

1. Solve the following equations:

(i) $2(3 - 2x) = 13$

(ii) $(3/5)y - 2 = (7/10)$

Solution:

(i) Given

$$2(3 - 2x) = 13$$

$$6 - 4x = 13$$

Transposing 6 to R.H.S. we get,

$$-4x = 13 - 6$$

$$-4x = 7$$

We get,

$$x = (7 / -4)$$

$$x = (-7 / 4)$$

(ii) $(3/5)y - 2 = (7/10)$

Multiplying both sides by 5, we get,

$$3y - 10 = (7/10) \times 5$$

$$3y - 10 = (7/2)$$

Transposing -10 to R.H.S. we get,

$$3y = (7/2) + 10$$

On taking L.C.M. we get,

$$3y = \{(7 + 20) / 2\}$$

$$3y = (27/2)$$

$$y = \{27 / (2 \times 3)\}$$

We get,

$$y = (9/2)$$

$$y = 4\frac{1}{2}$$

2.

(i) $(x/2) = 5 + (x/3)$

(ii) $2\{x - (3/2)\} = 11$

Solution:

(i) $(x/2) = 5 + (x/3)$

On multiplying both sides by 6, we get,

$$6 \times (x/2) = 6 \{5 + (x/3)\}$$

$$3x = 30 + 2x$$

Transposing 2x to L.H.S. we get,

$$3x - 2x = 30$$

We get,
 $x = 30$

$$(ii) 2 \{x - (3 / 2)\} = 11$$

$$2x - 3 = 11$$

Transposing -3 to R.H.S. we get,

$$2x = 11 + 3$$

$$2x = 14$$

We get,

$$x = (14 / 2)$$

$$x = 7$$

3.

$$(i) 7(x - 2) = 2(2x - 4)$$

$$(ii) 21 - 3(x - 7) = x + 20$$

Solution:

$$(i) 7(x - 2) = 2(2x - 4)$$

$$7x - 14 = 4x - 8$$

On transposing 4x to L.H.S. and -14 to R.H.S. we get,

$$7x - 4x = -8 + 14$$

$$3x = 6$$

$$x = (6 / 3)$$

$$x = 2$$

$$(ii) 21 - 3(x - 7) = x + 20$$

$$21 - 3x + 21 = x + 20$$

On further calculation, we get,

$$42 - 3x = x + 20$$

On transposing x to L.H.S. and 42 to R.H.S. we get,

$$-3x - x = 20 - 42$$

$$-4x = -22$$

$$x = (22 / 4)$$

We get,

$$x = (11 / 2)$$

$$x = 5\frac{1}{2}$$

4. If 7 is added to five times a number, the result is 57. Find the number.

Solution:

Let the required number be x

Five times of this number = $5x$

If 7 is added, then the number becomes = $7 + 5x$

As per the given condition,

$$7 + 5x = 57$$

$$5x = 57 - 7$$

$$5x = 50$$

$$x = (50 / 5)$$

We get,

$$x = 10$$

Therefore, the required number = 10

5. Find a number, such that one-fourth of the number is 3 more than 7.

Solution:

Let the required number = x

According to the condition,

$$(1 / 4) x - 3 = 7$$

Transposing -3 to R.H.S. we get,

$$(1 / 4) x = 7 + 3$$

$$(1 / 4) x = 10$$

$$x = 10 \times 4$$

We get,

$$x = 40$$

Therefore, the required number is 40

6. If the replacement set is $(-5, -3, -1, 0, 1, 3, 4)$, find the solution set of:

(i) $x < -2$

(ii) $x > 1$

(iii) $x \geq -1$

(iv) $-5 < x < 3$

(v) $-3 \leq x < 4$

(vi) $0 \leq x < 7$

Solution:

Given

Replacement set = $\{-5, -3, -1, 0, 1, 3, 4\}$

(i) The solution set of $x < -2 = \{-5, -3\}$

(ii) The solution set of $x > 1 = \{3, 4\}$

(iii) The solution set of $x \geq -1 = \{-1, 0, 1, 3, 4\}$

(iv) The solution set of $-5 < x < 3 = \{-3, -1, 0, 1\}$

(v) The solution set of $-3 \leq x < 4 = \{-3, -1, 0, 1, 3\}$

(vi) The solution set of $0 \leq x < 7 = \{0, 1, 3, 4\}$

7. Represent the following inequations graphically:

(i) $x \leq 3, x \in \mathbb{N}$

(ii) $x < 4, x \in \mathbb{W}$

(iii) $-2 \leq x < 4, x \in \mathbb{I}$

(iv) $-3 \leq x \leq 2, x \in \mathbb{I}$

Solution:

Given

$x \leq 3, x \in \mathbb{N}$

Therefore,

The solution set = $\{1, 2, 3\}$

The solution set is shown by thick dots on the number line below



(ii) $x < 4, x \in \mathbb{W}$

Therefore,

The solution set = $\{0, 1, 2, 3\}$

The solution set is shown by thick dots on the number line below



(iii) $-2 \leq x < 4, x \in \mathbb{I}$

Therefore,

The solution set = $\{-2, -1, 0, 1, 2, 3\}$

The solution set is shown by thick dots on the number line below



(iv) $-3 \leq x \leq 2, x \in \mathbb{I}$

Therefore,

The solution set = $\{-3, -2, -1, 0, 1, 2\}$

The solution set is shown by thick dots on the number line below

