

## Exercise 9.2

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1. In Fig. 9.15, ABCD is a parallelogram,  $AE \perp DC$  and  $CF \perp AD$ . If  $AB = 16$  cm,  $AE = 8$  cm and  $CF = 10$  cm, find AD.

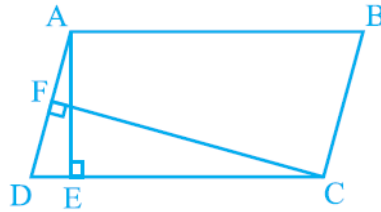


Fig. 9.15

**Solution:**

Given,

$AB = CD = 16$  cm (Opposite sides of a parallelogram)

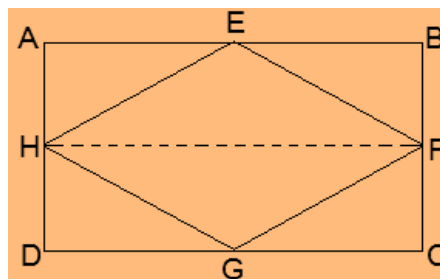
$CF = 10$  cm and  $AE = 8$  cm

Now,

$$\begin{aligned} \text{Area of parallelogram} &= \text{Base} \times \text{Altitude} \\ &= CD \times AE = AD \times CF \\ &\Rightarrow 16 \times 8 = AD \times 10 \\ &\Rightarrow AD = 128/10 \text{ cm} \\ &\Rightarrow AD = 12.8 \text{ cm} \end{aligned}$$

2. If E, F, G and H are respectively the mid-points of the sides of a parallelogram ABCD, show that  $\text{ar}(EFGH) = \frac{1}{2} \text{ar}(ABCD)$ .

**Solution:**



Given,

E, F, G and H are the mid-points of the sides of a parallelogram ABCD respectively.

To Prove,

$$\text{ar}(EFGH) = \frac{1}{2} \text{ar}(ABCD)$$

Construction,

H and F are joined.

Proof,

$AD \parallel BC$  and  $AD = BC$  (Opposite sides of a parallelogram)

$$\Rightarrow \frac{1}{2} AD = \frac{1}{2} BC$$

Also,

$AH \parallel BF$  and  $DH \parallel CF$

$$\Rightarrow AH = BF \text{ and } DH = CF \text{ (H and F are mid points)}$$

$\therefore$ , ABFH and HFCD are parallelograms.

Now,

We know that,  $\triangle EFH$  and parallelogram  $ABFH$ , both lie on the same  $FH$  the common base and in-between the same parallel lines  $AB$  and  $HF$ .

$\therefore$  area of  $EFH = \frac{1}{2}$  area of  $ABFH$  --- (i)

And, area of  $GHF = \frac{1}{2}$  area of  $HFCD$  --- (ii)

Adding (i) and (ii),

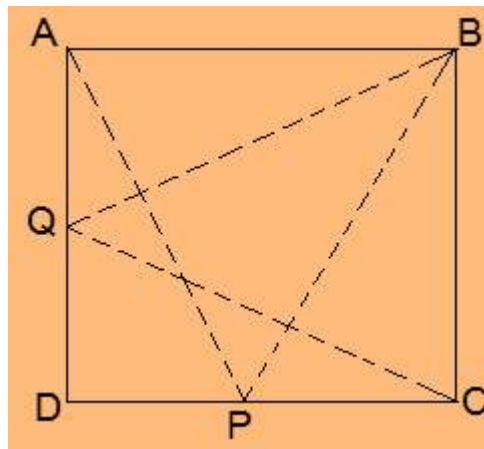
area of  $\triangle EFH$  + area of  $\triangle GHF = \frac{1}{2}$  area of  $ABFH$  +  $\frac{1}{2}$  area of  $HFCD$

$\Rightarrow$  area of  $EFGH =$  area of  $ABFH$

$\therefore$  ar (EFGH) =  $\frac{1}{2}$  ar(ABCD)

**3. P and Q are any two points lying on the sides DC and AD respectively of a parallelogram ABCD. Show that  $\text{ar}(\triangle APB) = \text{ar}(\triangle BQC)$ .**

**Solution:**



$\triangle APB$  and parallelogram  $ABCD$  lie on the same base  $AB$  and in-between same parallel  $AB$  and  $DC$ .

$\therefore$   
 $\text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(\text{parallelogram } ABCD)$  --- (i)

Similarly,

$\text{ar}(\triangle BQC) = \frac{1}{2} \text{ar}(\text{parallelogram } ABCD)$  --- (ii)

From (i) and (ii), we have

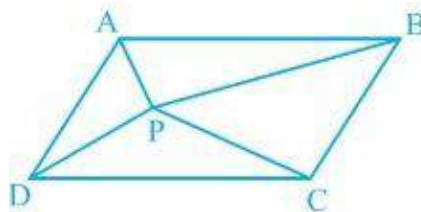
$\text{ar}(\triangle APB) = \text{ar}(\triangle BQC)$

**4. In Fig. 9.16, P is a point in the interior of a parallelogram ABCD. Show that**

**(i)  $\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(\text{ABCD})$**

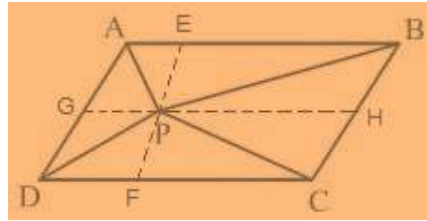
**(ii)  $\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$**

**[Hint : Through P, draw a line parallel to AB.]**



**Fig. 9.16**

**Solution:**



- (i) A line GH is drawn parallel to AB passing through P.

