

# RBSE Class 10th Maths Question Paper With Solution 2019

QUESTION PAPER CODE S-09-Mathematics

## PART - A

**Question 1: Find the square of 62 by Dwandwa yoga method.**

**Solution:**

Simplify the expression,

Dwandwa of 6 / dwandwa of 62 / dwandwa of 2

$$= 36 / 2 * 6 * 2 / 2^2$$

$$= 36 / 24 / 4$$

$$= 3844$$

The square of 62 is 3844.

**Question 2: Solve :  $(x + 1)(x + 2) = (x - 5)(x - 6)$ .**

**Solution:**

$$(x + 1)(x + 2) = (x - 5)(x - 6)$$

$$a = 1, b = 2, c = -5, d = -6$$

$$x = [cd - ab] / [a + b - c - d]$$

$$= [30 - 2] / [1 + 2 + 5 + 6]$$

$$= 28 / 14$$

$$= 2$$

Hence, the value is 2.

**Question 3: Find the HCF of 68 and 119.**

**Solution:**

The prime factorization of 68 and 119 is as follows :

$$68 = 2 * 2 * 17$$

$$119 = 7 \times 17$$

Therefore, the required H.C.F. of 68 and 117 will be,

$$\text{H.C.F.}(68, 119) = 17$$

Thus, the required H.C.F. is 17.

**Question 4: Find the value of  $\tan^2 60^\circ + 3\cos^2 30^\circ$ .**

**Solution:**

$$\begin{aligned}\tan^2 60^\circ + 3 \cos^2 30^\circ \\ &= (\sqrt{3})^2 + 3 \times (\sqrt{3} / 2)^2 \\ &= 3 + 3 \times 3 / 4 \\ &= (12 + 9) / 4 \\ &= 21 / 4\end{aligned}$$

**Question 5: If  $\sin 2A = \cos (A - 18^\circ)$ , then find the value of A.**

**Solution:**

$$\begin{aligned}\sin 2A &= \cos (A - 18^\circ) \\ \Rightarrow \cos (90^\circ - 2A) &= \cos (A - 18^\circ) \\ \Rightarrow 90^\circ - 2A &= A - 18^\circ \\ \Rightarrow 2A + A &= 90^\circ + 18^\circ \\ \Rightarrow 3A &= 108^\circ \\ \Rightarrow A &= 36^\circ\end{aligned}$$

**Question 6: Write the locus of the centre of a rolling circle in a plane.**

**Solution:**

The locus is a circle of between with inset of planes from a given point with a 2-dimensional plane. It will provide the parallel plane provided by the centre of the rolling circle in a plane. A cycloid is the aim of the centre of the rolling circle in a plane.

**Question 7: If  $\triangle ABC \sim \triangle DEF$  in which  $AB = 1.6\text{cm}$  and  $DE = 2.4\text{cm}$ . Find the ratio of the areas of  $\triangle ABC$  and  $\triangle DEF$ .**

**Solution:**

For similar triangles, the ratio of the area of triangles = ratios of the square of their corresponding sides.

$$\text{Area of } \triangle ABC / \text{area of } \triangle DEF = AB^2 / DE^2$$

$$= [1.6 * 1.6] / [2.4 * 2.4]$$

$$= 2.56 / 5.76$$

$$= 4 / 9$$

The ratio is 4:9.

**Question 8: Two players A and B played a chess match. It is given that the probability of winning the match by A is  $5 / 6$ . Find the probability of winning the match by B.**

**Solution:**

$$P(A) + P(B) = 1$$

$$[5 / 6] + P(B) = 1$$

$$1 - [5 / 6] = P(B)$$

$$= [6 - 5] / 6$$

$$P(B) = 1 / 6$$

**Question 9: If the fare of a car for the first kilometre is Rs. 20 and for after 1 kilometre is Rs. 11, then find the total fare for 15 kilometres.**

**Solution:**

Fare for first km = Rs 20

After first km = Rs 11 per km

Fare of 15 km = Fare of 1<sup>st</sup> km + Fare of next 14 km

$$= 20 + 11 * 14$$

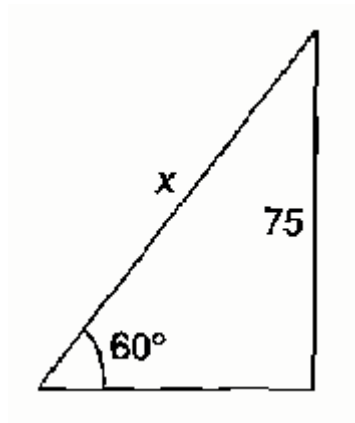
$$= 20 + 154$$

$$= 174$$

Rs 174 is the fare for 15 km.

