

EXERCISE 2.1

1. Evaluate:

(i) $(3/5)^{-2}$

(ii) $(-3)^{-3}$

(iii) $(2/7)^{-4}$

Solution:

(i) $(3/5)^{-2}$

Let us evaluate the given expression,

By using the formula, $(a^{-n} = 1/a^n)$

So,

$$\begin{aligned}(3/5)^{-2} &= (5/3)^2 \\ &= (5/3) \times (5/3) \\ &= 25/9\end{aligned}$$

(ii) $(-3)^{-3}$

Let us evaluate the given expression,

By using the formula, $(a^{-n} = 1/a^n)$

So,

$$\begin{aligned}(-3)^{-3} &= (-1/3)^3 \\ &= (-1/3) \times (-1/3) \times (-1/3) \\ &= -1/27\end{aligned}$$

(iii) $(2/7)^{-4}$

Let us evaluate the given expression,

By using the formula, $(a^{-n} = 1/a^n)$

So,

$$\begin{aligned}(2/7)^{-4} &= (7/2)^4 \\ &= (7/2) \times (7/2) \times (7/2) \times (7/2) \\ &= 2401/16\end{aligned}$$

2. Simplify:

(i) $[(2)^{-1} + (4)^{-1} + (3)^{-1}]^{-1}$

(ii) $[(4)^{-1} - (5)^{-1}]^2 \times (5/8)^{-1}$

(iii) $[4^0 + 4^2 - 2^3] \times 3^{-2}$

(iv) $[(5)^2 - (1/4)^{-2}] \times (3/4)^{-2}$

Solution:

(i) $[(2)^{-1} + (4)^{-1} + (3)^{-1}]^{-1}$

Let us simplify the given expression,

$$\begin{aligned}
 [(2)^{-1} + (4)^{-1} + (3)^{-1}]^{-1} &= [(1/2) + (1/4) + (1/3)]^{-1} \\
 &= [(6+3+4)/12]^{-1} \\
 &= [13/12]^{-1} \\
 &= 12/13
 \end{aligned}$$

(ii) $[(4)^{-1} - (5)^{-1}]^2 \times (5/8)^{-1}$

Let us simplify the given expression,

$$\begin{aligned}
 [(4)^{-1} - (5)^{-1}]^2 \times (5/8)^{-1} &= [(1/4) - (1/5)]^2 \times (8/5)^1 \\
 &= [(5-4)/20]^2 \times (8/5) \\
 &= [1/20]^2 \times (8/5) \\
 &= (1/20) \times (1/20) \times (8/5) \\
 &= 1/250
 \end{aligned}$$

(iii) $[4^0 + 4^2 - 2^3] \times 3^{-2}$

Let us simplify the given expression,

$$\begin{aligned}
 [4^0 + 4^2 - 2^3] \times 3^{-2} &= [1 + 16 - 8] \times (1/3^2) \\
 &= 9 \times (1/9) \\
 &= 1
 \end{aligned}$$

(iv) $[(5)^2 - (1/4)^{-2}] \times (3/4)^{-2}$

Let us simplify the given expression,

$$\begin{aligned}
 [(5)^2 - (1/4)^{-2}] \times (3/4)^{-2} &= [25 - (4)^2] \times (4/3)^2 \\
 &= [25 - 16] \times (16/9) \\
 &= 9 \times (16/9) \\
 &= 16
 \end{aligned}$$

3. Find the multiplicative inverse of the following:

(i) $(81/16)^{-3/4}$

(ii) $\{(-3/2)^{-4}\}^{1/2}$

(iii) $(5/7)^{-2} \times (5/7)^4 \div (5/7)^3$

Solution:

(i) $(81/16)^{-3/4}$

Let us simplify to find the multiplicative inverse of the given expression,

$$\begin{aligned}
 (81/16)^{-3/4} &= (16/81)^{3/4} \\
 &= (2^4/3^4)^{3/4} \\
 &= (2/3)^{4 \times 3/4} \\
 &= (2/3)^3 \\
 &= (2/3) \times (2/3) \times (2/3) \\
 &= 8/27
 \end{aligned}$$

So, the multiplicative inverse of $8/27$ is $27/8$.

