

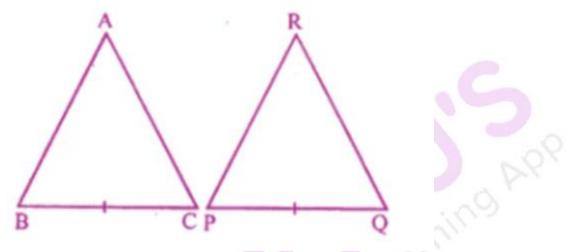
EXERCISE 10.1

1. It is given that $\triangle ABC \cong \triangle RPQ$. Is it true to say that BC = QR ? Why?

Solution:

Given $\triangle ABC \cong \triangle RPQ$

Therefore their corresponding sides and angles are equal.



Therefore BC = PQ Hence it is not true to say that BC = QR

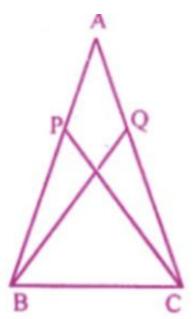
2. "If two sides and an angle of one triangle are equal to two sides and an angle of another triangle, then the two triangles must be congruent." Is the statement true? Why?

Solution:

No, it is not true statement as the angles should be included angle of there two given sides.

3. In the given figure, AB=AC and AP=AQ. Prove that
(i) ΔAPC ≅ ΔAQB
(ii) CP = BQ
(iii) ∠APC = ∠AQB.





Solution:

(i) In \triangle APC and \triangle AQB AB=AC and AP=AQ [given] From the given figure, $\angle A = \angle A$ [common in both the triangles] Therefore, using SAS axiom we have \triangle APC $\cong \triangle$ AQB

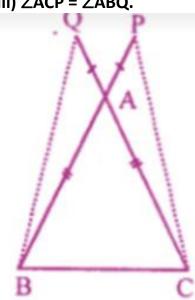
(ii) In \triangle APC and \triangle AQB AB=AC and AP=AQ [given] From the given figure, $\angle A = \angle A$ [common in both the triangles] By using corresponding parts of congruent triangles concept we have BQ = CP

(iii) In \triangle APC and \triangle AQB AB=AC and AP=AQ [given] From the given figure, $\angle A = \angle A$ [common in both the triangles] By using corresponding parts of congruent triangles concept we have $\angle APC = \angle AQB$.

4. In the given figure, AB = AC, P and Q are points on BA and CA respectively such that AP = AQ. Prove that
(i) ΔAPC ≅ ΔAQB
(ii) CP = BQ







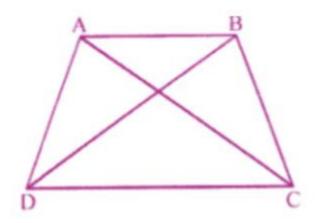
Solution:

(i) In the given figure AB = ACP and Q are point on BA and CA produced respectively such that AP = AQ Now we have to prove $\triangle APC \cong \triangle AQB$ By using corresponding parts of congruent triangles concept we have CP = BQ $\angle ACP = \angle ABQ$ (ii) CP = BQ

(iii) $\angle ACP = \angle ABQ$ In \triangle APC and \triangle AQB AC = AB (Given) AP = AQ (Given) \angle PAC = \angle QAB (Vertically opposite angle)

5. In the given figure, AD = BC and BD = AC. Prove that : $\angle ADB = \angle BCA$ and $\angle DAB = \angle CBA$.





Solution:

Given: in the figure, AD = BC, BD = AC

B

To prove : (i) $\angle ADB = \angle BCA$ (ii) $\angle DAB = \angle CBA$ Proof : in $\triangle ADB$ and $\triangle ACB$ AB = AB (Common) AD = BC (given) DB = AC (Given) $\triangle ADB = \triangle ACD$ (SSS axiom) $\angle ADB = \angle BCA$ $\angle DAB = \angle CBA$

