

1. Which of the following are positive rational numbers?

$5/8, -3/11, 0/5, 7, -4, -3/-13, -17/-6, 9/-20.$

Solution:

The positive rational numbers are:

$5/8, 0/5, 7, -3/-13, -17/-6.$

2. Which of the following are negative rational numbers?

$-5/7, 4/-3, -3/-11, -6, 9, 0, -28/5, 31/7.$

Solution:

The negative rational numbers are:

$-5/7, 4/-3, -6, -28/5.$

3. Find four rational numbers equivalent to each of the following rational numbers:

(i) $3/-7$

(ii) $-5/-9$

Solution:

(i) $3/-7$

Let us find the equivalent numbers:

Firstly multiply and divide by 2,

$$(3/-7) \times (2/2) = 6/-14$$

Similarly, multiply and divide by 3,

$$(3/-7) \times (3/3) = 9/-21$$

Multiply and divide by 4,

$$(3/-7) \times (4/4) = 12/-28$$

Multiply and divide by 5,

$$(3/-7) \times (5/5) = 15/-35$$

Hence, four equivalent rational numbers are:

$6/-14, 9/-21, 12/-28, 15/-35$

(ii) $-5/-9$

Let us find the equivalent numbers:

Firstly multiply and divide by 2,

$$(-5/-9) \times (2/2) = -10/-18 = 10/18$$

Similarly, multiply and divide by 3,
 $(-5/-9) \times (3/3) = -15/-27 = 15/27$

Multiply and divide by 4,
 $(-5/-9) \times (4/4) = -20/-36 = 20/36$

Multiply and divide by 5,
 $(-5/-9) \times (5/5) = -25/-45 = 25/45$

Hence, four equivalent rational numbers are:
10/18, 15/27, 20/36, 25/45

4. Write each of the following rational numbers with positive denominators:

(i) $4/-9$

(ii) $17/-33$

(iii) $-15/-38$

Solution:

(i) $4/-9 = -4/9$

(ii) $17/-33 = -17/33$

(iii) $-15/-38 = 15/38$

5. Write next four rational numbers in each of the following patterns:

(i) $-1/4, -2/8, -3/12, -4/16, \dots$

(ii) $2/-3, -4/6, -6/9, -8/12, \dots$

Solution:

(i) $-1/4, -2/8, -3/12, -4/16, \dots$

The next four rational numbers in the same patterns are:

$-1/4, -2/8, -3/12, -4/16, -5/20, -6/24, -7/28, -8/32$

(ii) $2/-3, -4/6, -6/9, -8/12, \dots$

The next four rational numbers in the same patterns are:

$2/-3, -4/6, -6/9, -8/12, -10/15, -12/18, -14/21, -16/24$

6. Which of the following pairs of rational numbers are equal?

(i) $-3/-7$ and $15/35$

(ii) $-6/8$ and $10/-15$

(iii) $6/-10$ and $-12/20$

Solution:**(i)** $-3/-7$ and $15/35$

Let us simplify, we get

 $-3/-7$ and $15/35$

$$(-3/-7) = (15/35)$$

Let us cross multiply, we get

$$(-3 \times 35) = (15 \times -7)$$

$$-105 = -105$$

 $\therefore -3/-7$ and $15/35$ are equal pairs.**(ii)** $-6/8$ and $10/-15$

Let us simplify, we get

 $-6/8$ and $10/-15$

$$(-6/8) = (10/-15)$$

Let us cross multiply, we get

$$(-6 \times -15) = (10 \times 8)$$

$$90 = 80$$

 $\therefore -6/8$ and $10/-15$ are not equal pairs.**(iii)** $6/-10$ and $-12/20$

Let us simplify, we get

 $6/-10$ and $-12/20$

$$(6/-10) = (-12/20)$$

Let us cross multiply, we get

$$(6 \times 20) = (-12 \times -10)$$

$$120 = 120$$

 $\therefore 6/-10$ and $-12/20$ are equal pairs.**7. Which of the following pairs represent the same rational number?****(i)** $-7/21$, $3/9$ **(ii)** $-16/20$, $20/-25$ **(iii)** $-3/5$, $-12/20$ **(iv)** $8/-5$, $-24/15$ **Solution:****(i)** $-7/21$, $3/9$

Let us simplify, we get

$$(-7/21) = (3/9)$$

$$(-1/3) = (1/3)$$

$$(-1/3) \neq (1/3)$$

$\therefore -7/21, 3/9$ are not same rational numbers.

(ii) $-16/20, 20/-25$

Let us simplify, we get

$$(-16/20) = (20/-25)$$

$$(-4/5) = (4/-5)$$

$$(-4/5) = (-4/5)$$

$\therefore -16/20, 20/-25$ are same rational numbers.

(iii) $-3/5, -12/20$

Let us simplify, we get

$$(-3/5) = (-12/20)$$

$$(-3/5) = (-3/5)$$

$\therefore -3/5, -12/20$ are same rational numbers.

(iv) $8/-5, -24/15$

Let us simplify, we get

$$8/-5, -24/15$$

$$(8/-5) = (-24/15)$$

$$(8/-5) = (-8/5)$$

$$(-8/5) = (-8/5)$$

$\therefore 8/-5, -24/15$ are same rational numbers.