Board Question Paper : March 2018

BOARD QUESTION PAPER : MARCH 2018 GEOMETRY

Time: 2 Hours

Note:

- i. Solve *all* questions. Draw diagrams wherever necessary.
- ii. Use of calculator is not allowed.
- iii. Figures to the right indicate full marks.
- iv. Marks of constructions should be distinct. They should not be rubbed off.
- v. Diagram is essential for writing the proof of the theorem.

1. Attempt any *five* sub-questions from the following :

- i. Δ DEF ~ Δ MNK. If DE = 5 and MN = 6, then find the value of $\frac{A(\Delta DEF)}{A(\Delta MNK)}$.
- ii. If two circles with radii 8 cm and 3 cm respectively touch externally, then find the distance between their centres.
- iii. Find the length of the altitude of an equilateral triangle with side 6 cm.
- iv. If $\theta = 45^\circ$, then find tan θ .
- v. Slope of a line is 3 and y intercept is -4. Write the equation of a line.
- vi. Using Euler's formula, find V, if E = 30, F = 12.

2. Attempt any *four* sub-questions from the following :

- i. The ratio of the areas of two triangles with common base is 4:3. Height of the larger triangle is 6 cm, then find the corresponding height of the smaller triangle.
- ii. In the following figure, point 'A' is the centre of the circle. Line MN is tangent at point M. If AN = 12 cm and MN = 6 cm, determine the radius of the circle.



iii. Draw $\angle PQR$ of measure 70° and bisect it.

iv. If $\cos \theta = \frac{3}{5}$, where ' θ ' is an acute angle. Find the value of $\sin \theta$.

- v. The volume of a cube is 1000 cm^3 . Find its side.
- vi. The radius and slant height of a cone are 4 cm and 25 cm respectively. Find the curved surface area of that cone. ($\pi = 3.14$)

3. Attempt any *three* sub-questions from the following :

- i. In the following figure, seg DH \perp seg EF and seg GK \perp seg EF. If DH = 6 cm, GK = 10 cm and A(\triangle DEF) = 150 cm², then find :
 - i. EF
 - ii. $A(\Delta \text{ GEF})$
 - iii. $A(\Box DFGE)$.



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ii. In the following figure, ray PA is the tangent to the circle at point A and PBC is a secant. If AP = 14, BP = 10, then find BC.



- iii. Draw the circle with centre C and radius 3.6 cm. Take point B which is at distance 7.2 cm from the centre. Draw tangents to the circle from point B.
- iv. Show that: $\sqrt{\frac{1-\sin x}{1+\sin x}} = \sec x \tan x.$
- v. Write the equation of the line passing through points C(4, -5) and D(-1, -2) in the form of ax + by + c = 0.

4. Attempt any *two* sub-questions from the following :

i. Prove that, "the lengths of the two tangent segments to a circle drawn from an external point are equal".

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- ii. A tree is broken by the wind. The top of that tree struck the ground at an angle of 30° and at a distance of 30 m from the root. Find the height of the whole tree. ($\sqrt{3} = 1.73$)
- iii. A(5, 4), B(-3, -2) and C(1,-8) are the vertices of a triangle ABC. Find the equation of median AD.

5. Attempt any *two* sub-questions from the following :

- i. Prove that, in a right-angled triangle, the square of hypotenuse is equal to the sum of the square of remaining two sides.
- ii. \triangle SHR ~ \triangle SVU, in \triangle SHR, SH = 4.5 cm, HR = 5.2 cm, SR = 5.8 cm and $\frac{\text{SH}}{\text{SV}} = \frac{3}{5}$.

Construct \triangle SVU.

iii. If 'V' is the volume of a cuboid of dimensions $a \times b \times c$ and 'S' is its surface area, then prove that:

$$\frac{1}{V} = \frac{2}{S} \left[\frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right].$$

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