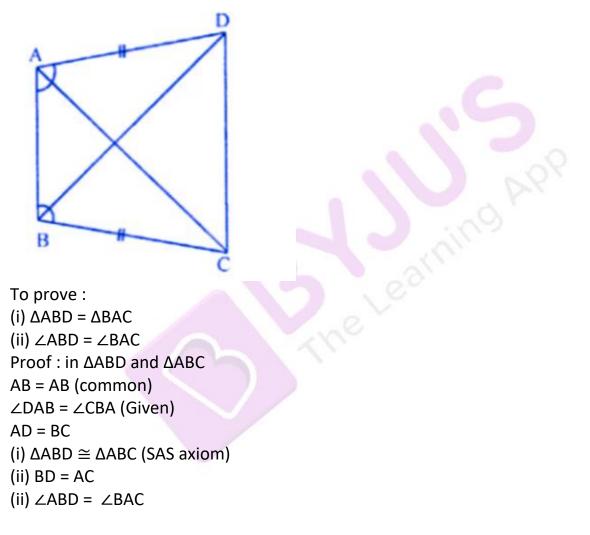
6. In the given figure, ABCD is a quadrilateral in which AD = BC and ∠DAB = ∠CBA. Prove that
(i) ΔABD ≅ ΔBAC
(ii) BD = AC



(iii) ∠ABD = ∠BAC.

Solution:

Given : in the figure ABCD is a quadrilateral In which AD = BC \angle DAB = \angle CBA



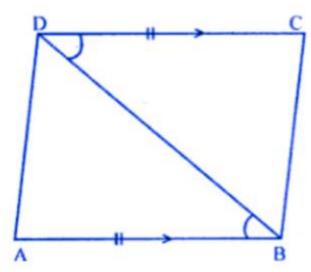
7.In the given figure, AB = DC and AB || DC. Prove that AD = BC.

Solution :

Given: in the given figure. AB = DC, AB || DC To prove : AD = BC Proof : AB || DC

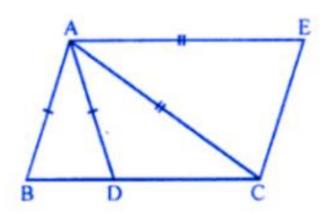


 $\angle ABD = \angle CDB$ (Alternate angles) In $\triangle ABD$ and $\triangle CDB$ AB = DC



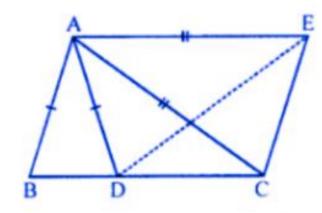
 $\angle ABD = \angle CDB$ (Alternate angles) BD = BD (common) $\triangle ABD \cong CDB$ (SAS axiom) AD = BC

8. In the given figure. AC = AE, AB = AD and \angle BAD = \angle CAE. Show that BC = DE.



Solution: Given: in the figure, AC = AE, AB = AD \angle BAD = \angle CAE To prove : BC = DE





Proof : in \triangle ABC and \triangle ADE AB = AD (given) AC = AE (given) \angle BAD + \angle DAC + \angle CAE \angle BAC = \angle DAE \triangle ABC = \triangle ADE (SAS axiom) BC = DE

9. In the adjoining figure, AB = CD, CE = BF and $\angle ACE = \angle DBF$. Prove that (i) $\triangle ACE \cong \triangle DBF$ (ii) AE = DF.

Solution:

Given : in the given figure AB = CD CE = BF $\angle ACE = \angle DBF$



To prove : (i) $\triangle ACE \cong \triangle DBF$ (i) $\triangle ACE \cong \triangle DBF$ (SAS axiom) AE = DE

(ii) AE = DFProof : AB = CDAdding BC to both sides AB + BC = BC + CD AC = BDNow in $\triangle ACE$ and $\triangle DBF$ AC = BD (Proved) CE = BF (Given) $\angle ACE = \angle DBF$ (SAS axiom)



EXERCISE 10.2

1. In triangles ABC and PQR, $\angle A = \angle Q$ and $\angle B = \angle R$. Which side of APQR should be equal to side AB of AABC so that the two triangles are congruent? Give reason for your answer.

Solution:

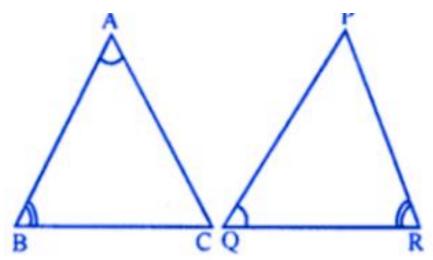
AB = QP

Because triangles are congruent of their corresponding two angles and included sides are equal

2. In triangles ABC and PQR, $\angle A = \angle Q$ and $\angle B = \angle R$. Which side of APQR should be equal to side BC of AABC so that the two triangles are congruent? Give reason for your answer.

