







So, the first term = 4

Sum of two terms =  $3 * 2^2 + 2 = 14$

2<sup>nd</sup> term =  $14 - 4 = 10$

For finding  $d = 10 - 4 = 6$

Or

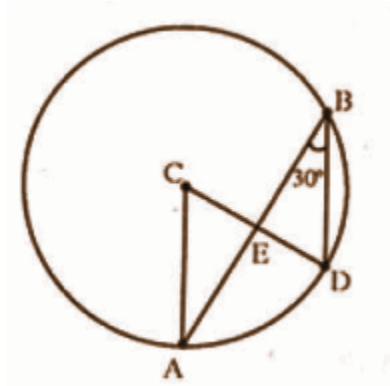
Sum of coefficients of  $n^2$  and  $n = 3 + 1 = 4$

The first term = 4

Double the coefficient of  $n^2$  is a common difference.

So,  $d = 6$ .

### Question 7:

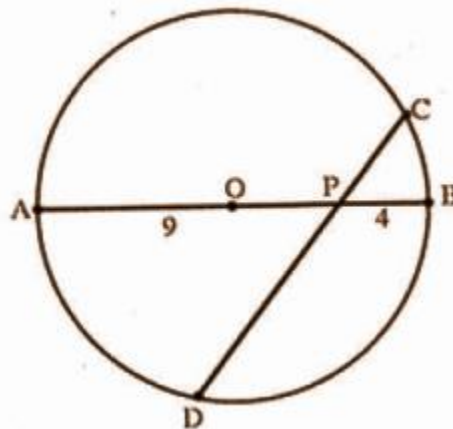


In the figure, O is the centre of the circle and  $\angle ABD = 30^\circ$ .

[a] What is the measure of  $\angle ACD$ ?

[b] If  $\angle ABD = \angle CAB$  and  $AB = 6\text{cm}$ , find the radius of the circle.

OR



In the figure, O is the centre of the circle. CD is the chord which is not perpendicular to the diameter AB. PA = 9cm and PB = 4cm.

[a] What is PC \* PD?

[b] Show that the length of PC and PD cannot be natural numbers at a time.

**Solution:**

[a]  $\angle ACD = 60^\circ$

[b] CE bisects AB or  $\angle AEC = 90^\circ$

Using the property of  $30^\circ, 60^\circ, 90^\circ$  triangle,

$$AC = 2\sqrt{3}$$

The radius of the circle =  $2\sqrt{3}$  cm

**OR**

[a]  $PC \times PD = 9 \times 4 = 36$

[b] If  $PC \times PD = 9 \times 4 = 36$  then natural number values of PC and PD are (1, 36), (2, 18), (3, 12), (4, 9), (6, 6). Here the longest chord or diameter is 13cm. So, (1, 36), (2, 18), (3, 12) are not acceptable values for PC and PD. CD is not a diameter hence it cannot be 13cm. So, (4, 9) is also not acceptable. CD is not perpendicular to AB, hence (6, 6) is also not acceptable. So the length of PC and PD cannot be natural numbers

**Question 8:**



There is a mark on the outermost part of the wheel of radius 30cm. Now the mark is close to the ground as shown in the figure. If the wheel rolls 31.4 cm on a straight line, then

[a] Find the angle by which the wheel rotates.

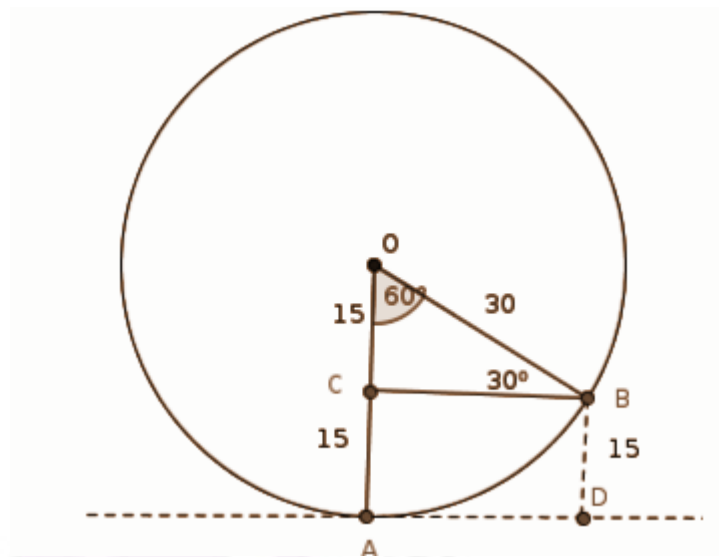
[b] What will be the height of the mark from the ground?

