Exercise Solutions

Question 1: When $1.0 \times 10^{12}$ electrons are transferred from one conductor to another, a potential difference of 10V appears between the conductors. Calculate the capacitance of the two-conductor system.

Solution:
The capacitance of a parallel plate Capacitor: $C = \frac{Q}{V}$ ...(1)

Here, $C =$ capacitance of the parallel plate capacitor

Where $Q$ is the charge on the capacitor and $V$ is the Voltage or potential difference.

Also, we know, $Q = ne = (1 \times 10^{12}) \times (1.6 \times 10^{-19}) = 1.6 \times 10^{-7} \text{ C}$

Therefore,

(1) => $C = \frac{1.6 \times 10^{-7}}{10} = 1.6 \times 10^{-8} \text{ F}$

Question 2: The plates of a parallel-plate capacitor are made of circular discs of radii 5.0 cm each. If the separation between the plates is 1.0 mm, what is the capacitance?

Solution:
Since capacitor plates are made of circular discs, so $A =$ area of the circle $= \pi r^2$.

Here $r = 5 \times 10^{-2}$

=> $A = \pi (5 \times 10^{-2})^2$

We know, Capacitance of the capacitor $= C = \frac{\varepsilon_0 A}{d}$

Where, $A =$ area of the plate

$\varepsilon_0 =$ Permittivity of free space $= 8.85 \times 10^{-12} \text{ F/m}$

$d =$ Separation between the plates

Now, $C = \frac{8.85 \times 10^{-12} \times 3.14 \times (5 \times 10^{-2})^2}{1.0 \times 10^{-3}}$

= $6.95 \times 10^{-5} \mu\text{F}$

Remember:

Parallel plate capacitor: When two conducting plates are connected in parallel and separated by some distance then parallel plate capacitor will be formed.
**Question 3:** Suppose, one wishes to construct a 1.0 farad capacitor using circular discs. If the separation between the discs be kept at 1.0 mm, what would be the radius of the discs?

**Solution:**

Here, \( C = 1 \, \text{F} \) and \( d = 1 \, \text{mm} \)

We know, Capacitance of the capacitor = \( C = \frac{\varepsilon_0 A}{d} \)

Where, \( A = \) area of the plate  
\( \varepsilon_0 = \) Permittivity of free space = \( 8.85 \times 10^{-12} \, \text{F/m} \)  
\( d = \) Separation between the plates

Since capacitor plates are circular discs, \( A = \pi r^2 \)

Now, \( C = \frac{\varepsilon_0 \pi r^2}{d} \)

Or \( r^2 = \frac{Cd}{\varepsilon_0 \pi} \)

\[
= \frac{[1 \times (1\times10^{-3})]}{[3.14 \times 8.85 \times 10^{-12}]}
\]

\[= 36 \times 10^6 \]

Or \( r = 6000 \, \text{m} = 6 \, \text{Km} \)

**Question 4:** A parallel-plate capacitor having plate area 25 cm² and separation 1.00 mm is connected to a battery of 6.0 V. Calculate the charge flown through the battery. How much work has been done by the battery during the process?

**Solution:**

Here Area, \( A = 25 \, \text{cm}^2 = 25 \times 10^{-4} \, \text{m}^2 \)  
Voltage = \( V = 6V \) and \( d = 1mm = 1 \times 10^{-3} \)

When a capacitor is connected to a capacitor, the charge is \( Q = CV \) ...(1)

Also, We know, Capacitance of the capacitor = \( C = \frac{\varepsilon_0 A}{d} \)

Where, \( A = \) area of the plate  
\( \varepsilon_0 = \) Permittivity of free space = \( 8.85 \times 10^{-12} \, \text{F/m} \)  
\( d = \) Separation between the plates

\[
=> C = \frac{[8.85 \times 10^{-12} \times 25 \times 10^{-4}]}{[1 \times 10^{-3}]} = 2.21 \times 10^{-11} \, \text{F} 
\]

When the capacitor is connected to a battery for voltage 6V, then flow of \( Q \) (Charge) from the battery is
same as the charge that the given capacitor have.