Solution: In $\triangle ABC$ and $\triangle PQR$





∠A = ∠Q ∠B = ∠R

Their included sides AB and QR will be equal for their congruency. Therefore, BC = PR by corresponding parts of congruent triangles.

3. "If two angles and a side of one triangle are equal to two angles and a side of another triangle, then the two triangles must be congruent". Is the statement true? Why?

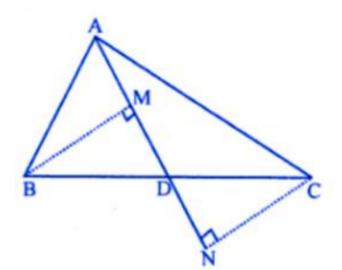
Solution:

The given statement can be true only if the corresponding (included) sides are equal otherwise not.

4. In the given figure, AD is median of \triangle ABC, BM and CN are perpendiculars drawn from B and C respectively on AD and AD produced. Prove that BM = CN.

Solution:



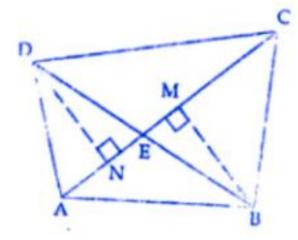


Given in \triangle ABC, AD is median BM and CN are perpendicular to AD form B and C respectively.

To prove: BM = CNProof: In ΔBMD and ΔCND BD = CD (because AD is median) $\angle M = \angle N$ $\angle BDM = \angle CDN$ (vertically opposite angles) $\Delta BMD \cong \Delta CND$ (AAS axiom) Therefore, BM = CN.

5. In the given figure, BM and DN are perpendiculars to the line segment AC. If BM = DN, prove that AC bisects BD.



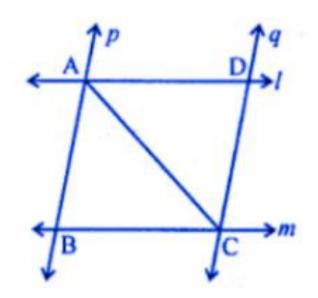


Solution:

Given in figure BM and DN are perpendicular to AC BM = DN To prove: AC bisects BD that is BE = ED Construction: Join BD which intersects Ac at E Proof: In Δ BEM and Δ DEN BM = DN $\angle M = \angle N$ (given) $\angle DEN = \angle BEM$ (vertically opposite angles) Δ BEM $\cong \Delta$ DEN BE = ED Which implies AC bisects BD

6. In the given figure, I and m are two parallel lines intersected by another pair of parallel lines p and q. Show that $\triangle ABC \cong \triangle CDA$.





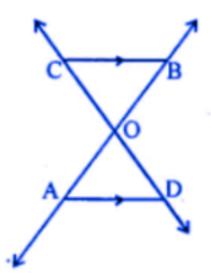
Solution:

In the given figure, two lines I and m are parallel to each other and lines p and q are also a pair of parallel lines intersecting each other at A, B, C and D. AC is joined.

To prove: $\Delta ABC \cong \Delta CDA$ Proof: In ΔABC and ΔCDA AC = AC (common) $\angle ACB = \angle CAD$ (alternate angles) $\angle BAC = \angle ACD$ (alternate angles) $\Delta ABC \cong \Delta$ DCA (ASA axiom)

7. In the given figure, two lines AB and CD intersect each other at the point O such that BC || DA and BC = DA. Show that O is the mid-point of both the line segments AB and CD.





Solution:

In the given figure, lines AB and CD intersect each other at O such that BC || AD and BC = DA

To prove:

O is the midpoint of Ab and Cd

Proof:

Consider $\triangle AOD$ and $\triangle BOC$

AD = BC (given)

 $\angle OAD = \angle OBC$ (alternate angles)

 $\angle ODA = \angle OCB$ (alternate angles)

 $\Delta AOD \cong \Delta BOC$ (SAS axiom)

Therefore, OA = OB and OD = OC

Therefore O is the midpoint of AB and CD.