**Solution:**

[a] For finding the circumference of the wheel =  $2\pi r$   
=  $2 \times 3.14 \times 30$   
= 188.4cm

The wheel rolls 31.4cm it rotates  $1/6$  part of its circumference.  
Angle =  $1/6 \times 360$   
=  $60^\circ$

[b]



$\angle O = 60^\circ$

$\angle OBC = 30^\circ$ ,  $OB = 30$  cm

$OC = 15$  cm

$\Rightarrow AC = 15$  cm

$\Rightarrow BD = 15$  cm

The height of the mark from the ground = 15cm.

[10 \* 4 =

40]

**Question 9:** A box contains 8 black beads and 12 white beads. Another box contains 9 black beads and 6 white beads. One bead from each box is taken.

[a] What is the probability that both the beads are black?

[b] What is the probability of getting one black and one white bead?

**Solution:**

Total number of pairs =  $20 \times 15 = 300$

The probability that both beads are black =  $72 / 300$   
 $= 6 / 25$

The probability that both beads are white =  $72 / 300$   
 $= 6 / 25$

The probability of getting one black and one white bead =  $156 / 300$   
 $= 13 / 25$

**Question 10:** Write the polynomial  $3x^2 - 5x - 2$  as a product of two first degree polynomials.

**Solution:**

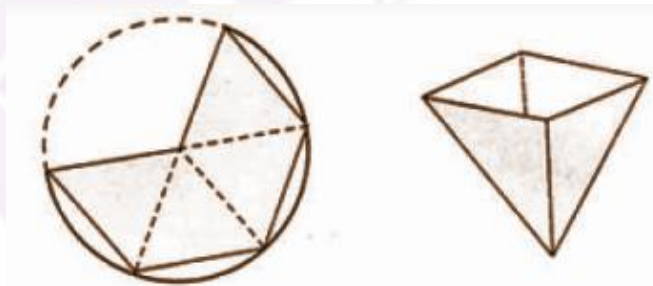
$$3x^2 - 5x - 2$$

$$= 3x^2 - 6x + x - 2$$

$$= 3x(x - 2) + (x - 2)$$

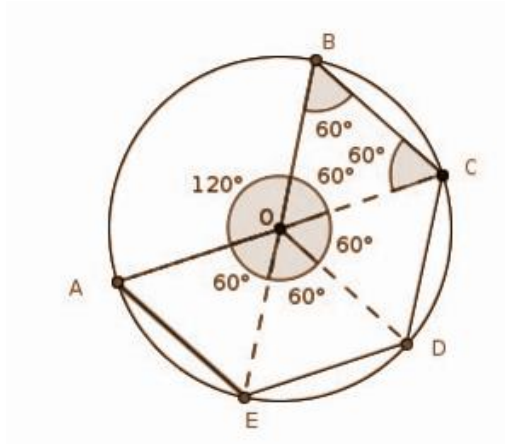
$$= (3x + 1)(x - 2)$$

$$x = 2, -1 / 3$$

**Question 11:**

From a tin sheet, a sector of radius 20cm and central angle  $240^\circ$  is divided into 4 equal parts as shown in the figure. The shaded portion is cut off. Using this, a vessel in the shape of a square pyramid is made. What is the capacity of this vessel?

**Solution:**



In  $\triangle OBC$ ,

$$\angle O = \angle B = \angle C = 60^\circ$$

$$OB = BC = OC = 20 \text{ cm}$$

$$e = 20 \text{ cm}$$

$$a = 20 \text{ cm} \Rightarrow d = 20\sqrt{2}$$

$$h^2 = e^2 - (d/2)^2 = 20^2 - (10\sqrt{2})^2$$

$$= 400 - 200$$

$$= 200$$

$$h = \sqrt{200} = 10\sqrt{2} \text{ cm}$$

$$\text{Volume} = [1/3] a^2 h$$

$$= [1/3] \times 20^2 \times 10\sqrt{2}$$

$$= 4000\sqrt{2} / 3 \text{ cm}^3$$

**Question 12:** The table below shows the classification of students participated in a camp, according to their height. Calculate the mean height of the students.



