

CBSE Class 12 Maths Question Paper 2020

Set 1

MATHS SET 1

General Instructions:

Read the following instructions very carefully and strictly follow them:

- (i) This question paper comprises **four** Sections A, B, C and D. This question paper carries **36** questions. **All** questions are compulsory.
- (ii) **Section A** – Questions no. **1 to 20** comprises of **20** questions of **1** mark each.
- (iii) **Section B** – Questions no. **21 to 26** comprises of **6** questions of **2** mark each.
- (iv) **Section C** – Questions no. **27 to 32** comprises of **6** questions of **4** mark each.
- (v) **Section D** – Questions no. **33 to 36** comprises of **4** questions of **6** mark each.
- (vi) There is no overall choice in the question paper. However, an internal choice has been provided in 3 questions of one mark, 2 questions of two marks, 2 questions of four marks and 2 questions of six marks. Only one of the choices in such questions have to be attempted.
- (vii) In addition to this, separate instructions are given with each section and question, wherever necessary.
- (viii) Use of calculators is **not** permitted.

SECTION – A

Question numbers 1 to 10 are multiple choice type questions. Select the correct option.

1. If A is a square matrix of order 3, such that $A(\text{adj } A) = 10I$ then $|\text{adj } A|$ is equal to
(a) 1 (b) 10 (c) 100 (d) 101
2. If A is a 3×3 matrix such that $|A| = 8$ then $|3A|$ equals
(a) 8 (b) 24 (c) 72 (d) 216
3. If $y = Ae^{5x} + Be^{-5x}$ then $\frac{d^2y}{dx^2}$ is equal to
(a) 25y (b) 5y (c) 0-25y (d) 15y
4. $\int x^2 \cdot e^{x^3} \cdot dx$ equals
(a) $\frac{1}{3}e^{x^3} + c$ (b) $\frac{1}{3}e^{x^4} + c$ (c) $\frac{1}{2}e^{x^3} + c$ (d) $\frac{1}{2}e^{x^2} + c$
5. If $\hat{i}, \hat{j}, \hat{k}$ are unit vectors along three mutually perpendicular directions, then
(a) $\hat{i} \cdot \hat{j} = 1$ (b) $\hat{i} \times \hat{j} = 1$ (c) $\hat{i} \cdot \hat{k} = 0$ (d) $\hat{i} \times \hat{k} = 0$
6. ABCD is a Rhombus whose diagonals intersect at E. Then $\overrightarrow{EA} + \overrightarrow{EB} + \overrightarrow{EC} + \overrightarrow{ED}$ equals
(a) 0 (b) \overrightarrow{AD} (c) $2\overrightarrow{BC}$ (d) $2\overrightarrow{AD}$

7. The lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{4-z}{K}$ and $\frac{x-1}{K} = \frac{y-4}{2} = \frac{z-5}{-2}$ are mutually perpendicular if the value of K is
- (a) $\frac{-2}{3}$ (b) $\frac{2}{3}$ (c) -2 (d) 2
8. The graph of the inequality $2x + 3y > 6$ is
- (a) half plane that contains the origin
 (b) half plane that neither contains the origin nor the points of the line $2x + 3y = 6$
 (c) whole xoy – plane excluding the points on the line $2x + 3y = 6$
 (d) entire xoy plane
9. A card is picked at random from a pack of 52 playing cards. Given that the picked card is queen. The probability of this card to be a card of spade is
- (a) $\frac{1}{3}$ (b) $\frac{4}{13}$ (c) $\frac{1}{4}$ (d) $\frac{1}{2}$
10. A die is thrown once. Let A be the event that the number obtained is greater than 3. Let B be the event that the number obtained is less than 5. Then $P(A \cup B)$ is
- (a) $\frac{2}{5}$ (b) $\frac{3}{5}$ (c) 0 (d) 1

Fill in the blanks in question numbers 11 to 15.

11. A relation in a set A is called identity relation, if each element of A is related to itself.

12. If $A + B = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ and $A - 2B = \begin{bmatrix} -1 & 1 \\ 0 & -1 \end{bmatrix}$ then $A =$ _____

13. The least value of the function $f(x) = ax + \frac{b}{x}, (a > 0, b > 0, x > 0)$ is _____

14. The integrating factor of the differential equation $x \cdot \frac{dy}{dx} + 2y = x^2$ is _____

(OR)

The degree of the differential equation $1 + \left(\frac{dy}{dx}\right)^2 = x$ is _____

15. The vector equation of a line which passes through the points $(3, 4, -7)$ and $(1, -1, 6)$ is _____

(OR)

The line of shortest distance between two skew lines is _____ to both the lines.

Question numbers 16 to 20 are of very short answer type questions.

16. Find the value of $\sin^{-1}\left[\sin\left(\frac{-17\pi}{8}\right)\right]$

17. For $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$ write A^{-1}

18. If the function f defined as $f(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & , x \neq 3 \\ K & , x = 3 \end{cases}$ is continuous at $x = 3$. Find the value of K .

19. If $f(x) = x^4 - 10$ then find approximate value of $f(2.1)$

(OR)

Find the slope of the Tangent to the curve $y = 2.\sin^2(3x)$ at $x = \pi/6$

20. Find the value of $\int_1^4 |x-5|.dx$

SECTION - B

Question numbers 21 to 26 carry 2 marks each.

21. If $f(x) = \frac{4x+3}{6x-4}, x \neq \frac{2}{3}$ then show that $f(df(x)) = x$ for all $x \neq \frac{2}{3}$, also write inverse of f .

(OR)

Check if the relation R in the set R of real numbers defined as $R = \{(a, b) : a < b\}$ is

(i) Symmetric (ii) Transitive

22. Find $\int \frac{x}{x^2 + 3x + 2}.dx$

23. If $x = a \cos \theta, y = b \sin \theta$ then find $\frac{d^2y}{dx^2}$

(OR)

Find the differential of $\sin^2 x$ w.r.t. $e^{\cos x}$

24. Evaluate $\int_1^2 \left[\frac{1}{x} - \frac{1}{2x^2} \right] e^{2x}.dx$

25. Find the value of $\int_0^1 x(1-x)^n .dx$

26. Given two independent events A and B such that $P(A) = 0.3$ and $P(B) = 0.6$. Find $P(A' \cap B')$

SECTION - C

Question numbers 27 to 32 carry 4 marks each.

27. Solve for x : $\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2}$

28. If $y = (\log x)^x + x^{\log x}$ then find $\frac{dy}{dx}$

29. Solve the differential equation

$$x \cdot \sin\left(\frac{y}{x}\right) \cdot \frac{dy}{dx} + x - y \cdot \sin\left(\frac{y}{x}\right) = 0$$

Given that $x = 1$ when $y = \frac{\pi}{2}$

30. If $\vec{a} = i + 2j + 3k$ and $b = 2i + 4j - 5k$ represent two adjacent sides of a parallelogram, find unit vectors parallel to the diagonals of the parallelogram.

(OR)

Using vectors, find area of the triangle ABC with vertices

$$A(1, 2, 3), B(2, -1, 4) \text{ and } C(4, 5, -1)$$

31. A company manufactures two types of novelty souvenirs made of plywood. Souvenirs of type A require 5 minutes each for cutting and 10 minutes each for assembling. Souvenirs of type B require 8 minutes each for cutting and 8 minutes each for assembling. There are 3 hours 20 minutes available for cutting and 4 hours for assembling. The profit is Rs.100 each for type A and Rs.120 each for type B souvenirs. How many souvenirs of each type should the company manufacture in order to maximize the profit. Formulate the problem as an LPP and solve it graphically.