EXERCISE 10.3

1. ABC is a right angled triangle in which $\angle A = 90^{\circ}$ and AB = AC. Find $\angle B$ and $\angle C$.

Solution:

In right angled triangle ABC, $\angle A = 90^{\circ}$ $\angle B + \angle C = 180^{\circ} - \angle A$ $= 180^{\circ} - 90^{\circ} = 90^{\circ}$

Because AB = AC $\angle C = \angle B$ (Angles opposite to equal sides) $\angle B + \angle B = 90^{\circ} (2 \angle B = 90^{\circ})$ $\angle B = 90/2^{\circ} = 45^{\circ}$ $\angle B = \angle C = 45^{\circ}$ $\angle B = \angle C = 45^{\circ}$

2. Show that the angles of an equilateral triangle are 60° each.

Solution:

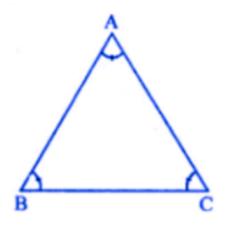
 $\begin{array}{l} \Delta ABC \text{ is an equilateral triangle} \\ AB = BC = CA \\ \angle A = \angle B = \angle C \text{ (opposite to equal sides)} \\ But \angle A + \angle B + \angle C = 180^{\circ} \text{ (sum of angles of a triangle)} \\ 3 \angle A = 180^{\circ} (\angle A = 180^{\circ/3} = 60^{\circ}) \\ \angle A = \angle B = \angle C = 60^{\circ} \end{array}$

3. Show that every equiangular triangle is equilateral.



Solution:

ΔABC is an equiangular

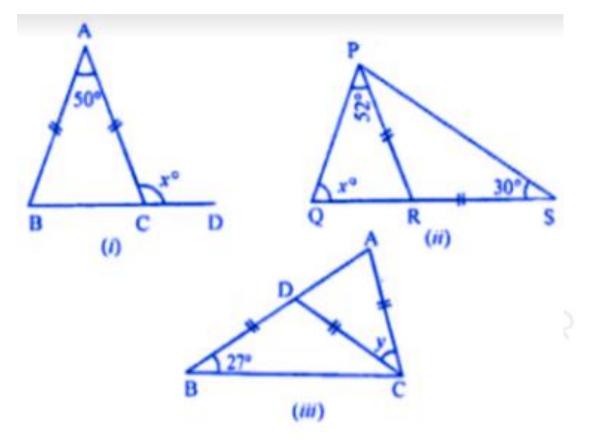


 $\angle A = \angle B = \angle C$ In $\triangle ABC$ $\angle B = \angle C$ AC = AB (sides opposite to equal angles) Similarly, $\angle C = \angle A$ BC = AB From (i) and (ii) AB = BC = AC $\triangle ABC$ is an equilateral triangle

4. In the following diagrams, find the value of x:







Solution:

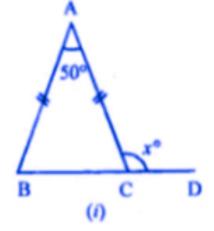
(i) in following diagram given that AB =AC

That is $\angle B = \angle ACB$ (angles opposite to equal sides in a triangle are equal)

In a triangle are equal)

Now, $\angle A + \angle B + \angle ACB = 180^{\circ}$

(sum of all angles in a triangle is 180°)



 $50 + \angle B + \angle B = 180^{\circ}$

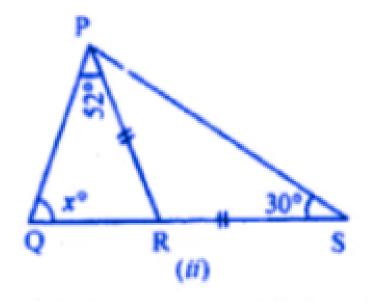


 $(\angle A = 50^{\circ} \text{ (given) } \angle B = \angle ACB)$ $50^{\circ} + 2 \angle B = 180^{\circ} (2 \angle B = 180^{\circ} - 50^{\circ})$ $2 \angle B = 130^{\circ} (\angle B = 130/2 = 65^{\circ})$ $\angle ACB = 65^{\circ}$ Also $\angle ACB + x^{\circ} = 180^{\circ} \text{ (Linear pair)}$ $65^{\circ} + x^{\circ} = 180^{\circ} (x^{\circ} = 180^{\circ} - 65^{\circ})$ $x^{\circ} = 115^{\circ}$ Hence, Value of x = 115