**Question 10:** A kite is flying at a height of 75 metres from the level of ground attached to a string inclined at  $60^\circ$  to the horizontal. Find the length of the string.

**Solution:**



$$\begin{aligned}\sin 60^\circ &= 75 / x \\ x &= 75 / \sin 60^\circ \\ &= 75 / [\sqrt{3} / 2] \\ &= 150 / \sqrt{3} \\ &= 50\sqrt{3} \text{ m}\end{aligned}$$

The length of this string is  $50\sqrt{3}\text{m}$ .

### PART - B

(2 \* 5 = 10)

**Question 11:** Find the cube of 42 by using Upsutra Anurupyena.

**Solution:**

Cube of 42 by Upsutra Anurupyena method:

I II III IV

$$\begin{array}{r} 4^3 * 4^2 \times 2 \quad 4 \times 2^2 * 2^3 \\ 64 \quad 32 \quad 16 \quad 8 \\ +64 \quad +32 \\ \hline 64 \quad 96 \quad 48 \quad 8 \end{array}$$

$$\begin{aligned}
&= 64 / 96 / 48 / 8 \\
&= 64 / 96 / 48 / 8 \\
&= 73 / 10 / 8 / 8 \\
&= 73 / 10 / 8 / 8 \\
&= 74 / 0 / 8 / 8 \\
&= 74088
\end{aligned}$$

**Question 12: Prove that  $7\sqrt{5}$  is an irrational number.**

**Solution:**

Let us assume that  $7\sqrt{5}$  is a rational number

Hence  $7\sqrt{5}$  can be written in the form of  $a / b$ , where  $a, b$  ( $b \neq 0$ ) are co-prime.

$$\Rightarrow 7\sqrt{5} = a / b$$

$$\Rightarrow \sqrt{5} = a / 7b$$

But here  $\sqrt{5}$  is irrational and  $a / 7b$  is rational.

As rational  $\neq$  irrational, the assumption is a contradiction.

Hence,  $7\sqrt{5}$  is an irrational number.

**Question 13: Radius of a circle is 9cm and the angle of the sector is  $70^\circ$ . Find the area of the minor sector of the circle.**

**Solution:**

Given, radius  $r = 9$  units

Angle  $\theta = 70^\circ$

Area of the minor sector  $= \theta * \pi r^2 / 360^\circ$

$$= [70^\circ * (22 / 7) * 9^2] / 360^\circ$$

$$= 49.48 \text{ square units}$$

**Question 14: The height of a cylinder is 21cm and its curved surface area is  $924\text{cm}^2$ . Find the radius of the cylinder.**

**Solution:**

The curved surface area of cylinder  $= 2\pi rh$

$$924 = 2 \times [22 / 7] \times r \times [21]$$

$$924 = 2 \times 22 \times 3 \times r$$

$$462 = 22 \times 3 \times r$$

$$154 = 22 \times r$$

$$r = 7\text{cm}$$

**Question 15:** The distance between A and B is 125 km and there are Eight(8) traffic signals in between A and B. If a car by 50 km/h speed reaches point B crossing all green signals in 2 hours and 30 minutes but on other days due to heavy traffic it happens to stop as follows. First Traffic Signal - 1 minute, Second Traffic Signal - 2 minutes and up to Eight(8th) signal - 8 minutes. Calculate the total time taken by that car if it follows the total traffic signals.

**Solution:**

According to the question,

$$A - B = 125\text{km}$$

$$\text{Speed of the car} = 50 \text{ km/hr}$$

$$T = 125 / 50 = 2.5 \text{ hours}$$

An arithmetic sequence is 1, 2, 3 ..... 8.

$$a = 1$$

$$d = 1$$

$$n = 8$$

$$S_n = [n / 2] [2a + [n - 1] d]$$

$$= [8 / 2] [2 * 1 + (8 - 1) * 1]$$

$$= [4] * [9]$$

$$= 36 \text{ minutes}$$

$$= 2.5 \text{ hours} + 36 \text{ minutes}$$

$$= 3 \text{ hours } 6 \text{ minutes}$$

## PART - C

(10 \* 3 = 30)