(1) \[ Q = 2.21 \times 10^{-11} \times 6 = 1.33 \times 10^{-10} \text{ C} \]

**Work is done by the battery:**

\[ W = \text{magnitude of the charge transferred} \times \text{voltage of the battery} \]

\[ => W = QV = 1.33 \times 10^{-10} \times 6 = 8.0 \times 10^{-10} \text{ J} \]

**Question 5:** A parallel-plate capacitor has plate area 25.0 cm\(^2\) and separation of 2.00 mm between the plates. The capacitor is connected to a battery of 12.0V.

a) Find the charge on the capacitor.

b) The plate separation is decreased to 1.00 mm. Find the extra charge given by the battery to the positive plate.

**Solution:**

a) Voltage = \( V = 12 \text{V} \); \( d = 2 \text{ mm} \)

Area = \( A = 25 \text{ cm}^2 = 25 \times 10^{-4} \text{ m}^2 \)

We know, Charge of the capacitor = \( Q = CV \)

Also, We know, Capacitance of the capacitor = \( C = \varepsilon_0 A/d \)

Where, \( \varepsilon_0 = \text{Permittivity of free space} = 8.85 \times 10^{-12} \text{ F/m} \)

\( d = \text{Separation between the plates} \)

\[ C = \frac{[8.85 \times 10^{-12} \times 25 \times 10^{-4}]}{[2 \times 10^{-3}]} = 11.06 \times 10^{-12} \text{ F} \]

Now, charge on the capacitor = \( Q = CV = 11.06 \times 10^{-12} \times 12 = 1.33 \times 10^{-10} \text{ C} \)

b) \[ C = \frac{[8.85 \times 10^{-12} \times 25 \times 10^{-4}]}{[1 \times 10^{-3}]} = 22.12 \times 10^{-12} \text{ F} \]

Now, charge on the capacitor = \( Q' = CV = 22.12 \times 10^{-12} \times 12 = 2.652 \times 10^{-10} \text{ C} \)

Therefore, Extra charge = \( Q' - Q = 2.652 \times 10^{-10} - 1.33 \times 10^{-10} = 1.33 \times 10^{-10} \text{ C} \)
Question 6: Find the charges on the three capacitors connected to a battery as shown in figure. Take $C_1 = 2.0 \ \mu F$, $C_2 = 4.0 \ \mu F$, $C_3 = 6.0 \ \mu F$ and $V = 12$ volts.

Solution:
All three capacitors are connected in parallel. So, equivalent capacitance is:

$$C_{\text{eq}} = C_1 + C_2 + C_3 = (2+4+6) = 12 \ \mu F = 12 \times 10^{-6} \ F$$

Let “Q” be the Charge of a capacitor, then $Q = C_{\text{eq}} \ V$

Find charge on each capacitor:

Charge on capacitor $C_1$:

$$Q_1 = C_1 \times V = 2 \times 12 = 24 \ C$$

Charge on capacitor $C_2$:

$$Q_2 = C_2 \times V = 4 \times 12 = 48 \ C$$

Charge on capacitor $C_3$:

$$Q_3 = C_3 \times V = 6 \times 12 = 72 \ C$$

Question 7: Three capacitors having capacitances 20 $\mu F$, 30 $\mu F$ and 40 $\mu F$ are connected in series with a 12 V battery. Find the charge on each of the capacitors. How much work has been done by the battery in charging the capacitors?

Solution:
All three capacitors are connected in series. So, equivalent capacitance is:

$$\frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

$$= \frac{C_1 C_2 C_3}{C_1 C_2 + C_2 C_3 + C_3 C_1}$$
= \frac{20 \times 30 \times 40}{20 \times 30 + 30 \times 40 + 40 \times 20}

=> \ C_{eq} = 9.23 \ \mu F

**Find charge on each capacitor:**

Let “Q” be the Charge of a capacitor, then \ Q = C_{eq} V

\ Q = 9.23 \times 12 = 110.76 \ \mu F

**Work done by the battery:**

\ W = QV = 110.76 \times 12 \times 10^{-6} = 1.33 \times 10^{-3} \ J

**Question 8:** Find the charge appearing on each of the three capacitors shown in the figure.

![Diagram of capacitors](https://byjus.com)

**Solution:**

Capacitors B and C are in parallel.