(ii) in ∆PRS, Given that PR = RS

∠PSR = ∠RPS

(Angles opposite in a triangle, equal sides are equal)



 $30^{\circ} = \angle RPS (\angle PPS = 30^{\circ}.....(1)$ $\angle QPS = \angle QPR + \angle RPS$ $\angle QPS = 52^{\circ} + 30^{\circ}$ (Given, $\angle QPR = 52^{\circ}$ and from (i), $\angle RPS = 30^{\circ}$ $\angle QPS = 82^{\circ}$ Now, In $\triangle PQS$ $\angle QPS + \angle QSP + PQS = 180^{\circ}$ (sum of all angles in a triangles is 180°) $= 82^{\circ} + 30^{\circ} + x^{\circ} = 180^{\circ}$ (from (2) $\angle QPS = 82^{\circ}$ and $\angle QSP = 30^{\circ}$ (given)

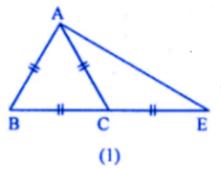


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112^{\circ} + x^{\circ} = 180^{\circ} (x^{\circ} = 180^{\circ} - 112^{\circ})
Hence, Value of x = 68
(iii) In the following figure, Given
That, BD = CD = AC and \angleDBC = 27°
Now in \triangle BCD
BD = CD (Given)
\angle DBC = \angle BCD \dots (1)
(in a triangle sides opposite equal angles are equal)
Also,, \angle DBC = 27^{\circ} (given) .....(2)
From (1) and (2) we get
\angle BCD = 27^{\circ}
Now, ext \angleCDA = \angleDBC + \angleBCD
(exterior angles is equal to sum of two interior opposite angles)
Ext \angleCDA = 27° + 27° (from (2) and (3)
 \angleCDA = 54° (from (4)) .....(5)
Also, in \triangle ACD
\angle CAD + \angle CDA + \angle ACD = 180^{\circ}
(sum of all angles in a triangle is 180°)
54^{\circ} + 54^{\circ} + Y = 180^{\circ}
108^{\circ} + Y = 180^{\circ} (Y = 180^{\circ} - 108^{\circ})
y = 72^{\circ}
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5. (a) In the figure (1) given below, ABC is an equilateral triangle. Base BC is produced to E, such that BC'= CE. Calculate \angle ACE and \angle AEC.

(b) In the figure (2) given below, prove that \angle BAD : \angle ADB = 3 : 1.

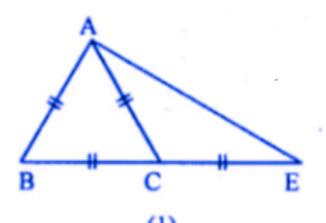
(c) In the figure (3) given below, AB || CD. Find the values of x, y and \angle .



Solution:



(a) in following figure Given. ABC is an equilateral triangle BC = CE To find. $\angle ACE$ and $\angle AEC$

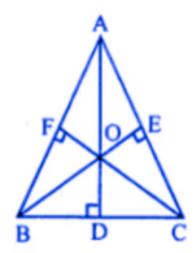


As given that ABC is an equilateral triangle, That is $\angle BAC = \angle B = \angle ACB = 60^{\circ}$ (1) (each angle of an equilateral triangle is 60°) Now, $\angle ACE = \angle BAC + CB$ (Exterior angle is equal to sum of two interior opposite angles) ($\angle ACE = 60^{\circ} + 60^{\circ}$)

6. In the given figure, AD, BE and CF arc altitudes of \triangle ABC. If AD = BE = CF, prove that ABC is an equilateral triangle.

Given : in the figure given, AD, BE and CF are altitudes of \triangle ABC and AD = BE = CF

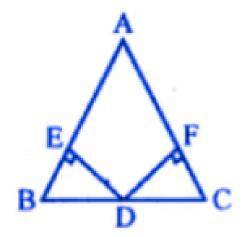




To prove : $\triangle ABC$ is an equilateral triangle Proof: in the right $\triangle BEC$ and $\triangle BFC$ Hypotenuse BC = BC (Common) Side BE = CF (Given) $\triangle BEC \cong \triangle BFC$ (RHS axiom) $\angle C = \angle B$ AB = AC (sides opposite to equal angles) Similarly we can prove that $\triangle CFA \cong \triangle ADC$ $\angle A = \angle C$ AB = BC From (i) and (ii) AB = BC = AC $\triangle ABC$ is an equilateral triangle