In a parallelogram,

$$AB \parallel GH \text{ (by construction) --- (i)}$$

$\therefore$ ,

$$AD \parallel BC \Rightarrow AG \parallel BH \text{ --- (ii)}$$

From equations (i) and (ii),

ABHG is a parallelogram.

Now,

$\triangle APB$  and parallelogram ABHG are lying on the same base AB and in-between the same parallel lines AB and GH.

$$\therefore \text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(\text{ABHG}) \text{ --- (iii)}$$

also,

$\triangle PCD$  and parallelogram CDGH are lying on the same base CD and in-between the same parallel lines CD and GH.

$$\therefore \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(\text{CDGH}) \text{ --- (iv)}$$

Adding equations (iii) and (iv),

$$\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} [\text{ar}(\text{ABHG}) + \text{ar}(\text{CDGH})]$$

$$\Rightarrow \text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(\text{ABCD})$$

- (ii) A line EF is drawn parallel to AD passing through P.

In the parallelogram,

$$AD \parallel EF \text{ (by construction) --- (i)}$$

$\therefore$ ,

$$AB \parallel CD \Rightarrow AE \parallel DF \text{ --- (ii)}$$

From equations (i) and (ii),

AEDF is a parallelogram.

Now,

$\triangle APD$  and parallelogram AEFD are lying on the same base AD and in-between the same parallel lines AD and EF.

$$\therefore \text{ar}(\triangle APD) = \frac{1}{2} \text{ar}(\text{AEFD}) \text{ --- (iii)}$$

also,

$\triangle PBC$  and parallelogram BCFE are lying on the same base BC and in-between the same parallel lines BC and EF.

$$\therefore \text{ar}(\triangle PBC) = \frac{1}{2} \text{ar}(\text{BCFE}) \text{ --- (iv)}$$

Adding equations (iii) and (iv),

$$\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \frac{1}{2} \{ \text{ar}(\text{AEFD}) + \text{ar}(\text{BCFE}) \}$$

$$\Rightarrow \text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$$

**5. In Fig. 9.17, PQRS and ABRS are parallelograms and X is any point on side BR. Show that**

$$\text{ar}(\text{PQRS}) = \text{ar}(\text{ABRS})$$

$$\text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(\text{PQRS})$$

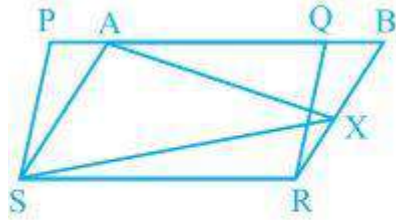


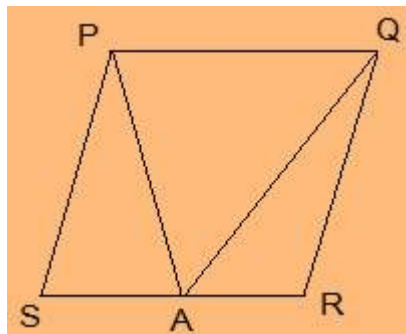
Fig. 9.17

**Solution:**

- (i) Parallelogram PQRS and ABRS lie on the same base SR and in-between the same parallel lines SR and PB.  
 $\therefore \text{ar}(PQRS) = \text{ar}(ABRS) \text{ --- (i)}$
- (ii)  $\triangle AXS$  and parallelogram ABRS are lying on the same base AS and in-between the same parallel lines AS and BR.  
 $\therefore \text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(ABRS) \text{ --- (ii)}$   
 From (i) and (ii), we find that,  
 $\text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(PQRS)$

**6. A farmer was having a field in the form of a parallelogram PQRS. She took any point A on RS and joined it to points P and Q. In how many parts the fields is divided? What are the shapes of these parts? The farmer wants to sow wheat and pulses in equal portions of the field separately. How should she do it?**

**Solution:**



The field is divided into three parts each in triangular shape.

Let,  $\triangle PSA$ ,  $\triangle PAQ$  and  $\triangle QAR$  be the triangles.

$$\text{Area of } \triangle PSA + \triangle PAQ + \triangle QAR = \text{Area of PQRS} \text{ --- (i)}$$

$$\text{Area of } \triangle PAQ = \frac{1}{2} \text{ area of PQRS} \text{ --- (ii)}$$

Here, the triangle and parallelogram are on the same base and in-between the same parallel lines.

From (i) and (ii),

$$\text{Area of } \triangle PSA + \text{Area of } \triangle QAR = \frac{1}{2} \text{ area of PQRS} \text{ --- (iii)}$$

From (ii) and (iii), we can conclude that,

The farmer must sow wheat or pulses in  $\triangle PAQ$  or either in both  $\triangle PSA$  and  $\triangle QAR$ .