Height (cm) -	Number of students
130-135	8
135-140	12
140-145	20
145-150	28
150-155	32
155-160	22
160-165	16
165-170	12

**Solution:**

Height	Number of students (f)	Mid Value (x)	$\Sigma fx$
130 - 135	8	132.5	1060
135 - 140	12	137.5	1650
140 - 145	20	142.5	2850
145 - 150	28	147.5	4130
150 - 155	32	152.5	4880
155 - 160	22	157.5	3465
160 - 165	16	162.5	2600
165 - 170	12	167.5	2010
	<b>150</b>		<b>22645</b>

$$\text{Mean} = 22645 / 150 = 150.97$$

**Question 13:**

[a] What is the volume of a solid metal cylinder of height 4cm and radius 5cm?

[b] The solid is melted and recast into 5 cones of equal height and radius 2cm. Find the height of such a cone.

OR

A tank is in the shape of a cylinder with two hemispheres attached to both ends as shown in the figure.



Its common diameter is 2m and total length is 8m. Find the total cost of painting the outer surface of this tank at the rate of 60 rupees per square meter.

**Solution:**

$$\begin{aligned} \text{[a] Volume of cylinder} &= \pi r^2 h \\ &= \pi \times 5 \times 5 \times 4 \\ &= 100\pi \text{ cubic cm} \end{aligned}$$

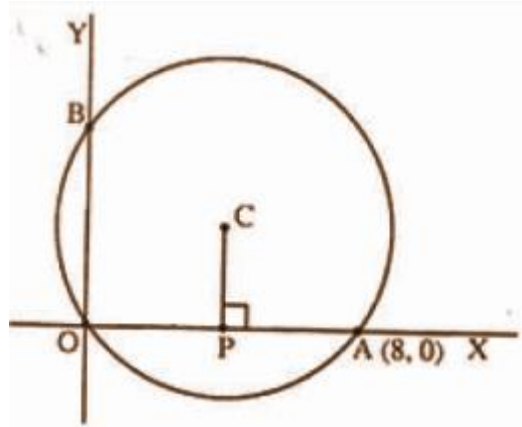
$$\begin{aligned} \text{[b] Volume of 5 cones} &= 5 \times \frac{1}{3} \pi r^2 h \\ \text{Volume of cylinder} &= \text{volume of 5 cones} \\ \text{To find the height of one cone} &= 15\text{cm} \end{aligned}$$

OR

$$\begin{aligned} \text{Curved surface area of 2 hemispheres} &= 2 \times 2\pi r^2 = 4\pi \text{ sq.m} \\ \text{Curved surface area of cylinder} &= 2\pi r h = 2 \times \pi \times 1 \times 6 = 12\pi \text{ sq.m} \\ \text{Total area to be painted} &= 4\pi + 12\pi = 16\pi \text{ sq.m} \end{aligned}$$

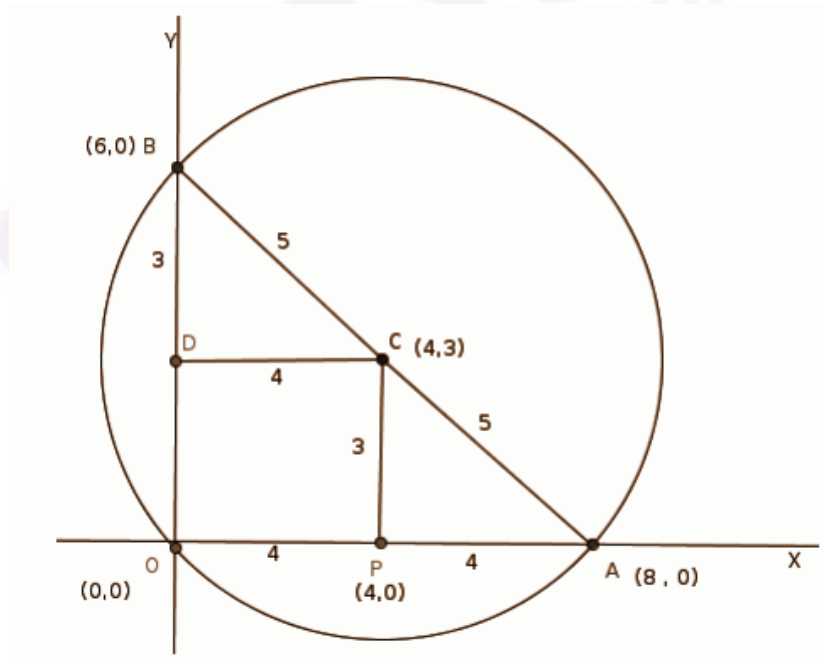
Cost of painting =  $16 \times 3.14 \times 60 = \text{Rs.}3014.40$