(ii) $\{(-3/2)^{-4}\}^{1/2}$

Let us simplify to find the multiplicative inverse of the given expression,

$$\begin{aligned}\{(-3/2)^{-4}\}^{1/2} &= (-3/2)^{-4 \times 1/2} \\ &= (-3/2)^{-2} \\ &= (2/-3)^2 \\ &= (2/-3) \times (2/-3) \\ &= 4/9\end{aligned}$$

So, the multiplicative inverse of $4/9$ is $9/4$.

(iii) $(5/7)^{-2} \times (5/7)^4 \div (5/7)^3$

Let us simplify to find the multiplicative inverse of the given expression,

$$\begin{aligned}(5/7)^{-2} \times (5/7)^4 \div (5/7)^3 &= (7/5)^2 \times (5/7)^4 \div (5/7)^3 \\ &= (7/5)^2 \times (5/7)^{4-3} \\ &= (7/5)^2 \times (5/7) \\ &= (7/5) \times (7/5) \times (5/7) \\ &= 7/5\end{aligned}$$

So, the multiplicative inverse of $7/5$ is $5/7$.

4. (i) Express 16^{-2} as a power with base 2.

(ii) Express 125^{-4} as a power with base 5.

Solution:

(i) Express 16^{-2} as a power with base 2.

Let us simplify,

$$\begin{aligned}(16)^{-2} &= (2^4)^{-2} \\ &= 2^{-8} \\ &= 1/2^8\end{aligned}$$

(ii) Express 125^{-4} as a power with base 5.

Let us simplify,

$$\begin{aligned}(125)^{-4} &= (5^3)^{-4} \\ &= 5^{-12} \\ &= 1/5^{12}\end{aligned}$$

5. Write the following numbers in expanded form using exponents:

(i) 2789.453

(ii) 3007.805

Solution:

(i) 2789.453

The expanded form of

$$2789.453 = 2 \times 10^3 + 7 \times 10^2 + 8 \times 10^1 + 9 \times 10^0 + 4 \times 10^{-1} + 5 \times 10^{-2} + 3 \times 10^{-3}$$

(ii) 3007.805

The expanded form of

$$3007.805 = 3 \times 10^3 + 7 \times 10^0 + 8 \times 10^{-1} + 5 \times 10^{-3}$$

6. Simplify and write in exponential form with positive exponent:

(i) $\left\{ \left(\frac{5}{7} \right)^2 \right\}^{-1}^{-3}$

(ii) $\left(\frac{2}{7} \right)^2 \times \left(\frac{7}{2} \right)^{-3} \div \left\{ \left(\frac{7}{5} \right)^{-2} \right\}^{-4}$

(iii) $\left(\frac{4}{5} \right)^2 \times 5^4 \times \left(\frac{2}{5} \right)^{-2} \div \left(\frac{5}{2} \right)^{-3}$

(iv) $\left[8^{-1} \times 5^3 \right] / 2^{-4}$

Solution:

(i) $\left\{ \left(\frac{5}{7} \right)^2 \right\}^{-1}^{-3}$

Let us simplify,

$$\begin{aligned} \left\{ \left(\frac{5}{7} \right)^2 \right\}^{-1}^{-3} &= \left\{ \left(\frac{5}{7} \right)^2 \right\}^{-1 \times -3} \\ &= \left(\frac{5}{7} \right)^{2 \times 3} \\ &= \left(\frac{5}{7} \right)^6 \end{aligned}$$

The exponential form is $\left(\frac{5}{7} \right)^6$.

(ii) $\left(\frac{2}{7} \right)^2 \times \left(\frac{7}{2} \right)^{-3} \div \left\{ \left(\frac{7}{5} \right)^{-2} \right\}^{-4}$

Let us simplify,

$$\begin{aligned} \left(\frac{2}{7} \right)^2 \times \left(\frac{7}{2} \right)^{-3} \div \left\{ \left(\frac{7}{5} \right)^{-2} \right\}^{-4} &= \left(\frac{2}{7} \right)^2 \times \left(\frac{2}{7} \right)^3 \div \left(\frac{7}{5} \right)^8 \\ &= \left(\frac{2}{7} \right)^2 \times \left(\frac{2}{7} \right)^3 \times \left(\frac{5}{7} \right)^8 \\ &= \left(\frac{2^2}{7^2} \right) \times \left(\frac{2^3}{7^3} \right) \times \left(\frac{5^8}{7^8} \right) \\ &= \left(\frac{2^{2+3}}{7^{2+3}} \right) \times \left(\frac{5^8}{7^8} \right) \\ &= \left(\frac{2^5}{7^5} \right) \times \left(\frac{5^8}{7^8} \right) \\ &= \left(\frac{2^5 \times 5^8}{7^{5+8}} \right) \\ &= \left(\frac{2^5 \times 5^8}{7^{13}} \right) \end{aligned}$$

The exponential form is $\left(\frac{2^5 \times 5^8}{7^{13}} \right)$.

