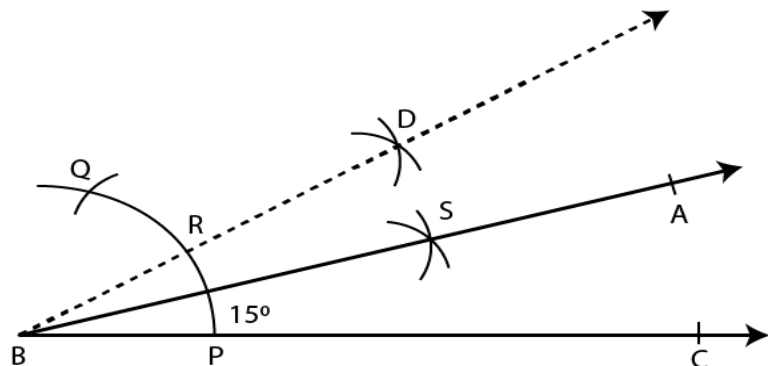
1. Construct a line segment BC.
2. Taking B as centre and a suitable radius construct an arc which meets BC at the point P.
3. Taking P as centre and same radius cut off the arc at the point Q.
4. Consider P and Q as centre construct two arcs which intersect each other at the point R.
5. Now join BR and produce it to point A forming  $\angle ABC = 30^\circ$



(ii)  $15^\circ$

Steps of Construction:

1. Construct a line segment BC.
2. Taking B as centre and a suitable radius construct an arc which meets BC at the point P.
3. Taking P as centre and same radius cut off the arc at the point Q.
4. Consider P and Q as centres, construct two arcs which intersect each other at the point D and join BD.
5. Taking P and R as centre construct two more arcs which intersect each other at the point S.
6. Now join BS and produce it to point A.  $\angle ABC = 15^\circ$

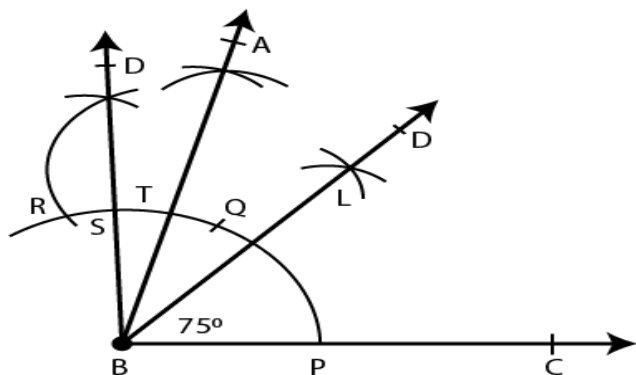


(iii)  $75^\circ$

Steps of Construction:

1. Construct a line segment BC.
2. Taking B as centre and suitable radius construct an arc and cut off PQ then QR of the same radius.
3. Taking Q and R as centre, construct two arcs which intersect each other at the point S.
4. Now join SB.
5. Taking Q and D as centre construct two arcs which intersect each other at the point T.
6. Now join BT and produce it to point A.

$\angle ABC = 75^\circ$

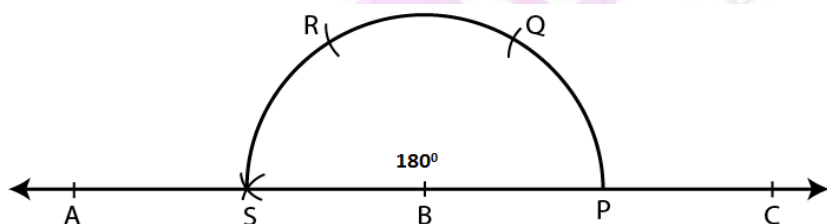


(iv)  $180^\circ$

Steps of Construction:

1. Construct a line segment BC.
2. Taking B as centre and some suitable radius construct an arc which meets BC at the point P.
3. Taking P as centre and with same radius cut off the arcs PQ, QR and RS.
4. Now join BS and produce it to point A.