So, \ C_{eq} = C_B + C_C = 4 + 4 = 8 \ \mu F

Now, \ C_{eq} and C_A is series, so

\ \frac{1}{C} = \frac{1}{C_{eq}} + \frac{1}{C_A}

= \frac{1}{8} + \frac{1}{4}

= \frac{1}{4}

or \ C = 4 \ \mu F

System of A, B and C has the same capacitor values. So, exhibit the same potential difference between them.
The charge of the capacitor \( Q = CV \)

Charge flows through A \( Q_A = 8 \times 6 = 48 \mu C \)

Charge flows through B \( Q_B = 4 \times 6 = 24 \mu C \)

Charge flows through C \( Q_C = 4 \times 6 = 24 \mu C \)

**Question 9:** Take \( C_1 = 4.0 \mu F \) and \( C_2 = 6.0 \mu F \) in figure. Calculate the equivalent capacitance of the combination between the points indicated.

**Solution:**

In figure, (a)

\( C_1 \) and \( C_2 \) are in parallel.

\[
\Rightarrow \frac{1}{C_{eq}} = \frac{1}{C_1 + C_2} + \frac{1}{C_1 + C_2} = \frac{2}{C_1 + C_2}
\]

\[
= \frac{2}{4 + 6} = \frac{2}{10} = \frac{1}{5}
\]

\( C_{eq} = 5 \mu F \)

Form figure (b):

\[
\frac{1}{C_a} = \frac{1}{C_1 + C_2} + \frac{1}{C_1 + C_2} = \frac{1}{5}
\]

\( C_a = 5 \mu F \)

Also, \( C_b = 5 \mu F \)

Now, \( C_{eq} = C_a + C_b = 10 \mu F \)
Question 10: Find the charge supplied by the battery in the arrangement shown in the figure.

Solution:
Here, \( C_1 = 5 \ \mu F \) and \( C_2 = 6 \ \mu F \) and \( V = 10 \ V \)

The equivalent circuit for the given is:

Here, \( C_1 \) and \( C_2 \) are parallel, so

\[ C_{eq} = C_1 + C_2 = 5 + 6 = 11 \ \mu F \]

So, Charge supplied by battery \( Q = CV = 11 \times 10 = 110 \ \mu C \)

Question 11: The outer cylinders of two cylindrical capacitors of capacitance 2.2 \( \mu \)F each are kept in contact, and the inner cylinders are connected through a wire. A battery of emf 10V is connected as shown in the figure. Find the total charge supplied by the battery to the inner cylinders.
Solution:

Inner cylinders are connected through a wire and Outer cylinders kept in contact. The equivalent circuit for the given case is:

Consider, inner cylinders as A and B, and outer cylinders as A' and B'.

Now, Magnitude of the charge on each capacitor = $Q = CV = 2.2 \times 10 = 22 \mu C$

Inner cylinders of the capacitor are connected to the positive terminal of the battery. The charge on both the plates is same, i.e. $+22\mu C$

Net charge on the inner cylinders is $= 22\mu C + 22\mu C = +44\mu C$

Question 12: Two conducting spheres of radii $R_1$ and $R_2$ are kept widely separated from each other. What is their individual capacitance? If the spheres are connected by a metal wire, what will be the capacitance of the combination? Think in terms of series-parallel connections.
Solution:
Capacitance of the charged sphere can be found by imagining a concentric sphere of infinite radius consisting of \(-Q\) charge.

The capacitance of isolated charge sphere: \( C = 4\pi \varepsilon_o R \)

Capacitances of spheres of radii \( R_1 \) and \( R_2 \) are \( C_1 \) and \( C_2 \), respectively.

The capacitance of isolated charge sphere 1 = \( C_1 = 4\pi \varepsilon_o R_1 \)

The capacitance of isolated charge sphere 2 = \( C_2 = 4\pi \varepsilon_o R_2 \)

Since both the spheres are connected by a metal wire. So, the charge will flow one sphere to another up to their potential becomes the same when they are connected in parallel.

\( C_{eq} = C_1 + C_2 \)

\( = 4\pi \varepsilon_o (R_1 + R_2) \)

**Question 13:** Each of the capacitors shown in the figure has a capacitance of 2 \( \mu \)F. Find the equivalent capacitance of the assembly between the points A and B. Suppose, a battery of emf 60 volts is connected between A and B. Find the potential difference appearing on the individual capacitors.