**Question 16:** Solve  $1 / [x - 2] + 2 / [x - 1] = 6 / x$ , where  $x \neq 1, 2$  by factorisation method.

**Solution:**

$$1 / (x - 2) + 2 / (x - 1) = 6 / x$$

$$\Rightarrow (x - 2) + 2(x - 2) / (x - 2)(x - 1) = 6 / x$$

$$\Rightarrow 3x - 5 / x^2 - 3x + 2 = 6 / x$$

$$\Rightarrow 3x^2 - 5x = 6x^2 - 18x + 12$$

$$\Rightarrow 3x^2 - 13x + 12 = 0$$

By using the factorization method,

$$\Rightarrow 3x^2 - 13x + 12 = 0$$

$$\Rightarrow 3x^2 - 9x - 4x + 12 = 0$$

$$\Rightarrow 3x(x - 3) - 4(x - 3) = 0$$

$$\Rightarrow (x - 3)(3x - 4) = 0$$

$$\Rightarrow x - 3 = 0 \text{ or } 3x - 4 = 0$$

$$\Rightarrow x = 3, 4 / 3$$

Here,  $x = 3, 4 / 3$ .

**Question 17: Find the sum of all the natural numbers divisible by 5 between 2 and 101.**

**Solution:**

The numbers are 5, 10, 15,..... 100

Here,  $a = 5$

$$d = 10 - 5 = 5$$

To find the number of terms 'n'.

$$a_n = a + (n - 1)d$$

$$100 = 5 + (n - 1) 5$$

$$100 = 5 + 5n - 5$$

$$100 = 5n$$

$$n = 100 / 5 = 20$$

To find the sum of natural numbers divisible by 5.

$$S_n = [n / 2] [2a + (n - 1)d]$$

$$= [20 / 2] [2 * 5 + 19 * 5]$$

$$= 10 [10 + 95]$$

$$= 1050$$

The sum of natural numbers divisible by 5 between 2 and 101 is 1050.

**Question 18:** From a point on the ground which is 120m away from the foot of the unfinished tower, the angle of elevation of the top of the tower is found to be  $30^\circ$ . Find how much height the tower has to increase so that its angle of elevation at the same point becomes  $60^\circ$ ?

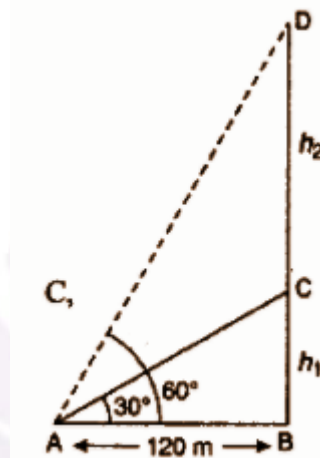
**Solution:**

Let BC is an incomplete tower with height  $h_1$ .

Point A is 120 m distance from its base B, the angle of elevation is  $30^\circ$  from its top, i.e.,  $\angle BAC = 30^\circ$ .

Let the tower be given height  $h_2$ m till point D.

So that angle of elevation becomes  $60^\circ$  from point A.



$$\angle BAD = 60^\circ$$

From right-angled  $\triangle ABC$ ,

$$\tan 30^\circ = BC / AB$$

$$1 / \sqrt{3} = h_1 / 120$$

$$h_1 = 120 / \sqrt{3}$$

$$= 40\sqrt{3} \text{ m}$$

From right angled  $\triangle ABD$ ,

$$\tan 60^\circ = BD / AB$$

$$\sqrt{3} = (h_1 + h_2) / 120$$

$$h_1 + h_2 = 120\sqrt{3}$$

$$40\sqrt{3} + h_2 = 120\sqrt{3}$$

$$h_2 = 120\sqrt{3} - 40\sqrt{3}$$

$$= 80\sqrt{3} \text{ m}$$

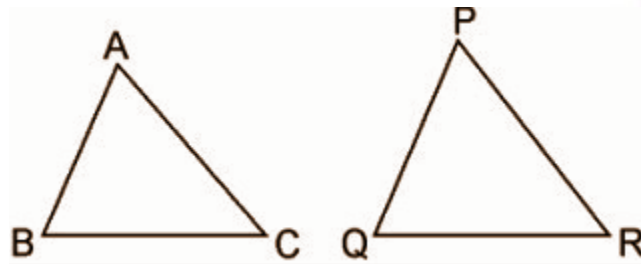
$$= 80 \times 1.732$$

$$CD = 138.56 \text{ m}$$

Hence, 138.56 m height of the tower has to be increased.