$\angle ABC = 180^\circ$

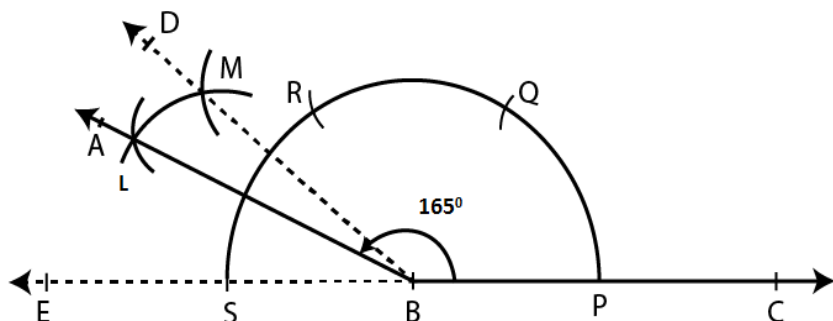


(v)  $165^\circ$

Steps of Construction:

1. Construct a line segment BC.
2. Taking B as centre and some suitable radius construct an arc which meets BC at the point P.
3. Taking P as centre and same radius cut off arcs at PQ, QR and then RS.
4. Now join SB.
5. Taking R and S as centres construct two arcs which intersect each other at the point M.
6. Taking T and S as centres construct two arcs which intersect each other at the point L.
7. Now join BL and produce it to point A.

$\angle ABC = 165^\circ$



2. Draw  $\angle ABC = 120^\circ$ . Bisect the angle using ruler and compasses only. Measure each angle so obtained and check whether the angles obtained on bisecting  $\angle ABC$  are equal or not.

**Solution:**

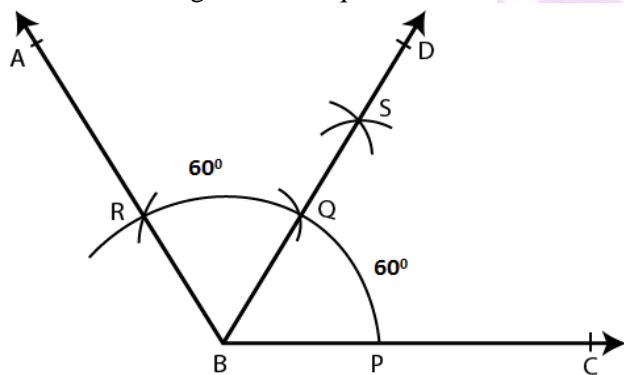
Steps of Construction:

1. Construct a line segment BC.
2. Taking B as centre and some suitable radius construct an arc which meets BC at the point P.
3. Taking P as centre and with same radius cut off the arcs PQ and QR.
4. Now join BR and produce it to point A
5. Taking P and R as centres construct two arcs which intersect each other at the point S.
6. Now join BS and produce it to point D.

Here BD is the bisector of  $\angle ABC$

By measuring each angle we get to know that is it  $60^\circ$

Yes, both the angles are of equal measure.



3. Draw a line segment PQ = 6 cm. Mark a point A in PQ so that AP = 2 cm. At point A, construct angle QAR =  $60^\circ$ .

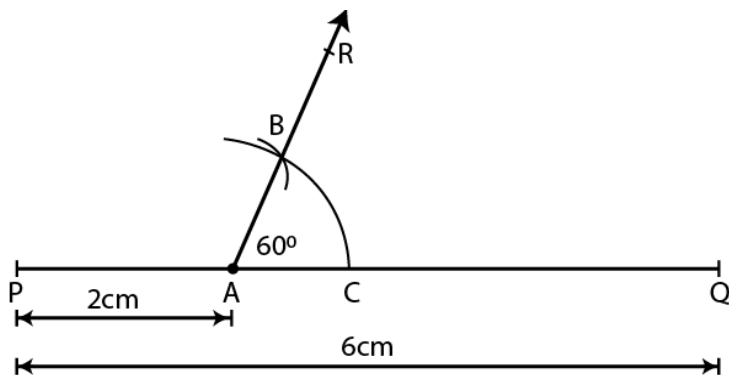
**Solution:**

Steps of Construction:

1. Construct a line segment PQ = 6cm.
2. Now mark point A on PQ so that AP = 2 cm.
3. Taking A as centre and some suitable radius construct an arc which meets AQ at the point C.
4. Taking C as centre and with same radius cut the arc CB.
5. Now join AB and produce it to point R.

$\angle QAR = 60^\circ$ .