**Question 14:**



In the figure, the radius of the circle centred at C is 5. The circle passes through point A (8, 0). If PC is perpendicular to the x-axis, find the coordinates of the points P, B and C.

**Solution:**



$$OA = 8$$

$$OP = 4$$

$$\Rightarrow P(4, 0)$$

$$AC = 5, PA = 4$$

$$\Rightarrow PC = 3$$

$$\Rightarrow C(4, 3)$$

$$CD = 4, BC = 5$$

$$\Rightarrow BD = 3$$

$$\Rightarrow B(6, 0)$$

**Question 15: The terms of an arithmetic sequence with common difference 4 are natural numbers.**

**[a] If  $x$  is a term in this sequence, what is the next term?**

**[b] If the sum of the reciprocals of two consecutive terms of this sequence is  $4/15$ , find those terms.**

**OR**

**[a] Lengths of sides of a right-angled triangle are in arithmetic sequence with common difference  $d$ . If the length of the smallest side of the triangle is  $x - d$ , write the length of its other two sides.**

**[b] Show that any right-angled triangle with sides in an arithmetic sequence is similar to the right-angled triangle with sides 3, 4 and 5.**

**Solution:**

[a] The next term =  $x + 4$

$$[b] \frac{1}{x} + \frac{1}{x+4} = \frac{4}{15}$$

$$\frac{(x+4+x)}{x(x+4)} = \frac{4}{15}$$

$$\frac{(2x+4)}{(x^2+4x)} = \frac{4}{15}$$

$$4(x^2+4x) = 15(2x+4)$$

$$4x^2 + 16x = 30x + 60$$

$$4x^2 + 16x - 30x - 60 = 0$$

$$4x^2 - 14x - 60 = 0$$

$$2x^2 - 7x - 30 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{(7 \pm \sqrt{49 + 240})}{4}$$

$$= (7 \pm 17) / 4$$

$$x = 6 \text{ and } x = -5 / 2$$

**OR**

[a] The lengths of the other two sides are  $x$ ,  $x+d$ .

[b] By Pythagoras theorem,

$$(x - d)^2 + x^2 = (x + d)^2$$

$$x^2 - 2xd + d^2 + x^2$$

$$\Rightarrow x^2 + 2xd + d^2$$

$$\Rightarrow x^2 - 4xd = 0$$

$$x(x - 4d) = 0$$

$$x = 0 \text{ or } x = 4d$$

Length of the sides are,

$$x - d = 4d - d = 3d$$

$$x = 4d$$

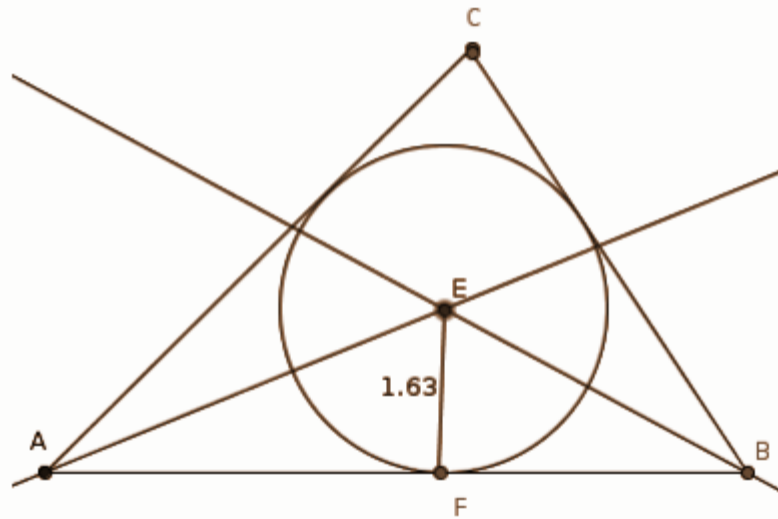
$$x + d = 4d + d = 5d$$

Hence the sides  $3d$ ,  $4d$ ,  $5d$  are similar to pythagorean triplet sides 3, 4, 5.