(iii) $\left(\frac{4}{5} \right)^2 \times 5^4 \times \left(\frac{2}{5} \right)^{-2} \div \left(\frac{5}{2} \right)^{-3}$

Let us simplify,

$$\begin{aligned} \left(\frac{4}{5} \right)^2 \times 5^4 \times \left(\frac{2}{5} \right)^{-2} \div \left(\frac{5}{2} \right)^{-3} &= \left(\frac{2^2}{5^2} \right) \times 5^4 \times \left(\frac{2^{-2}}{5^{-2}} \right) \times \left(\frac{2^{-3}}{5^{-3}} \right) \\ &= \left(\frac{2^4 \times 5^4 \times 2^{-2} \times 2^{-3}}{5^2 \times 5^{-2} \times 5^{-3}} \right) \\ &= \frac{2^{4-2-3} \times 5^{4-2+3}}{1} \\ &= 2^{-1} \times 5^7 \\ &= \frac{5^7}{2^1} \end{aligned}$$

The exponential form is $5^7/2^1$.

(iv) $[8^{-1} \times 5^3]/2^{-4}$

Let us simplify,

$$\begin{aligned} [8^{-1} \times 5^3]/2^{-4} &= [(2^3)^{-1} \times 5^3]/2^{-4} \\ &= [2^{-3} \times 5^3]/2^{-4} \\ &= 2^{-3+4} \times 5^3 \\ &= 2^1 \times 5^3 \\ &= 2 \times 5 \times 5 \times 5 \\ &= 250 \end{aligned}$$

The exponential form is 250.

7. Simplify and write the following in exponential form:

(i) $((-2)^3)^2 + 5^{-3} \div 5^{-5} - (-1/2)^0$

(ii) $3^{-5} \times 3^2 \div 3^{-6} + (2^2 \times 3)^2 + (2/3)^{-1} + 2^{-1} + (1/19)^{-1}$

Solution:

(i) $((-2)^3)^2 + 5^{-3} \div 5^{-5} - (-1/2)^0$

Let us simplify,

$$\begin{aligned} ((-2)^3)^2 + 5^{-3} \div 5^{-5} - (-1/2)^0 &= (-2)^6 + 1/5^3 \div 1/5^5 - 1 \\ &= 64 + 1/5^3 \times 5^5 - 1 \\ &= 64 + 5^{5-3} - 1 \\ &= 64 + 5^2 - 1 \\ &= 64 + 25 - 1 \\ &= 88 \end{aligned}$$

The exponential form is 88.

(ii) $3^{-5} \times 3^2 \div 3^{-6} + (2^2 \times 3)^2 + (2/3)^{-1} + 2^{-1} + (1/19)^{-1}$

Let us simplify,

$$\begin{aligned} 3^{-5} \times 3^2 \div 3^{-6} + (2^2 \times 3)^2 + (2/3)^{-1} + 2^{-1} + (1/19)^{-1} &= 3^{-5+2+6} + (2^4 \times 3^2) + 3/2 + 1/2 + 19^1 \\ &= 3^3 + (16 \times 9) + 4/2 + 19 \\ &= 27 + 144 + 2 + 19 \\ &= 192 \end{aligned}$$

The exponential form is 192.