**Question 19: Prove that if the area of two similar triangles is equal, then they are congruent.**

**Solution:**



Use the theorem that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides, then prove that they are congruent.

To prove:  $\triangle ABC \cong \triangle PQR$

Given:

$$\triangle ABC \sim \triangle PQR$$

$$\text{Area of } \triangle ABC = \text{Area of } \triangle PQR$$

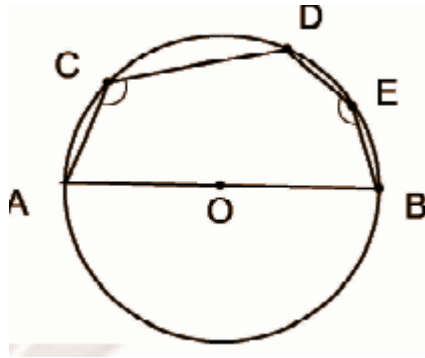
$$\text{Area of } \triangle ABC / \text{area of } \triangle PQR = 1$$

$$\Rightarrow AB^2 / PQ^2 = BC^2 / QR^2 = CA^2 / PR^2 = 1$$

$$\Rightarrow AB = PQ, BC = QR \text{ \& } CA = PR$$

Thus,  $\triangle ABC \cong \triangle PQR$  [By SSS criterion of congruence].

**Question 20: In fig. AOB is the diameter of a circle and C, D and E are three points situated on a semi-circle. Find the value of  $\angle ACD + \angle BED$ .**



**Solution:**

Construction: Join CO, DO and EO

Assume  $AC = CD = AO$

Assume  $DE = EB$

In  $\triangle ACO$ , it is an equilateral triangle, hence  $\angle ACO = 60^\circ$

In  $\triangle CDO$ , it is an equilateral triangle, hence  $\angle DCO = 60^\circ$

$$\angle DOE = \angle EOB$$

$$\text{As } \angle AOB = 180^\circ$$

$$180^\circ = \angle AOC + \angle COD + \angle DOE + \angle EOB$$

$$\angle AOC = \angle COD = 60^\circ$$

$$\angle DOE = \angle EOB$$

$$2\angle DOE = 180^\circ - 60^\circ - 60^\circ$$

$$\angle DOE = 30^\circ$$

In  $\triangle ODE$ ,  $\angle ODE = \angle OED$  (isosceles triangle)

$$\angle ODE + \angle OED + \angle DOE = 180^\circ$$

$$2\angle ODE = 180^\circ - 30^\circ = 150^\circ$$

$$\angle ODE = 75^\circ$$

In  $\triangle OEB$ ,  $\angle OEB = \angle OBE$  (isosceles triangle)

$$\angle OEB + \angle OEB + \angle BOE = 180^\circ$$

$$2\angle OEB = 180^\circ - 30^\circ = 150^\circ$$

$$\angle OEB = 75^\circ$$

$$\angle ACD + \angle BED$$

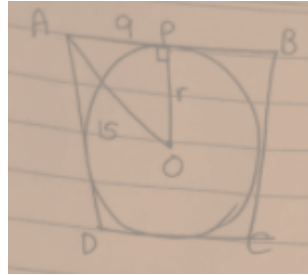
$$= \angle ACO + \angle DCO + \angle DEO + \angle BEO$$

$$= 60^\circ + 60^\circ + 75^\circ + 75^\circ$$

$$= 270^\circ$$

**Question 21:** A circle with centre 'O' touches all the four sides of a quadrilateral. ABCD internally in such a way that it divides AB in 3:1 and AB = 12cm then find the radius of the circle where OA = 15 cm.

**Solution:**



$$OA = 15 \text{ cm}$$

Say, the circle touches AB at P.

AB is divided by P in 3:1

$$AP = (3 / (3 + 1)) * AB$$

$$= 3AB / 4$$

$$= 3 * [12 / 4]$$

$$= 9 \text{ cm}$$

$$OA^2 = OP^2 + AP^2$$

$$\Rightarrow 15^2 = OP^2 + 9^2$$

$$\Rightarrow 225 = OP^2 + 81$$

$$\Rightarrow OP^2 = 144$$

$$\Rightarrow OP = 12 \text{ cm}$$

$$\text{Radius} = 12 \text{ cm}$$

**Question 22:** Construct an incircle of an equilateral triangle with side 5 cm.

**Solution:**

An equilateral triangle ABC in which AB = BC = CA = 5 cm.