**Question 16: Draw a triangle of sides 5cm, 6cm and 7cm. Draw its incircle.**

**Measure and read the radius of the incircle.**

**Solution:**



Radius of the incircle = 1.6 cm.

**Question 17: A line of slope 2 passes through the point A (1, 3).**

**[a] Check whether the B(3, 7) is a point on this line.**

**[b] Write down the equation of this line.**

**[c] Find the coordinates of a point C on the line such that  $BC = 2AB$ .**

**Solution:**

The slope of the line is 2 and passes through A(1, 3)

$$[y - 3] / [x - 1] = 2$$

$$y - 3 = 2x - 2$$

$$y = 2x + 1$$

[a] For point B(3, 7)

$$2(3) + 1 = 7$$

Hence the point B (3, 7) lies on the line  $y = 2x + 1$ .

[b] Equation of the line is  $y = 2x + 1$ .

[c] Let  $(x_1, y_1)$  be the coordinates of point C on line.

Therefore it satisfies the equation of line a  $y = 2x + 1$ .

$$BC = 2AB$$

$$\Rightarrow \sqrt{(x_1 - 3)^2 + (y_1 - 7)^2} = 2\sqrt{(3 - 1)^2 + (7 - 3)^2}$$

On squaring both sides,

$$(x_1 - 3)^2 + (y_1 - 7)^2 = 4[(3 - 1)^2 + (7 - 3)^2]$$

$$5(x_1 - 3)^2 = 80$$

$$(x_1 - 3)^2 = 16$$

$$x_1 - 3 = \pm 4$$

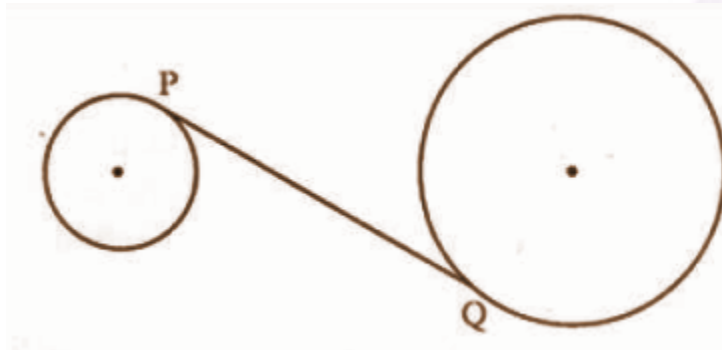
$$x_1 = 7 \text{ or } -1$$

$$y_1 = 2x_1 + 1 = 2(7) + 1 = 15$$

$$y_1 = 2x_1 + 1 = 2(-1) + 1 = -1$$

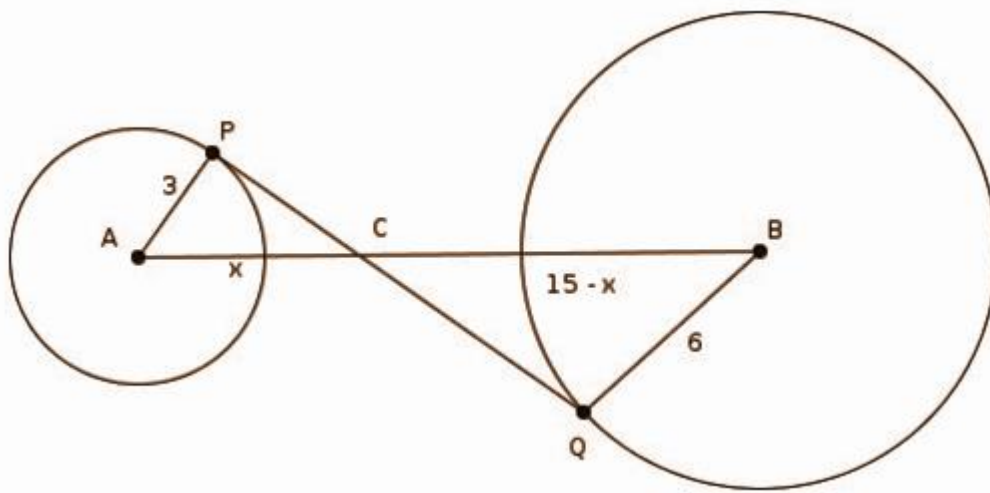
The coordinates of point C are (7, 15) or (-1, -1).