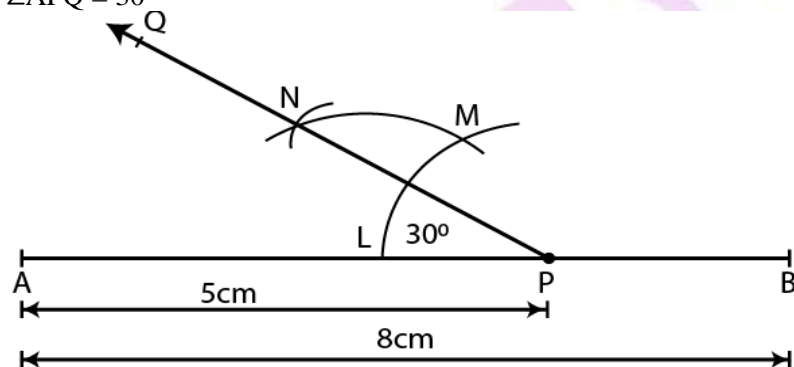
4. Draw a line segment  $AB = 8$  cm. Mark a point  $P$  in  $AB$  so that  $AP = 5$  cm. At  $P$ , construct angle  $APQ = 30^\circ$ .

**Solution:**

Steps of Construction:

1. Construct a line segment  $AB = 8$  cm.
2. Now mark the point  $P$  on  $AB$  such that  $AP = 5$  cm.
3. Taking  $P$  as centre and some suitable radius construct an arc which meets  $AB$  in  $L$ .
4. Taking  $L$  as centre and same radius cut the arc  $LM$ .
5. Now bisect the arc  $LM$  at the point  $N$ .
6. Join  $PN$  and produce it to point  $Q$ .

$\angle APQ = 30^\circ$



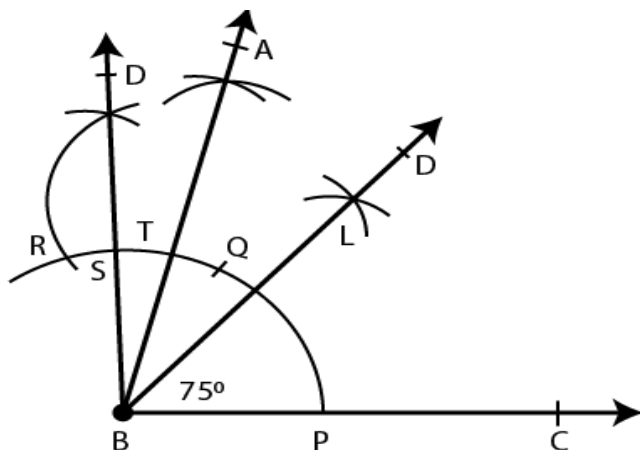
5. Construct an angle of  $75^\circ$  and then bisect it.

**Solution:**

Steps of Construction:

1. Construct a line segment  $BC$ .
2. At the point  $B$  construct an angle  $ABC$  which is equal to  $75^\circ$ .
3. Taking  $P$  and  $T$  as centres construct arcs which intersect each other at the point  $L$ .
4. Now join  $BL$  and produce it to point  $D$ .

Here  $BD$  bisects  $\angle ABC$ .

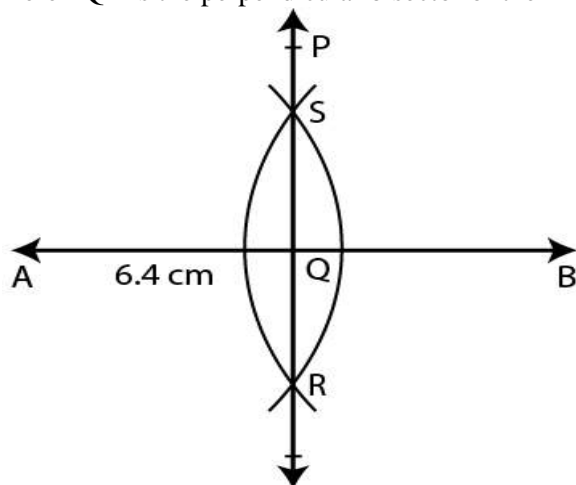


**6. Draw a line segment of length 6.4 cm. Draw its perpendicular bisector.**

**Solution:**

Steps of Construction:

1. Construct a line segment  $AB = 6.4$  cm.
  2. Taking A and B as centres and with some suitable radius construct arcs which intersect each other at the points S and R.
  3. Now join SR which intersects AB at the point Q.
- Here PQR is the perpendicular bisector of the line segment AB.