8. Simplify and write in exponential form with negative exponent:

(i) $5^3 \times (4/5)^3$

(ii) $[(3/7)^{-2}]^{-3}$

(iii) $(5/9)^{-2} \times (5/3)^2 \div (1/5)^{-2}$

(iv) $2^{-1} [(5/3)^4 + (3/5)^{-2}] \div (17/9)$

$$(v) (-7)^3 \times (1/-7)^{-9} \div (-7)^{10}$$

Solution:

$$(i) 5^3 \times (4/5)^3$$

Let us simplify,

$$\begin{aligned} 5^3 \times (4/5)^3 &= 5^3 \times (4^3/5^3) \\ &= 5^{3-3} \times 4^3 \\ &= 5^0 \times 4^3 \\ &= 1 \times 4^3 \\ &= (1/4)^{-3} \end{aligned}$$

The exponential form is $(1/4)^{-3}$.

$$(ii) [(3/7)^{-2}]^{-3}$$

Let us simplify,

$$\begin{aligned} [(3/7)^{-2}]^{-3} &= (3/7)^{-2 \times -3} \\ &= (3/7)^6 \\ &= (7/3)^{-6} \end{aligned}$$

The exponential form is $(7/3)^{-6}$.

$$(iii) (5/9)^{-2} \times (5/3)^2 \div (1/5)^{-2}$$

Let us simplify,

$$\begin{aligned} (5/9)^{-2} \times (5/3)^2 \div (1/5)^{-2} &= (5^{-2}/9^{-2}) \times (5^2/3^2) \div (1/5^{-2}) \\ &= (5^{-2} \times 5^2 \times 5^{-2}) / [(3^2)^{-2} \times 3^2] \\ &= (5^{-2+2-2}) / (3^{-4+2}) \\ &= 5^{-2}/3^{-2} \\ &= (5/3)^{-2} \end{aligned}$$

The exponential form is $(5/3)^{-2}$.

$$(iv) 2^{-1} [(5/3)^4 + (3/5)^{-2}] \div (17/9)$$

Let us simplify,

$$\begin{aligned} 2^{-1} [(5/3)^4 + (3/5)^{-2}] \div (17/9) &= 2^{-1} [(5^4/3^4) + (3^{-2}/5^{-2})] \div (17/9) \\ &= 2^{-1} [(5^4/3^4) + (5^2/3^2)] \div (17/9) \\ &= 2^{-1} [(625/81) + (25/9)] \div (17/9) \\ &= \frac{1}{2} [(625 + 225)/81] \times (9/17) \\ &= \frac{1}{2} \times (850/81) \times 9/17 \\ &= 25/9 \\ &= (5/3)^2 \\ &= (3/5)^{-2} \end{aligned}$$

The exponential form is $(3/5)^{-2}$.

$$(v) (-7)^3 \times (1/-7)^{-9} \div (-7)^{10}$$

Let us simplify,

$$\begin{aligned} (-7)^3 \times (1/-7)^{-9} \div (-7)^{10} &= (-7)^3 \times (-7)^9 \div (-7)^{10} \\ &= (-7)^{3+9-10} \\ &= (-7)^2 \\ &= (1/-7)^{-2} \end{aligned}$$

The exponential form is $(1/-7)^{-2}$.

9. Simplify:

$$(i) (49 \times z^{-3}) / (7^{-3} \times 10 \times z^{-5}) \quad (z \neq 0)$$

$$(ii) (9^3 \times 27 \times t^4) / (3^2 \times 3^4 \times t^2)$$

$$(iii) [(3^{-2})^2 \times (5^2)^{-3} \times (-t^3)^2] / [(3^{-2})^5 \times (5^3)^{-2} \times (t^4)^3]$$

$$(iv) (2^{-5} \times 15^{-5} \times 500) / (5^{-6} \times 6^{-5})$$

Solution:

$$(i) (49 \times z^{-3}) / (7^{-3} \times 10 \times z^{-5}) \quad (z \neq 0)$$

Let us simplify the given expression,

$$\begin{aligned} (49 \times z^{-3}) / (7^{-3} \times 10 \times z^{-5}) &= (7^2 \times z^{-3}) / (7^{-3} \times 10 \times z^{-5}) \\ &= (7^{2+3} \times z^{-3+5}) / 10 \\ &= (7^5 \times z^2) / 10 \end{aligned}$$

$$(ii) (9^3 \times 27 \times t^4) / (3^2 \times 3^4 \times t^2)$$

Let us simplify the given expression,

$$\begin{aligned} (9^3 \times 27 \times t^4) / (3^2 \times 3^4 \times t^2) &= [(3^2)^3 \times (3)^3 \times t^4] / (3^2 \times 3^4 \times t^2) \\ &= (3^6 \times 3^3 \times t^4) / (3^2 \times 3^4 \times t^2) \\ &= 3^{6+3-2-4} \times t^{4-2} \\ &= 3^3 \times t^2 \\ &= 27t^2 \end{aligned}$$

$$(iii) [(3^{-2})^2 \times (5^2)^{-3} \times (t^3)^2] / [(3^{-2})^5 \times (5^3)^{-2} \times (t^4)^3]$$