**Question 18:**



**In the figure, the radius of the smaller circle is 3cm, that of the bigger circle is 6cm and the distance between the centres of the circles is 15cm. PQ is a tangent to both circles. Find its length.**

**Solution:**



In  $\triangle APC$  and  $\triangle BQC$

$$\angle P = \angle Q = 90^\circ$$

$$\angle ACP = \angle BCQ$$

$$\triangle APC \sim \triangle BQC$$

$$AP / AC = BQ / BC$$

$$3 / x = 6 / 15 - x$$

$$6x = 3(15 - x)$$

$$= 45 - 3x$$

$$9x = 45$$

$$x = 5$$

$$AP = 3 \text{ cm}, AC = 5 \text{ cm}$$

$$\Rightarrow PC = 4 \text{ cm}$$

$$BQ = 6 \text{ cm}, BC = 10 \text{ cm}$$

$$\Rightarrow QC = 8 \text{ cm}$$

$$PQ = PC + QC$$

$$= 4 + 8$$

$$PQ = 12 \text{ cm}$$

**Question 19: Consider the arithmetic sequence 9, 15, 21,.....**

**[a] Write the algebraic form of this sequence.**

**[b] Find the 25<sup>th</sup> term of this sequence.**

**[c] Find the sum of terms from 25<sup>th</sup> to 15<sup>th</sup> of this sequence.**

**[d] Can the sum of some terms of this sequence be 2015? Why?**

**Solution:**

The sequence is 9, 15, 21, .....

First term =  $a = 9$

Common difference =  $d = 15 - 9 = 6$

[A] For natural number  $n$

$n^{\text{th}}$  term =  $[(n - 1) \times 6] + 9 = 6n + 3$  where  $n = 1, 2, 3, \dots$

Hence the algebraic form of sequence 9, 15, 21,..... is  $x_n = 6n + 3$ .

[B]  $n^{\text{th}}$  term =  $6n + 3$

25<sup>th</sup> term =  $6(25) + 3$



$$= 150 + 3$$
$$= 153$$

[C] Sum of first n terms is given by,

$$S_n = [1 / 2] n [X_1 + X_n]$$

Sum of 24 terms is

$$S_{24} = [1 / 2] n [X_1 + X_{24}]$$

$$= 24 / 2 [9 + 147]$$

$$= 1872$$

Sum of 50 terms is

$$S_{50} = [1 / 2] n [X_1 + X_{50}]$$

$$= [50 / 2] [9 + 6 (50) + 3]$$

$$= 7800$$

Sum of terms from twenty fifth to fiftieth

$$= S_{50} - S_{24}$$

$$= 7800 - 1872$$

$$= 5928$$

[D] Let the sum of first n terms is 2015,

$$S_n = [1 / 2] n [X_1 + X_n]$$

$$2015 = [1 / 2] n [9 + 6n + 3]$$

$$2015 = 3n^2 + 6n$$

$$n = -1 \pm \sqrt{(6054)/3}$$

$$n = -26.94, 24.94$$

The values of n are not natural numbers.

Hence 2015 cannot be the sum of some terms of this sequence.

