

NCERT Solutions For Class 10 Maths Chapter 13- Surface Areas and Volumes

Exercise: 13.4

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1. A drinking glass is in the shape of a frustum of a cone of height 14 cm. The diameters of its two circular ends are 4 cm and 2 cm. Find the capacity of the glass.

Solution:

Radius (r₁) of the upper base = 4/2 = 2 cm Radius (r₂) of lower the base = 2/2 = 1 cm Height = 14 cm Now, Capacity of glass = Volume of frustum of cone So, Capacity of glass = ($\frac{1}{3}$)× π ×h(r₁²+r₂²+r₁r₂) = ($\frac{1}{3}$)× π ×(14)(2²+1²+ (2)(1)) \therefore The capacity of the glass = 102×($\frac{2}{3}$) cm³

2. The slant height of a frustum of a cone is 4 cm and the perimeters (circumference) of its circular ends are 18 cm and 6 cm. Find the surface area of the frustum.

Solution:

Given, Slant height (I) = 4 cm Circumference of upper circular end of the frustum = 18 cm $\therefore 2\pi r_1 = 18$ Or, $r_1 = 9/\pi$ Similarly, circumference of lower end of the frustum = 6 cm $\therefore 2\pi r_2 = 6$ Or, $r_2 = 6/\pi$ Now, CSA of frustum = $\pi(r_1+r_2) \times I$ = $\pi(9/\pi+6/\pi) \times 4$ = $12 \times 4 = 48 \text{ cm}^2$

3. A fez, the cap used by the Turks, is shaped like the frustum of a cone (see Fig.). If its radius on the open side is 10 cm, radius at the upper base is 4 cm and its slant height is 15 cm, find the area of material used for making it.



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Fig. 13.24

Solution:

Given, For the lower circular end, radius $(r_1) = 10$ cm For the upper circular end, radius $(r_2) = 4$ cm Slant height (I) of frustum = 15 cm Now, The area of material to be used for making the fez = CSA of frustum + Area of upper circular end CSA of frustum = $\pi(r_1+r_2)\times I$ = 210 π And, Area of upper circular end = πr_2^2 = 16 π

 \therefore The area of material used = 710 × (2/7) cm²

4. A container, opened from the top and made up of a metal sheet, is in the form of a frustum of a cone of height 16 cm with radii of its lower and upper ends as 8 cm and 20 cm, respectively. Find the cost of the milk which can completely fill the container, at the rate of Rs. 20 per litre. Also find the cost of metal sheet used to make the container, if it costs Rs. 8 per 100 cm².

Solution:

Given, $r_1 = 20 \text{ cm}$, $r_2 = 8 \text{ cm}$ and h = 16 cm \therefore Volume of the frustum = ($\frac{1}{3}$)× π ×h(r_1^2 + r_2^2 + r_1r_2) = $\frac{314 \times 16 \times 208}{100000}$ litres

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It is given that the rate of milk = Rs. 20/litre So, Cost of milk = 20×volume of the frustum

= Rs. 20 ×
$$\frac{314 \times 16 \times 208}{100000}$$

= Rs. 209

Now, slant height will be

$$I = \sqrt{h^2 + (r_1 - r_2)^2} = \sqrt{16^2 + (20 - 8)^2} = \sqrt{16^2 + 12^2}$$

So, CSA of the container = $\pi (r_1 + r_2) \times I$
= $\frac{314}{100} (20 + 8) \times 20 \text{ cm}^2$

= 1758.4 cm²

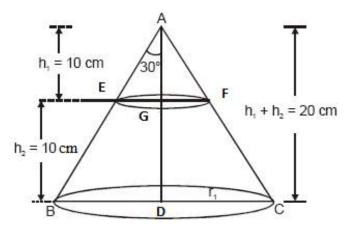
Hence, the total metal that would be required to make container will be = 1758.4 + (Area of bottom circle)

= 1758.4+201 = 1959.4 cm² ∴ Total cost of metal = Rs. (8/100) × 1959.4 = Rs. 157

5. A metallic right circular cone 20 cm high and whose vertical angle is 60° is cut into two parts at the middle of its height by a plane parallel to its base. If the frustum so obtained is drawn into a wire of diameter 1/16 cm, find the length of the wire.

Solution:

The diagram will be as follows



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Consider $\triangle AEG$ $\frac{EG}{AG} = \tan 30^{\circ}$ $EG = \frac{10}{\sqrt{3}} \text{ cm} = \frac{10\sqrt{3}}{3}$ In $\triangle ABD$, $\frac{BD}{AD} = \tan 30^{\circ}$ $BD = \frac{20}{\sqrt{3}} = \frac{20\sqrt{3}}{3} \text{ cm}$

Radius (r_1) of upper end of frustum = (10 $\sqrt{3}$)/3 cm Radius (r_2) of lower end of container = (20 $\sqrt{3}$)/3 cm Height (r_3) of container = 10 cm

Now,

Volume of the frustum = $(\frac{1}{3})\times\pi\times h(r_1^2+r_2^2+r_1r_2)$

$$=\frac{1}{3} \times \pi \times 10 \left[\left(\frac{10\sqrt{3}}{3} \right)^2 + \left(\frac{20\sqrt{3}}{3} \right)^2 + \frac{\left(10\sqrt{3} \right) \left(20\sqrt{3} \right)}{3 \times 3} \right]$$

Solving this we get,

Volume of the frustum = $22000/9 \text{ cm}^3$ The radius (r) of wire = $(1/16)\times(\frac{1}{2}) = 1/32 \text{ cm}$

Now, Let the length of wire be "I". Volume of wire = Area of cross-section x Length = $(\pi r^2)xI$ = $\pi (1/32)^2 x I$

Now, Volume of frustum = Volume of wire $22000/9 = (22/7)x(1/32)^2x I$ Solving this we get, I = 7964.44 m

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