Solution:

The equivalent capacitance of the first row: \( 1/c = 1/2 + 1/2 + 1/2 = 3/2 \)

\( => C = 2/3 \, \mu \)F

Similarly, capacitance of another rows is \((2/3) \, \mu \)F

All the three rows are arranged in parallel. So, Voltage or potential difference across each row is the same and is equal to 60V.

Voltage across each capacitor = 20V
Question 14: It is required to construct a 10 μF capacitor which can be connected across a 200V battery. Capacitors of capacitance 10 μF are available, but they can withstand only 50V. Design a combination which can yield the desired result.

Solution:

Let's assume some X capacitors are placed in series.

So, 50x = 200

=> x = 4 C

Construct 4 capacitors in a series to get the potential difference of 200V.

The capacitance of the parallel combination of four 10μF capacitors:

\[ \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \frac{1}{C_4} = \frac{4}{10} \]

\[ C = 2.5 \mu F \]

To get capacitor value 10 μF instead of only 2.5μF, add some more columns. Let us take Y as the columns, so

\[ 2.5Y = 10 \]

=> Y = 4 C

Add 4 columns as the same row, as shown below
Each capacitor value is 10 μF with voltage rating 50V.

**Question 15:** Take the potential of the point B in figure to be zero.

a) Find the potentials at the points C and D.

b) If a capacitor is connected between C and D, what charge will appear on this capacitor?

**Solution:**

Capacitors 4μF and 8μF are in series.

\[ C_1 = \frac{8}{3} \mu F \]

Capacitors 3μF and 6μF are in series

\[ C_2 = 2 \mu F \]

\[ C_1 \) and \( C_2 \) are in parallel combination. The voltage across each row is the same i.e. 50V.

we know, \( Q = CV \)
Now,

The Charge on the branch ACB with capacitance 8/3 \( \mu \text{F} \):

\[
Q = \frac{8}{3} \times 50 = \frac{400}{3} \, \mu\text{C}
\]

The Charge on the branch ADB with capacitance 2 \( \mu \text{F} \):

\[
Q = 2 \times 50 = 100 \, \mu\text{C}
\]

The potential at point D is

\[
V_D = \frac{q}{C_1} = \frac{100}{6} = \frac{50}{3} \, \text{V}
\]

In same way, potential at point C is \( V_C = \frac{50}{3} \, \text{V} \)

**Question 16:** Find the equivalent capacitances of the system shown in figure between the points a and b.

**Solution:**

From figure, \( C_1 \) and \( C_2 \) are in series. So,

Equivalent capacitance = \( C_a = \frac{1}{C_1} + \frac{1}{C_2} \)

\[
C_a = \frac{C_1 C_2}{C_1 + C_2}
\]

Similarly, \( C_b = \frac{C_1 C_2}{C_1 + C_2} \)

The capacitance \( C_a \), \( C_b \) and \( C_3 \) are connected in parallel combination across each other, so equivalent capacitance between a and b is \( C_{eq} \)

\[
C_{eq} = C_a + C_3 + C_b
\]

\[
= \frac{C_1 C_2}{C_1 + C_2} + C_3 + \frac{C_1 C_2}{C_1 + C_2}
\]

\[
= 2 \frac{C_1 C_2}{C_1 + C_2} + C_3
\]
Question 17: A capacitor is made of a flat plate of area A and the second plate having a stair-like structure as shown in the figure. The width of each stair is a, and the height is b. Find the capacitance of the assembly.

Solution:

Arrange all the capacitors in parallel, the equivalent figure is

Let "A" be the total area of the flat plate.
The width of each stair is the same.
Therefore, the area of each stair facing the flat plate is the same, i.e. A/3.

Here, the three capacitors are connected in parallel.

For capacitor C_1: Area of the plates = A/3 and the separation between the plates is d.

For capacitor C_2: Area of the plates = A/3 and the separation between the plates is (d + b).

For capacitor C_3: Area of the plates = A/3 and the separation between the plates is (d + 2b).