Let us simplify the given expression,

$$\begin{aligned} [(3^{-2})^2 \times (5^2)^{-3} \times (t^3)^2] / [(3^{-2})^5 \times (5^3)^{-2} \times (t^4)^3] &= [3^{-4} \times 5^{-6} \times t^6] / [3^{-10} \times 5^{-6} \times t^{12}] \\ &= 3^{-4+10} \times 5^{-6+6} \times t^{-6+12} \\ &= 3^6 \times 5^0 \times t^6 \\ &= 3^6 \times 1 \times t^6 \\ &= 729t^6 \end{aligned}$$

$$(iv) (2^{-5} \times 15^{-5} \times 500) / (5^{-6} \times 6^{-5})$$

Let us simplify the given expression,

$$(2^{-5} \times 15^{-5} \times 500) / (5^{-6} \times 6^{-5}) = (2^{-5} \times (3 \times 5)^{-5} \times 2^2 \times 5^3) / (5^{-6} \times (2 \times 3)^{-5})$$

$$\begin{aligned}
 &= (2^{-5} \times 3^{-5} \times 5^{-5} \times 2^2 \times 5^3) / (5^{-6} \times 2^{-5} \times 3^{-5}) \\
 &= 2^{-5+2+5} \times 3^{-5+5} \times 5^{-5+3+6} \\
 &= 2^2 \times 3^0 \times 5^4 \\
 &= 4 \times 1 \times 625 \\
 &= 2500
 \end{aligned}$$

10. By what number should $(3/-2)^{-3}$ be divided to get $(2/3)^2$?

Solution:

The required number is $(3/-2)^{-3} \div (2/3)^2$

Let us simplify the expression,

$$\begin{aligned}
 (3/-2)^{-3} \div (2/3)^2 &= (3^{-3})/(-2)^{-3} \times (3^2)/(2^2) \\
 &= [3^{-3} \times 3^2]/[-2^{-3} \times 2^2] \\
 &= [3^{-3+2}]/(-2)^{-3+2} \\
 &= 3^{-1}/-2^{-1} \\
 &= -2^1/3^1 \\
 &= -2/3
 \end{aligned}$$

11. Find the value of m for which $9^m \div 3^{-2} = 9^4$.

Solution:

Let us simplify the expression,

$$\begin{aligned}
 9^m \div 3^{-2} &= 9^4 \\
 (3^2)^m \div 3^{-2} &= (3^2)^4 \\
 3^{2m} \div 3^{-2} &= 3^8 \\
 3^{2m+2} &= 3^8
 \end{aligned}$$

Now by comparing the powers, we get

$$\begin{aligned}
 2m + 2 &= 8 \\
 2m &= 8 - 2 \\
 &= 6 \\
 m &= 6/2 \\
 &= 3
 \end{aligned}$$

12. If $(-5/7)^{-4} \times (-5/7)^{12} = \{(-5/7)^3\} \times (-5/7)^{-1}$, find the value of x.

Solution:

Let us simplify the given expression,

$$\begin{aligned}
 (-5/7)^{-4} \times (-5/7)^{12} &= \{(-5/7)^3\} \times (-5/7)^{-1} \\
 (-5/7)^{-4} \times (-5/7)^{12} &= (-5/7)^{3x} \times (-5/7)^{-1} \\
 (-5/7)^{-4+12} &= (-5/7)^{3x-1} \\
 (-5/7)^8 &= (-5/7)^{3x-1}
 \end{aligned}$$

Now by comparing the powers, we get

$$\begin{aligned}
 8 &= 3x - 1 \\
 3x &= 8 + 1 \\
 3x &= 9 \\
 x &= 9/3 \\
 &= 3
 \end{aligned}$$

13. Find x, if $(-2/3)^{-13} \times (3/-2)^8 = (-2/3)^{-2x+1}$

Solution:

Let us simplify the given expression,

$$\begin{aligned}
 (-2/3)^{-13} \times (3/-2)^8 &= (-2/3)^{-2x+1} \\
 (-2/3)^{-13} \times (-2/3)^{-8} &= (-2/3)^{-2x+1} \\
 (-2/3)^{-13-8} &= (-2/3)^{-2x+1} \\
 (-2/3)^{-21} &= (-2/3)^{-2x+1}
 \end{aligned}$$

Now by comparing the powers, we get

$$\begin{aligned}
 -21 &= -2x + 1 \\
 2x &= 1 + 21 \\
 2x &= 22 \\
 x &= 22/2 \\
 &= 11
 \end{aligned}$$

14. (i) If $5^{2x-1} = 1/(125)^{x-3}$, find x.

(ii) If $(9^n \times 3^5 \times 27^3)/(3 \times 81^4) = 27$, find n.

Solution:

(i) If $5^{2x-1} = 1/(125)^{x-3}$, find x.

Let us simplify the given expression,

$$\begin{aligned}
 5^{2x-1} &= 1/(5^3)^{x-3} \\
 5^{2x-1} &= 1/5^{3x-9} \\
 5^{2x-1} &= 5^{-3x+9}
 \end{aligned}$$

Now by comparing the powers, we get

$$\begin{aligned}
 2x - 1 &= -3x + 9 \\
 2x + 3x &= 9 + 1 \\
 5x &= 10 \\
 x &= 10/5 \\
 &= 2
 \end{aligned}$$

(ii) If $(9^n \times 3^5 \times 27^3)/(3 \times 81^4) = 27$

Let us simplify the given expression,

$$\begin{aligned}
 [(3^2)^n \times 3^5 \times (3^3)^3]/(3 \times (3^4)^4) &= 3^3 \\
 [3^{2n} \times 3^5 \times 3^9] &= (3 \times 3^{16}) = 3^3
 \end{aligned}$$

$$3^{2n+5+9-1-16} = 3^3$$

Now by comparing the powers, we get

$$2n + 5 + 9 - 1 - 16 = 3$$

$$2n - 3 = 3$$

$$2n = 3 + 3$$

$$2n = 6$$

$$n = 6/2$$

$$= 3$$



(vii) The distance from the Earth of the Sun is 149,600,000,000 m.

(viii) The speed of light is 300,000,000 m/sec.

(ix) Mass of the Earth is 5,970,000,000,000,000,000,000 kg.

(x) Express 3 years in seconds.

(xi) Express 7 hectares in cm^2 .

(xii) A sugar factory has annual sales of 3 billion 720 million kilograms of sugar.

Solution:

(i) The mass of a proton is 0.0000000000000000000000001673 gram, it is expressed in standard form as 1.673×10^{-24} gram.

(ii) Thickness of a piece of paper in standard form is 0.0016 cm; it is expressed in standard form as 1.6×10^{-3}

(iii) Diameter of a wire on a computer chip is 0.000003 m; it is expressed in standard form as 3.0×10^{-6} m

(iv) A helium atom has a diameter of $22/1000000000000$ m; it is expressed in standard form as $22 \times 10^{-12} = 2.2 \times 10^{-10}$

(v) Mass of a molecule of hydrogen gas is about 0.000000000000000000000000334 tons; it is expressed in standard form as 3.34×10^{-21} tons

(vi) Human body has 1 trillion of cells which vary in shapes and sizes; it is expressed in standard form as $1,000,000,000,000 = 10^{12}$

(vii) The distance from the Earth of the Sun is expressed in standard form as $149,600,000,000 \text{ m} = 1.496 \times 10^{11}$

(viii) The speed of light is 300,000,000 m/sec; it is expressed in standard form as 3.0×10^8 m/sec

(ix) Mass of the Earth is 5,970,000,000,000,000,000,000 kg; it is expressed in standard form as 5.97×10^{24} kg

(x) Express 3 years in seconds, it is expressed in standard form as

$$\begin{aligned} 3 \text{ years} &= 3 \times 365 \text{ days} \\ &= 3 \times 365 \times 24 \text{ hours} \\ &= 3 \times 365 \times 24 \times 3600 \text{ seconds} \\ &= 1040688000 \text{ seconds} \\ &= 1.040688 \times 10^9 \text{ seconds} \end{aligned}$$