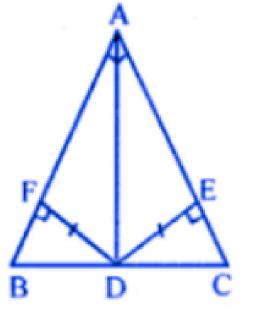
7. In the given figure, D is mid-point of BC, DE and DF are perpendiculars to AB and AC respectively such that DE = DF. Prove that ABC is an isosceles triangle.





Solution:

In triangle ABC D is the midpoint of BC DE perpendicular to AB And DF perpendicular to AC DE = DE



To prove: Triangle ABC is an isosceles triangle Proof: In the right angled triangle BED and CDF Hypotenuse BD = DC (because D is a midpoint)



Side DF = DE (given) $\Delta BED \cong \Delta CDF$ (RHS axiom) $\angle C = \angle B$ AB = AC (sides opposite to equal angles) ΔABC is an isosceles triangle



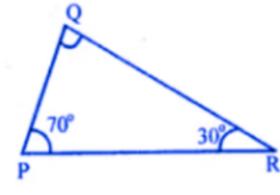


EXERCISE 10.4

1. In $\triangle PQR$, $\angle P = 70^{\circ}$ and $\angle R = 30^{\circ}$. Which side of this triangle is longest? Give reason for your answer.

Solution:

In $\triangle PQR$, $\angle P = 70^{\circ}$, $\angle R = 30^{\circ}$ But $\angle P + \angle Q + \angle R = 180^{\circ}$ $100^{\circ} + \angle Q = 180^{\circ}$

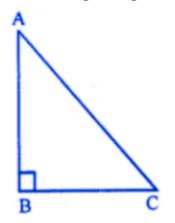


 $\angle Q = 180^{\circ} - 100^{\circ} = 180^{\circ}$ $\angle Q = 80^{\circ}$ the greatest angle Its opposite side PR is the longest side (side opposite to greatest angle is longest)

2. Show that in a right angled triangle, the hypotenuse is the longest side.

Solution:

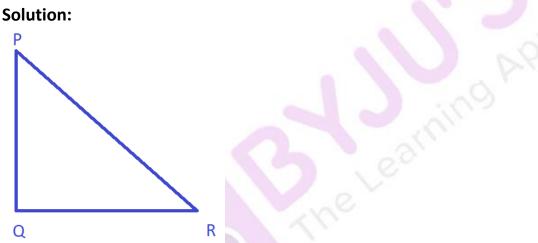
Given: in right angled $\triangle ABC$, $\angle B = 90^{\circ}$





To prove: AC is the longest side Proof : in \triangle ABC, \angle B = 90° \angle A and \angle C are acute angles That is less then 90° \angle B is the greatest angle Or \angle B> \angle C and \angle B> \angle A AC > AB and AC > BC Hence AC is the longest side

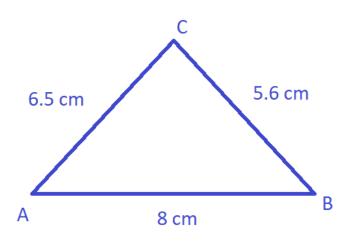
3. PQR is a right angle triangle at Q and PQ : QR = 3:2. Which is the least angle.



Here, PQR is a right angle triangle at Q. Also given that PQ : QR = 3:2 Let PQ = 3x, then, QR = 2xIt is clear that QR is the least side, Then, we know that the least angle has least side Opposite to it. Hence $\angle P$ is the least angle

4. In \triangle ABC, AB = 8 cm, BC = 5.6 cm and CA = 6.5 cm. Which is (i) the greatest angle ? (ii) the smallest angle ?





Solution:

Given that AB = 8 cm, BC = 5.6 cm, CA = 6.5 cm.

Here AB is the greatest side

Then $\angle C$ is the least angle

The greatest side has greatest angle opposite to it)

Also, BC Is the least side

Then $\angle A$ is the least angle

(the least side has least angle opposite to it)



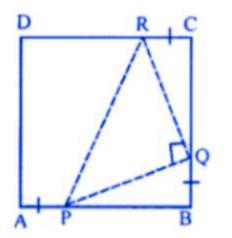
CHAPTER TEST

1. In triangles ABC and DEF, $\angle A = \angle D$, $\angle B = \angle E$ and AB = EF. Will the two triangles be congruent? Give reasons for your answer.