Capacitance among all the capacitors:
Capacitors are in parallel, so capacitance of the assembly of the capacitors:

\[ C_{eq} = C_1 + C_2 + C_3 \]

Substituting all the values. We get

\[ C_{eq} = \frac{3d^2 + 6bd + 2b^2}{d(d+b)(d+2b)} \]

**Question 18:** A cylindrical capacitor is constructed using two coaxial cylinders of the same length 10 cm and of radii 2 mm and 4 mm.

a) Calculate the capacitance.

b) Another capacitor of the same length is constructed with cylinders of radii 4 mm and 8 mm. Calculate the capacitance.

**Solution:**

(a)

We know, capacitance of the cylindrical capacitor is

\[ C = \frac{2\pi\varepsilon_0 l}{\ln\left(\frac{R_2}{R_1}\right)} \]

\[ l = \text{length of the cylinder} \]
\[ R_1 = \text{radius of inner cylinder} \]
\[ R_2 = \text{radius of outer cylinder} \]
\( \varepsilon_0 = \text{permittivity of the free space} = 8.85 \times 10^{-12} \text{ Fm}^{-1} \)

Given: \( R_1 = 2 \text{ mm} \); \( R_2 = 4 \text{ mm} \); \( l = 10 \text{ cm} \)

On putting values, we get

\[
C = \frac{2 \times 3.14 \times 8.85 \times 10^{-12}}{\ln(4/2)} = 8 \text{ pF}
\]

(b) If we compare the radii in both the parts, we get same ratio

\[
\frac{R_2}{R_1} = \frac{4}{2} = \frac{8}{4}
\]

=> 2 = 2

Which means capacitance is also same i.e. 8 pF

**Question 19:** A 100 \( \mu \text{F} \) capacitor is charged to a potential difference of 24V. It is connected to an uncharged capacitor of capacitance 20 \( \mu \text{F} \). What will be the new potential difference across the 100 pF capacitor?

**Solution:**

We know, \( Q = CV \)

=> \( Q = 100 \times 10^{-6} \times 24 = 2.4 \text{ mC} \)

This capacitor is connected to an uncharged capacitor of \( C_2 = 20 \mu \text{F} \)

Total charge = 2.4 + 0 = 2.4 mC

And, the potential difference across both capacitors will be the same.

=> \( \frac{Q_1}{C_1} = \frac{Q_2}{C_2} \)

=> \( \frac{Q_1}{100} = \frac{Q_2}{20} \)

=> \( Q_1 = 5Q_2 \)

Total charge = \( Q_1 + Q_2 \)

=> 2.4 = \( Q_1 + Q_2/5 \)

=> \( Q_1 = 2 \text{ mC} \)
New potential difference \( = \frac{Q_1}{C_1} = \frac{2}{100} = 20 \text{ V} \)

**Question 20:** Each capacitor shown in the figure has a capacitance of 5.0 μF. The emf of the battery is 50V. How much charge will flow through AB if the switch S is closed?

**Solution:**

Case 1: Switch S is open.

The equivalent capacitance \( C_{eq} = \frac{2C_1C_2}{3C_1} = \frac{2}{3} \times 5 \text{ μF} \)

And the charge supplied by battery: \( Q_1 = C_{eq}V \)

\[ \Rightarrow Q_1 = \left(\frac{2}{3}\right) \times 5 \times 50 = \frac{500}{3} \text{ μC} \]

Case 2: Switch S is Closed.

No current will flow through capacitor at switch. Now there will be only two capacitors which are in parallel. Thus, equivalent capacitance \( C_{eq} = C_1 + C_2 \)

\[ = 5 + 5 = 10 \text{ μF} \]

And the charge supplied by battery: \( Q_2 = C_{eq}V = 10 \times 50 = 500 \text{ μC} \)

Note: Here \( Q_1 \) will be negative because the capacitor is discharging.