Construction of  $\triangle ABC$

(1) Draw a line segment BC = 5 cm.

(2) Draw an arc of radius = 5 cm taking B as the centre.

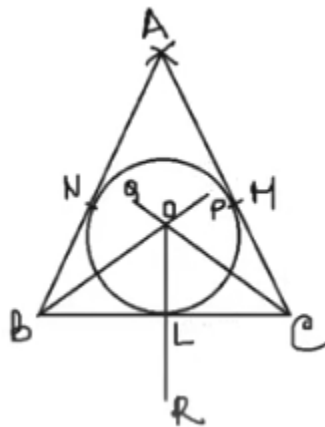
- (3) Draw another arc of radius = 5 cm taking B as the centre.
- (4) Draw another arc of radius = 5 cm taking C as a centre which intersects the previous arc at a point A.
- (5) Join AB and AC.

Thus the required  $\triangle ABC$  is constructed.

Construction of incircle of  $\triangle ABC$

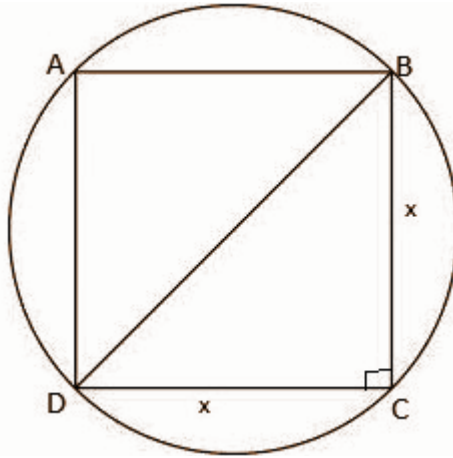
- (1) Draw BP and CQ the bisectors of angles  $\angle B$  and  $\angle C$  respectively and which intersect each other at point O.
- (2) Draw  $OR \perp BC$  which intersects BC at L.
- (3) Taking O as the centre and OL as radius draw a circle which touches the sides AB, BC and CA at points N, L and M respectively.
- (4) Measure the radius OL.

Thus the required incircle is constructed.



**Question 23:** Find the area of the square inscribed in a circle of radius 10cm.

**Solution:**



Radius =  $r = 10\text{cm}$

$\therefore$  The diagonals of the square subtend the right angle at circumference.

$\therefore$  The diagonals of the square are diameters of the circle.

$$BD = 2 * 10 = 20\text{cm}$$

Let the sides of the square be ' $x$ ' cm

In the right angle triangle BCD,

$$BC^2 + CD^2 = BD^2$$

$$x^2 + x^2 = 20^2$$

$$2x^2 = 400$$

$$x^2 = 200$$

Thus the area of the square is  $x^2 = 200\text{cm}^2$ .

**Question 24:** A sphere of 6cm diameter is dropped into a cylindrical vessel of diameter 12cm. Find the rise in water in the vessel.

**Solution:**

Diameter of the sphere ( $d$ ) = 6cm

Radius of the sphere ( $r$ ) =  $d / 2 = 6 / 2 = 3\text{cm}$

Diameter of the cylindrical vessel ( $D$ ) = 12 cm

Radius of the cylindrical vessel ( $R$ ) =  $12 / 2 = 6\text{ cm}$

Level of water raised =  $h$  cm

According to the problem given, the volume of the water raised in the vessel = volume of the sphere

$$\pi R^2 h = \left[ \frac{4}{3} \right] \times \pi r^3$$

$$h = (4 \times r^3) / (3 \times R^2)$$

$$h = (4 \times 3 \times 3 \times 3) / (3 \times 6 \times 6)$$

$$h = 1 \text{ cm}$$

Therefore, the level of water raised in the vessel =  $h = 1 \text{ cm}$

**Question 25: A bag contains 15 cards. The numbers 1, 2, 3, 4, ....., 15 are printed on them. A card is at random drawn from the bag. Find the probability that the number on the card is**

**(i) a prime number**

**(ii) a number is divisible by 2**

**Solution:**

Total number of cards = 15

Probability of an event = Number of favourable outcomes / total number of outcomes