Solution:

In $\triangle ABC$ and $\triangle DEF$ $\angle A = \angle D$ $\angle B = \angle E$ AB = EFIn $\triangle ABC$, two angles and included side is Given but in $\triangle DEF$, corresponding angles are Equal but side is not included of there angle. Triangles Cannot be congruent.

2. In the adjoining figure, ABCD is a square. P, Q and R are points on the sides AB, BC and CD respectively such that AP= BQ = CR and \angle PQR = 90°. Prove that (a) \triangle PBQ \cong \triangle QCR (b) PQ = QR (c) \angle PRQ = 45°



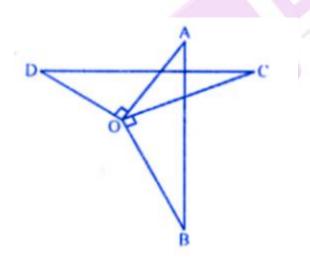
Solution:

Given : in the given figure, ABCD is a square P,Q and R are the Points on the sides AB, BC and CD respectively such that AP = BQ = CR, \angle PQR = 90° To prove: (a) \triangle PBQ = \triangle QCR (b) PQ = QR



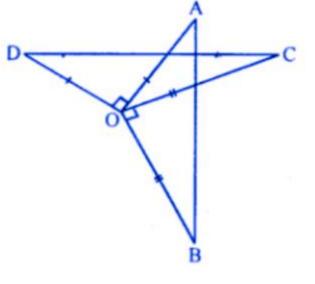
(c) ∠PQR = 45° Proof : AB = BC = CD (Sides of Square) And AP = BQ = CR (Given) Subtracting, we get AB - AP = BC - BQ = CD - CR(PB = QC = RD)Now in $\triangle PBQ$ and $\angle QCR$ PB = QC (Proved) BQ = CR (Given) $\angle B = \angle C$ (Each 90°) $\Delta PBQ \cong \Delta QCR$ PQ = QRBut $\angle PQR = 90^{\circ}$ $\angle RPQ = \angle PQR$ (Angles opposite to equal angles) But $\angle RPQ + \angle PRQ = 90^{\circ}$ $\angle RPQ = \angle PQR = 90^{\circ}$ $\angle RPQ = \angle PRQ = 90^{\circ}/2 = 45^{\circ}$

3. In the given figure, $OA \perp OD$, $OC \times OB$, OD = OA and OB = OC. Prove that AB = CD.



Solution : Given : in the figure OA \perp OD, OC \perp OB.

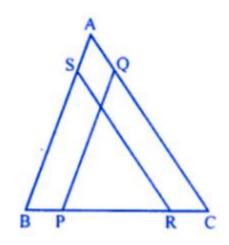




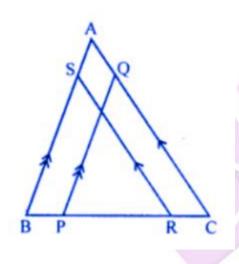
To prove : AB = CDProof : $\angle AOD = \angle COB$ (each 90°) Adding $\angle AOC$ $\angle AOD + \angle AOC = \angle AOC + \angle COB$ $\angle COD = \angle AOB$ Now, in $\triangle AOB$ and $\triangle DOC$ OA = OD (Given) OB = OC (Given) $\angle AOB = \angle COD$ (Proved) $\triangle AOB \cong \triangle DOC$ AB = CD

4. In the given figure, PQ || BA and RS CA. If BP = RC, prove that: (i) Δ BSR $\cong \Delta$ PQC (ii) BS = PQ (iii) RS = CQ.





Solution: PQ || BA, RS || CA BP = RC



To prove : (i) \triangle BSR $\cong \triangle$ PQC (ii) RS = CQ Proof : BP = RC BC - RC = BC - BP BR = PC Now, in \triangle BSR and \triangle PQC \angle B = \angle P (Corresponding angles) \angle R = \angle C (Corresponding angles) BR = PC (Proved)



 Δ BSR $\cong \Delta$ PQC BS = PQ RS = CQ