Now, the charge flows from A to B is:

\[ Q_{net} = Q_1 + Q_2 = -\frac{500}{3} + 500 = -3.3 \times 10^{-4} \text{ C} \]

**Question 21:** The particle P shown in figure has a mass of 10 mg and a charge of \(-0.01 \text{ μC}\). Each plate has a surface area 100 cm\(^2\) on one side. What potential difference \( V \) should be applied to the combination to hold the particle P in equilibrium?
Solution:

\[ m = 10 \text{ mg} \]

Charge of the particle = \( q = -0.01 \mu C = -0.01 \times 10^{-6} \text{ C} \)

Area of each capacitor plate = \( A = 100 \text{ cm}^2 = 100 \times 10^{-4} \text{ m}^2 \)

capacitance of each pair of the parallel capacitor plates = \( C = 0.04 \mu F = 0.04 \times 10^{-6} \text{ F} \)

The particle is balanced when electrical force on it is balanced by its weight.

\[ mg = qE = qV'/d \quad ...(1) \]

Where, \( V' \) = potential difference across the capacitor contained by particle

We know, capacitance of capacitor = \( C = \varepsilon_0 A/d \quad \ldots(2) \)

using (2) in (1), we get

\[ mg = qV' \times C/\varepsilon_0 A \]

or \( V' = mg \varepsilon_0 A/qC \)

\[ = \frac{[10^{-6} \times 9.8 \times 8.85 \times 10^{-12} \times 100 \times 10^{-4}]}{[0.01 \times 10^{-6} \times 0.04 \times 10^{-6}]} \]

\[ = 21.68 \text{ mV} \]

AS value of both the capacitors are equal, so

\[ V = 2V' = 2 \times 21.68 = 43 \text{ mV} \text{ (approx)} \]

**Question 22:** Both the capacitors shown in the figure are made of square plates of edge a. The separations between the plates of the capacitors are \( d_1 \) and \( d_2 \) as shown in the figure. A potential difference \( V \) is applied between the points a and b. An electron is projected between the plates of the upper capacitor along the central line. With what minimum speed should the electron be projected so that it does not
collide with any plate? Consider only the electric forces.

Solution:
Let us rearrange the figure,

Area of each plates = $a^2$, where $a$ = length of each plate

Horizontal distance, $x = ut$ ...(1)

Let $E$ be the electric field inside the capacitor

Acceleration of the electron = $qE/m$

Vertical distance = $y = \frac{1}{2}qE/m \cdot t^2 = \frac{1}{2}qE/m \cdot (x/u)^2$ ....

$Y = d_1/2$ and $x = a$

d_1/2 = $\frac{1}{2} \cdot qE/m \cdot (a/u)^2$ ....(2)

capacitance of two capacitors which are connected in series:
\[ C_1 = \frac{\epsilon_0 a^2}{d_1} \quad \text{and} \quad C_2 = \frac{\epsilon_0 a^2}{d_2} \]

\[ C_{eq} = \frac{C_1 C_2}{C_1 + C_2} \]

On putting values, we get

\[ C_{eq} = \frac{\epsilon_0 a^2}{d_1 + d_2} \]

Total charge on the system of capacitors = \( Q = C_{eq} V = \frac{\epsilon_0 a^2 V}{d_1 + d_2} \)

The potential difference across the capacitor containing the electron = \( V = \frac{Q}{C_1} \)

On substituting the values of \( Q \) and \( C_1 \), we get

\[ V = \frac{d_1}{d_1 + d_2} \]

Magnitude of electric field inside the capacitor = \( E = \frac{V}{d_1} = \frac{V}{(d_1 + d_2)} \)

Charge on electron \( q \) is shown as \( e \)

On putting the values of \( q \) and \( E \) in (2)

\[ \frac{d_1}{2} = \frac{1}{2} \frac{qV}{m(l_1 + l_2)} \times (a/u)^2 \]

on rearranging, we have the value of \( v \),

\[ v = \left[ \frac{Ve a^2}{m d_1 (d_1 + d_2)} \right]^{1/2} \]

**Question 23:** The plates of a capacitor are 2.00 cm apart. An electron-proton pair is released somewhere in the gap between the plates and it is found that the proton reaches the negative plate at the same time as the electron reaches the positive plate. At what distance from the negative plate was the pair released?

**Solution:**

Let "\( E \)" be the electric field inside the capacitor.