(i) For a prime number:

Sample space = {2, 3, 5, 7, 11, 13}

Number of prime numbers = 6

$$P(\text{getting a prime number}) = 6 / 15 = 2 / 5$$

(ii) For a number divisible by 2:

Sample space = {2, 4, 6, 8, 10, 12, 14}

Number of numbers divisible by 2 = 7

$$P(\text{getting a number divisible by 2}) = 7 / 15$$

## PART - D

$$[5 * 6 = 30]$$

**Question 26: Solve the following pair of linear equations by graphical method.  $3x - 5y = -1$  and  $2x - y = -3$ . Thus find the value of A in the relation  $(x + y)^2 = A$ .**

**Solution:**

$$3x - 5y = -1 \text{ ---- (1)}$$

$$2x - y = -3 \text{ ----- (2)}$$

$$2x + 3 = y \text{ ---- (3)}$$

Putting (3) in (1)

$$3x - 5[2x + 3] = -1$$

$$3x - 10x - 15 = -1$$

$$-7x - 15 = -1$$

$$-7x = 14$$

$$x = 14 / -7$$

$$x = -2$$

Putting  $x = -2$  in (1),

$$3(-2) - 5y = -1$$

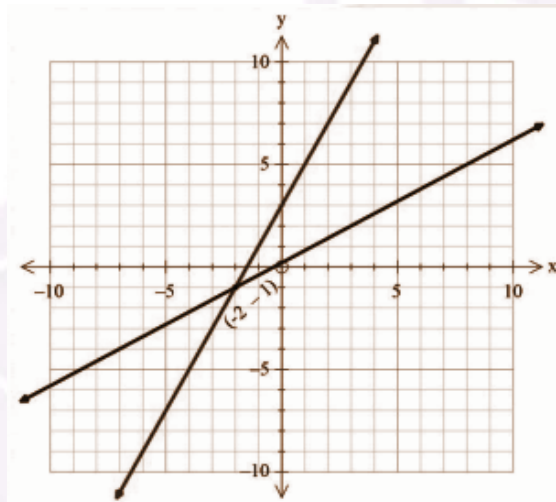
$$-6 - 5y = -1$$

$$-6 + 1 = 5y$$

$$-5 = 5y$$

$$y = -5 / 5$$

$$y = -1$$



$$(x + y)^2 = (-2 - 1)^2 = -3^2 = 9$$

The value of  $A = 9$ .

**Question 27: Prove that**

$$[a] \ [1 + \sec A] / \sec A = \sin^2 A / [1 - \cos A]$$

$$[b] \ \cos^2 \theta / [1 - \tan \theta] + \sin^3 \theta / [\sin \theta - \cos \theta] = 1 + \sin \theta \cos \theta$$

**OR**

**Prove that**

$$[a] \sin \theta / [1 + \cos \theta] + [1 + \cos \theta] / \sin \theta = 2 \operatorname{cosec} \theta$$

$$[b] [\sin \theta - 2\sin^3 \theta] / [2 \cos^3 \theta - \cos \theta] = \tan \theta$$

**Solution:**

$$\begin{aligned} [a] \text{ LHS} &= (1 + \sec A) / \sec A \\ &= (1 + 1 / \cos A) / (1 / \cos A) \\ &= [(\cos A + 1) / \cos A] / (1 / \cos A) \\ &= \cos A + 1 \\ &= (1 + \cos A) (1 - \cos A) / (1 - \cos A) \\ &= (1 - \cos^2 A) / (1 - \cos A) \\ &= \sin^2 A / (1 - \cos A) \\ &= \text{RHS} \end{aligned}$$

$$\begin{aligned} [b] \text{ LHS} &= \cos^2 \theta / [1 - \tan \theta] + \sin^3 \theta / [\sin \theta - \cos \theta] = 1 + \sin \theta \cos \theta \\ &= \cos^2 \theta / [1 - (\sin \theta / \cos \theta)] + \sin^3 \theta / [\sin \theta - \cos \theta] \\ &= [\cos^3 \theta / \cos \theta - \sin \theta] - \sin^3 \theta / [\sin \theta - \cos \theta] \\ &= [\cos \theta - \sin \theta] [\cos^2 \theta + \sin^2 \theta + \sin \theta \cos \theta] / [\cos \theta - \sin \theta] \\ &= 1 + \sin \theta \cos \theta \\ &= \text{RHS} \end{aligned}$$