**Question 20: In triangle ABC, AB = 5cm,  $\angle A = 80^\circ$ ,  $\angle B = 70^\circ$ . Calculate the radius of the circumcircle and length of the other 2 sides.**

**OR**

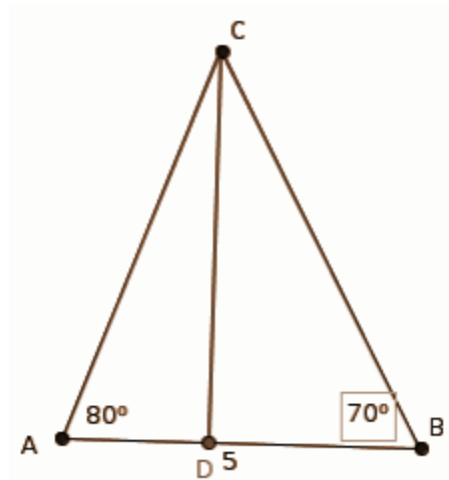
**Gopi and Gautham stand on opposite sides of a tower. The children and the tower are on a straight line. Gopi sees the top of the tower at an angle of**

elevation of  $36^\circ$  and Gautham sees it at an angle of elevation of  $52^\circ$ . The distance between the children is 60m.

[a] Draw a rough figure according to the given information.

[b] Find the height of the tower.

**Solution:**



$$CD = 5 * \tan 80^\circ * \tan 70^\circ / \tan 80^\circ + \tan 70^\circ$$

$$= [5 \times 2.75 \times 5.67] / [2.75 + 5.67]$$

$$= 77.9625 / 8.42$$

$$= 9.26 \text{ cm}$$

$$\sin 70^\circ = CD / BC$$

$$BC = CD / \sin 70^\circ$$

$$= 9.26 / 0.94$$

$$= 9.85 \text{ cm}$$

$$AC = CD / \sin 80^\circ$$

$$= 9.26 / 0.98$$

$$= 9.45 \text{ cm}$$

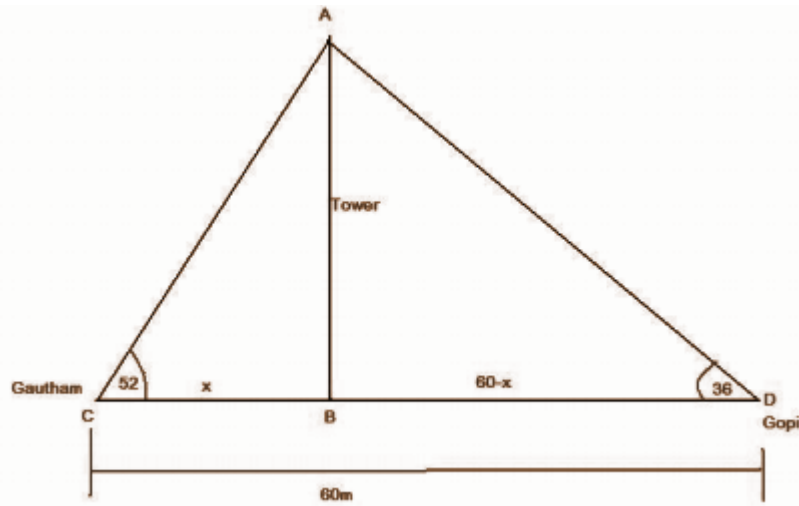
$$\text{Diameter} = AB / \sin 30^\circ$$

$$= 5 / 0.5$$

$$= 10 \text{ cm}$$

$$\text{Circumradius} = 10 / 2 = 5 \text{ cm}$$

**OR**



From  $\triangle ABC$  ,  $AB = x \tan 52^\circ = 1.28x$  ----(1)

From  $\triangle ABD$  ,  $AB = (60 - x) \tan 36^\circ$

$= (60 - x) 0.72$

$= 43.2 - 0.72x$ -----(2)

From (1) and (2)

$1.28x = 43.2 - 0.72x$

$2x = 43.2$

$x = 21.6$

Height of the tower

$= 1.28 \times 21.6$

$= 27.648\text{m}$  or  $27.65\text{m}$

**Question 21:** Equation of a line is  $y = 2x$ .

[a] A is a point on the line. If the coordinate of A is -2, find its y coordinate.

[b] Verify whether a circle of radius 5 centred at A passes through point B(5, 5).

[c] Radius of the circle passing through B is 5 and its centre is on the above-mentioned line. Find the coordinates of its centre.

**Solution:**

Equation of a line is  $y = 2x$ .