The distance in between the capacitor plates is 2 cm (Given)

Let \( m_p, m_e \) be the mass and \( q_p, q_e \) be the charge of proton and electron respectively.
Magnitude of acceleration of the electron: \( a_e = \frac{(q_e E)}{m_e} \)

Magnitude of acceleration of the proton: \( a_p = \frac{(q_p E)}{m_p} \)

Vertical distance travelled by proton to reach the negatively charged plate, say \( x \) cm. Thus, \((2-x)\) cm distance travelled by electron.

This implies,

\[ x = \frac{1}{2} \left( \frac{q_p E}{m_p} \right) x t^2 \quad \text{and} \quad 2 - x = \frac{1}{2} \left( \frac{q_e E}{m_e} \right) x t^2 \]

Where "\( t \)" be the time taken by the electron and proton to reach the positive and negative plates, respectively.

[Initial velocities of the proton and electron are zero.]

Divide above equations, to find the distance travelled by proton:

\[ \frac{x}{2-x} = \frac{\frac{1}{2} \frac{q_p E}{m_p} x t^2}{\frac{1}{2} \frac{q_e E}{m_e} x t^2} \]

\[ \frac{x}{2-x} = \frac{m_e}{m_p} \]

[Since charge of proton \( q_p \) = charge of electron \( q_e \)]

Mass of electron, \( m_e = 9.1 \times 10^{-31} \) kg

Mass of proton, \( m_p = 1.67 \times 10^{-27} \) kg

Substituting the above values, we get

\[ x = 1.08 \times 10^{-3} \text{ cm} \]

**Question 24:** Convince yourself that parts (a), (b) and (c) of figure are identical. Find the capacitance between the points A and B of the assembly.
Solution:
Given figures (a), (b) and (c) are identical. In this bridge circuit, two electrical paths are branched in parallel between the same potential difference, but are bridged by a third path, from intermediate points.

Here capacitors of 1 µF and 2 µF are connected to terminal A and the 5 µF capacitor and capacitors of 3 µF and 6 µF are connected to terminal B and the 5 µF capacitor.

Form given, No current will flow through the 5 µF capacitor as bridge is in balance.

To simplify the circuit, let us remove 5 µF capacitor from the circuit.

Now, remaining 1 µF and 3 µF capacitors are in one series. And 2 µF and 6 µF capacitors are in another series. Results of both the series are in parallel.

The equivalent capacitance in each of the arrangement: \[ C_{eq} = \frac{(1\times3)}{(1+3)} + \frac{(2\times6)}{(2+6)} = 2.25 \mu F \]

Thus, for all cases, equivalent capacitance of the circuit remains constant.

**Question 25:** Find the potential difference \( V_a - V_b \) between the points a and b shown in each part of the figure.
Solution:
(a)

\[ q = q_1 + q_2 \] \hspace{1cm} (1)

Let's apply Kirchhoff's voltage law in loop CabDC and in loop DCBAD

\[ \frac{q_2}{2} + \frac{q_2}{4} - \frac{q_1}{4} = 0 \]

\[ \Rightarrow 3q_2 = q_1 \] \hspace{1cm} (2)

And

\[ \frac{q}{2} + \frac{q_1}{4} - 12 = 0 \]

\[ \Rightarrow 3q_1 + 2q_2 = 48 \] \hspace{1cm} (3)

Solving (2) and (3), we get

\[ q_2 = 48/11 \]
Again,

\[ V_a - V_b = \frac{q_2}{4\mu F} = \frac{48}{44} = \left(\frac{12}{11}\right) V \]

(b)

\[ \frac{q}{2} + \frac{q}{4} - 24 - 12 = 0 \]

Where \( q \) be the charge in the loop.

\[ 3\frac{q}{4} = 12 \]

\[ q = 16 \mu C \]

\[ V_a - V_b = -\frac{q}{2} = -8V \text{ (putting value of } q) \]

(c)

\[ V_a - V_b = 2 - \frac{(2-q)}{2\mu F} \]

In the loop, we have
2 + 2 - q/2 - q/2 = 0

=> Q = 4C

V_a - V_b = 2 - 4/2 = 0

(d)

Net charge and net capacitance through all the branches:

q = 3x24 = 72 μC and C = 4+2+1 = 7μF

Total potential difference between a and b V = q/C = 72/7 = -10.3 V
[-ve sign due to negative terminals of the batteries connected to point a]