**OR**

$$\begin{aligned} [a] \text{ L.H.S.} &= \sin \theta / [1 + \cos \theta] + [1 + \cos \theta] / \sin \theta \\ &= \sin^2 \theta + (1 + \cos \theta)^2 / \sin \theta (1 + \cos \theta) \\ &= \sin^2 \theta + (1 + 2 \cos \theta + \cos^2 \theta) / \sin \theta (1 + \cos \theta) \\ &= (\sin^2 \theta + \cos^2 \theta) + 1 + 2 \cos \theta / \sin \theta (1 + \cos \theta) \\ &= 1 + 1 + 2 \cos \theta / \sin \theta (1 + \cos \theta) \\ &= 2 + 2 \cos \theta / \sin \theta (1 + \cos \theta) \\ &= 2 (1 + \cos \theta) / \sin \theta (1 + \cos \theta) \\ &= 2 / \sin \theta \\ &= 2 \operatorname{cosec} \theta \\ &= \text{RHS} \end{aligned}$$

$$[b] \text{ LHS} = [\sin \theta - 2\sin^3 \theta] / [2 \cos^3 \theta - \cos \theta] = \tan \theta$$

$$\begin{aligned}
& (\sin \theta - 2 \sin^3 \theta) / (2 \cos^3 \theta - \cos \theta) \\
&= \sin \theta (1 - 2 \sin^2 \theta) / \cos \theta (2 \cos^2 \theta - 1) \\
&= \sin \theta [1 - 2 (1 - \cos^2 \theta)] / \cos \theta (2 \cos^2 \theta - 1) \\
&= \sin \theta [1 - 2 + 2 \cos^2 \theta] / \cos \theta (2 \cos^2 \theta - 1) \\
&= \sin \theta (2 \cos^2 \theta - 1) / \cos \theta (2 \cos^2 \theta - 1) \\
&= \sin \theta / \cos \theta \\
&= \tan \theta
\end{aligned}$$

**Question 28:** If there are four points P (2, -1), Q (3, 4), R (-2, 3) and S (-3, -2) in a plane, then prove that PQRS is not a square but a rhombus.

**Solution:**

$$\begin{aligned}
PQ &= \sqrt{(3-2)^2 + (4+1)^2} = \sqrt{1^2 + 5^2} = \sqrt{26} \text{ units} \\
QR &= \sqrt{(-2-3)^2 + (3-4)^2} = \sqrt{25 + 1} = \sqrt{26} \text{ units} \\
RS &= \sqrt{(-3+2)^2 + (-2-3)^2} = \sqrt{1 + 25} = \sqrt{26} \text{ units} \\
SP &= \sqrt{(-3-2)^2 + (-2-3)^2} = \sqrt{26} \text{ units} \\
PR &= \sqrt{(-2-2)^2 + (3+1)^2} = \sqrt{16 + 16} = 4\sqrt{2} \text{ units} \\
\text{and, } QS &= \sqrt{(-3-3)^2 + (-2-4)^2} = \sqrt{36 + 36} = 6\sqrt{2} \text{ units} \\
\therefore PQ &= QR = RS = SP = \sqrt{26} \text{ units} \\
\text{and, } PR &\neq QS
\end{aligned}$$

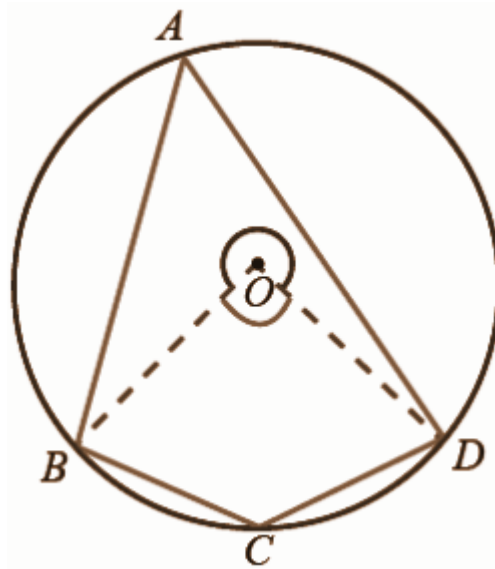
This means that PQRS is a quadrilateral whose sides are equal but diagonals are not equal. Thus, PQRS is a rhombus but not a square.