(xi) Express 7 hectares in cm^2 , it is expressed in standard form as

$$\begin{aligned}7 \text{ hectares} &= 7 \times 10000 \text{ m}^2 \\ &= 7 \times 10000 \times 100 \times 100 \text{ cm}^2 \\ &= 700000000 \text{ cm}^2 \\ &= 7.0 \times 10^8 \text{ cm}^2\end{aligned}$$

(xii) A sugar factory has annual sales of 3 billion 720 million kilograms of sugar, it is expressed in standard form as

Annual sale of a sugar factory = 3 billion

720 million kilograms sugar = 3,720,000,000 kg = 3.72×10^9 kg

4. Compare the following:

(i) Size of a plant cell to the thickness of a piece of paper.

(ii) Size of a plant cell to the diameter of a wire on a computer chip.

(iii) The thickness of a piece of paper to the diameter of a wire on a computer chip.

Given size of plant cell = 0.00001275 m

Thickness of a piece of paper = 0.0016 cm

Diameter of a wire on a computer chip = 0.000003 m

Solution:

Given:

Size of plant cell = 0.00001275 m = 1.275×10^{-5} m

Thickness of a piece of paper = 0.0016 cm = 1.6×10^{-3} cm

Diameter of a wire on a computer chip = 0.000003 m = 3.0×10^{-6} m

(i) Size of plant cell: thickness of a piece of paper

$$1.275 \times 10^{-5} : 1.6 \times 10^{-3}$$

Size of plant cell = $1.2/1.6 = 3/4$ times of thickness of paper.

(ii) Size of plant cell: diameter of wire on a computer chip

$$1.275 \times 10^{-5} : 3.0 \times 10^{-6}$$

$$12.75 : 3.00$$

Size of plant cell is 4 times of diameter of wire.

(iii) Thickness of a piece of paper: diameter of a wire on a computer chip

$$1.6 \times 10^{-3} : 3.0 \times 10^{-6} \times 100 \text{ cm}$$

$$1.6 \times 1000 : 300$$

$$16.1 : 3$$

Approximately 5 times is the thickness of paper to diameter of wire.

5. The number of red blood cells per cubic millimeter of blood is approximately 5.5 million. If the average body contains 5 liters of blood, what is the total number of red cell in the body? (1 liter = 1,00,000 mm³)

Solution:

Given:

$$\text{Red blood per cubic millimeter} = 5.5 \text{ million} = 5.5 \times 10^6$$

$$\text{Red blood in 5 liters of blood} = 5.5 \times 10^6 \times 5 \times 10^5 \text{ (1 litre} = 10^5 \text{ mm}^3\text{)}$$

$$= 27.5 \times 10^{6+5}$$

$$= 27.5 \times 10^{11}$$

$$= 2.75 \times 10 \times 10^{11}$$

$$= 2.75 \times 10^{12}$$

∴ Total number of red blood cells in the body is 2.75×10^{12} .

6. Mass of Mars is 6.42×10^{29} kg and the mass of the sun is 1.99×10^{30} kg. What is the total mass?

Solution:

Given:

$$\text{Mass of Mars} = 6.42 \times 10^{29} \text{ kg}$$

$$\text{and mass of sun} = 1.99 \times 10^{30}$$

$$\text{Total mass} = 6.42 \times 10^{29} + 1.99 \times 10^{30}$$

$$= 10^{29} (6.42 + 1.99 \times 10)$$

$$= 10^{29} (6.42 + 19.9)$$

$$= 26.32 \times 10^{29}$$

∴ Total mass of mars is 26.32×10^{29} .

7. A particular star is at a distance of about 8.1×10^{13} km from the Earth. Assuming that the light travels at 3×10^8 m/sec, find how long does light take from that star to reach the Earth.

Solution:

Given:

$$\text{Distance between earth and a particular star} = 8.1 \times 10^{13} \text{ km}$$

$$\text{Speed of light} = 3 \times 10^8 \text{ m/sec.}$$

$$\text{Time is taken to reach the earth} = (8.1 \times 10^{13}) / (3 \times 10^8)$$

$$= 2.7 \times 10^{16-8}$$

$$= 2.7 \times 10^8 \text{ sec}$$

∴ Light takes 2.7×10^8 sec from star to reach the earth.