[a]  $x = -2$

$\Rightarrow y = 2 \times -2$

$$= -4$$

[b] A (-2, -4)

$$AB = 5$$

$$(5 - [-2])^2 + (5 - [-4])^2$$

$$= 49 + 81$$

$$= 25$$

$$= 5^2$$

Hence a circle of radius 5 centred at point A(-2, -4) does not pass through the point B(5, 5).

[c] Let  $(x_1, y_1)$  be the coordinates of centre C on line.

$$(x_1 - 5)^2 + (y_1 - 5)^2 = 52$$

$$x_1^2 - 10x_1 + 25 + y_1^2 - 10y_1 + 25 = 52$$

$$y_1 = 2x_1$$

$$x_1^2 - 10x_1 + 4x_1^2 - 20x_1 = -25$$

$$5x_1^2 - 30x_1 = -5$$

$$x_1^2 - 6x_1 = -5$$

$$x_1^2 - 6x_1 + 9 = -5 + 9$$

$$(x_1 - 3)^2 = 4$$

$$x_1 - 3 = \pm 2$$

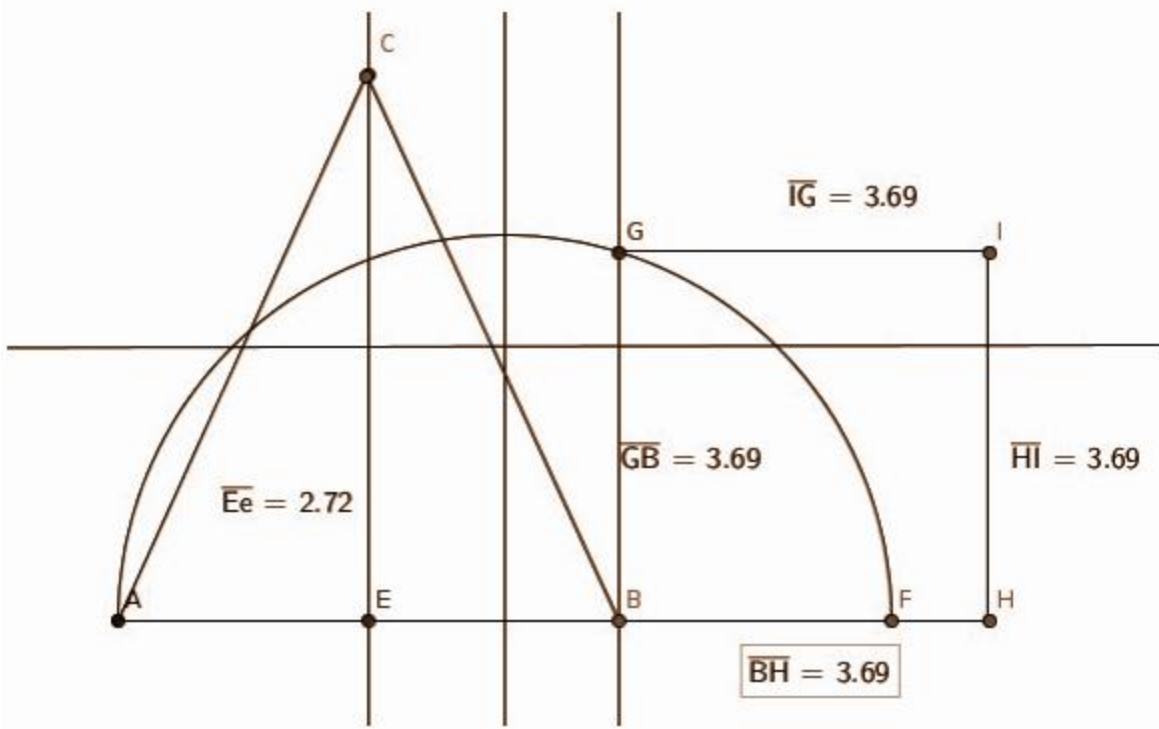
$$x_1 = 2 + 3 = 5 \text{ or } x_1 = -2 + 3 = 1$$

$$y_1 = 2 \times 5 = 10 \text{ or } y_1 = 2 \times 1 = 2$$

The coordinates of point of C are (5, 10) or (1, 2).

**Question 22: Draw a triangle with sides 5cm, 6cm and 6cm. Draw a square having the same area of the triangle.**

**Solution:**



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