**Question 29:** Prove that the opposite angles of a cyclic quadrilateral are supplementary or sum is  $180^\circ$ .

**OR**

**Prove that if a chord is drawn from a point of contact of the tangent of the circle then the angle made by this chord with the tangent is equal to the respective alternate angles made by segments with this chord.**

**Solution:**



O is the centre of the circle.

ABCD is the cyclic quadrilateral.

**To prove :**  $\angle BAD + \angle BCD = 180^\circ$ ,  $\angle ABC + \angle ADC = 180^\circ$

Construction: Join OB and OD

Proof:

(i)  $\angle BAD = (1/2) \angle BOD$ . (The angle subtended by an arc at the centre is double the angle on the circle.)

(ii)  $\angle BCD = (1/2) \text{ reflex } \angle BOD$ .

(iii)  $\angle BAD + \angle BCD = (1/2) \angle BOD + (1/2) \text{ reflex } \angle BOD$ .

Add (i) and (ii),

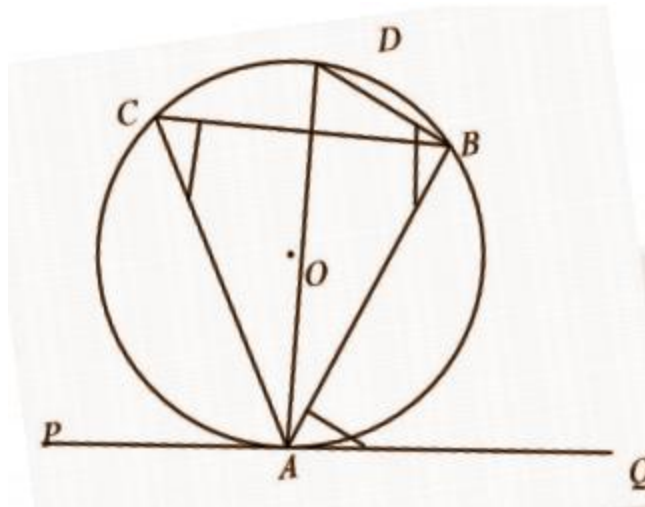
$$\angle BAD + \angle BCD = (1/2) (\angle BOD + \text{reflex } \angle BOD)$$

$\angle BAD + \angle BCD = (1/2) \cdot (360^\circ)$  (Complete angle at the centre is  $360^\circ$ )

$$\angle BAD + \angle BCD = 180^\circ$$

(iv) Similarly  $\angle ABC + \angle ADC = 180^\circ$ .

**OR**



$\angle ACB = \angle ADB$  ---- (i) [circle of segments are equal angles]

$\angle ABD = 90^\circ$  ---- (ii) [make an angle of semicircle]

$\angle DAQ = 90^\circ$  ---- (iii) [DA is perpendicular to PQ]

In the triangle ABD,

$\angle ABD + \angle BAD$  perpendicular to  $\angle ADB = 180^\circ$

$\angle BAD + \angle ADB = 90^\circ$

$\angle BAD + \angle ADB = \angle DAQ$

$\angle BAD + \angle ADB = \angle BAD + \angle BAQ$

$\angle ADB = \angle BAQ$

$\angle ACB = \angle QAB$  [from equation (i)]

**Question 30: Find the median and mode of the following frequency distribution.**

Class	10 - 25	25 - 40	40 - 55	55 - 70	70 - 85	85 - 100
$f_i$	6	20	44	26	3	1

**Solution:**

Class	10 - 25	25 - 40	40 - 55	55 - 70	70 - 85	85 - 100
$f_i$	6	20	44	26	3	1
Cumulative frequency	6	26	70	96	99	100

$$N = 100$$

$$N / 2 = 100 / 2 = 50$$

The cumulative frequency just greater than 44 is 70 and the corresponding class is 40 - 55.

$$l = 40, h = 15, f_1 = 44, f_0 = 20, f_2 = 26$$

$$\begin{aligned}
 \text{Mode} &= l + (f_1 - f_0) / (2f_1 - f_0 - f_2) * h \\
 &= 40 + \{(44 - 20) / (2 * 44 - 20 - 26)\} * 15 \\
 &= 40 + \{(24) / (42)\} * 15 \\
 &= 40 + 8.57 \\
 &= 48.57
 \end{aligned}$$