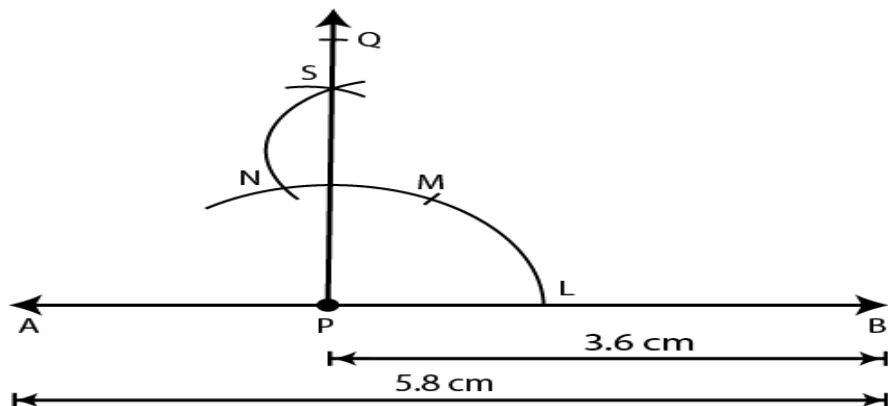
**7. Draw a line segment  $AB = 5.8$  cm. Mark a point P in AB such that  $PB = 3.6$  cm. At P, draw perpendicular to AB.**

**Solution:**

Steps of Construction:

1. Construct a line segment  $AB = 5.8$  cm.
2. Now mark a point P on the line segment AB such that  $PB = 3.6$  cm.
3. Taking P as centre and some suitable radius construct an arc which meets AB at the point L.
4. Taking L as centre and same radius cut off the arcs LM and then as N.
5. Now bisect the arc MN at the point S.
6. Join PS and produce it to point Q.

Here PQ is perpendicular to the line segment AB at point P.



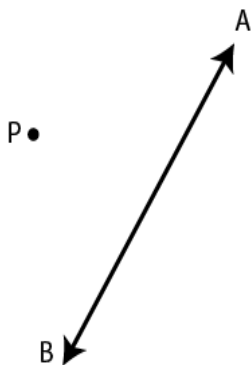
8. In each case, given below, draw a line through point P and parallel to AB:

(i)

P •



(ii)



(iii)

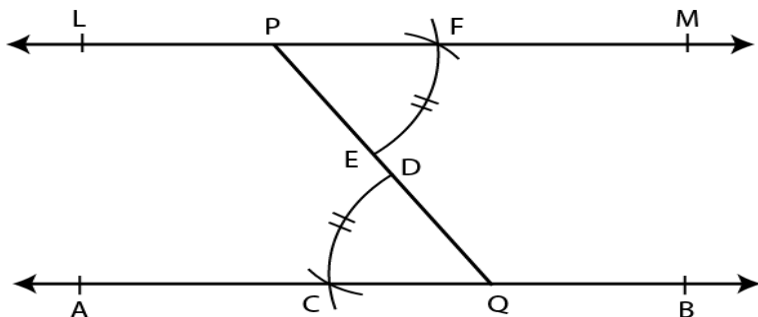


•P

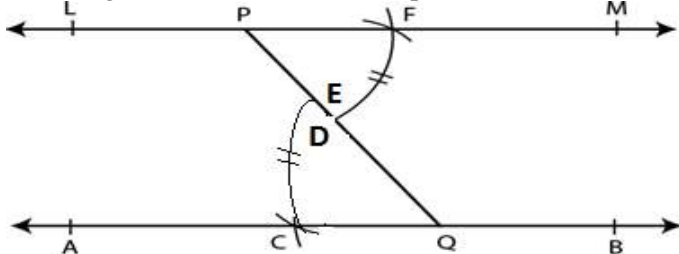
**Solution:**

Steps of Construction:

1. From the point P construct a line segment meeting AB
2. Taking Q as centre and some suitable radius construct an arc CD.
3. Taking P as centre and same radius construct another arc which meets PQ at the point E.



4. Taking E as centre and radius equal to CD cut this arc at the point F.



5. Now join PF and produce it to both sides to L and M.  
Here the line LM is parallel to the given line AB.

