Multiple Choice Questions I

9.1. A ray of light incident at an angle θ on a refracting face of a prism emerges from the other face normally. If the angle of the prism is 5º and the prism is made of a material of refractive index 1.5, the angle of incidence is
a) 7.5º
b) 5º
c) 15º
d) 2.5º
Answer:
a) 7.5º

9.2. A short pulse of white light is incident from air to a glass slab at normal incidence. After travelling through the slab, the first colour to emerge is
a) blue
b) green
c) violet
d) red
Answer:
d) red

9.3. An object approaches a convergent lens from the left of the lens with a uniform speed 5 m/s and stops at the focus. The image
a) moves away from the lens with an uniform speed 5 m/s
b) moves away from the lens with an uniform acceleration
c) moves away from the lens with a non-uniform acceleration
d) moves towards the lens with a non-uniform acceleration
Answer:
c) moves away from the lens with a non-uniform acceleration

9.4. A passenger in an aeroplane shall
a) never see a rainbow
b) may see a primary and a secondary rainbow as concentric circles
c) may see a primary and a secondary rainbow as concentric arcs
d) shall never see a secondary rainbow
Answer:
b) may see a primary and a secondary rainbow as concentric circles

9.5. You are given four sources of light each one providing a light of a single colour- red, blue, green, and yellow. Suppose the angle of refraction for a beam of yellow light corresponding to a particular angle of incidence at the interface of two media is 90o. Which of the following statements is correct if the source of yellow light is replaced with that of other lights without changing the angle of incidence?
a) the beam of red light would undergo total internal reflection
b) the beam of red light would bend towards normal while it gets refracted through the second medium
c) the beam of blue light would undergo total internal reflection
d) the beam of green light would bend away from the normal as it gets refracted through the second medium
Answer:
c) the beam of blue light would undergo total internal reflection

9.6. The radius of curvature of the curved surface of a plano-convex lens is 20 cm. If the refractive index of the material of the lens be 1.5, it will
a) act as a convex lens only for the objects that lie on its curved side
b) act as a concave lens only for the objects that lie on its curved side
c) act as a convex lens irrespective of the side on which the object lies
d) act as a concave lens irrespective of side on which the object lies
Answer:
c) act as a convex lens irrespective of the side on which the object lies

9.7. The phenomena involved in the reflection of radiowaves by ionosphere is similar to
a) reflection of light by a plane mirror
b) total internal reflection of light in air during a mirage
c) dispersion of light by water molecules during the formation of a rainbow
d) scattering of light by the particles of air
Answer:
b) total internal reflection of light in air during a mirage

9.8. The direction of ray of light incident on a concave mirror as shown by PQ while directions in which the ray would travel after reflection is shown by four rays marked 1, 2, 3, and 4. Which of the four rays correctly shows the direction of reflected ray?
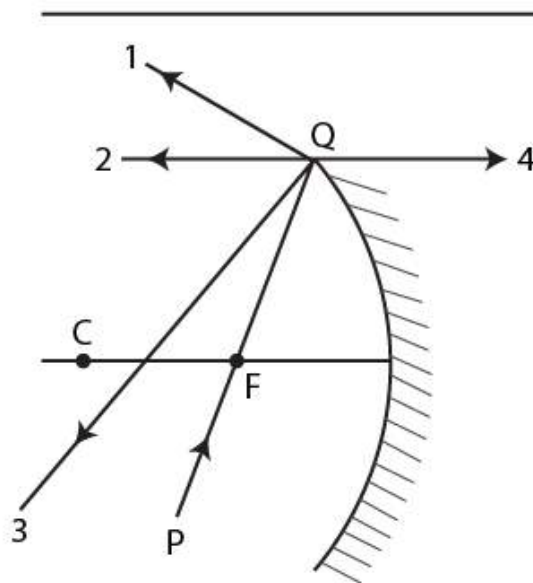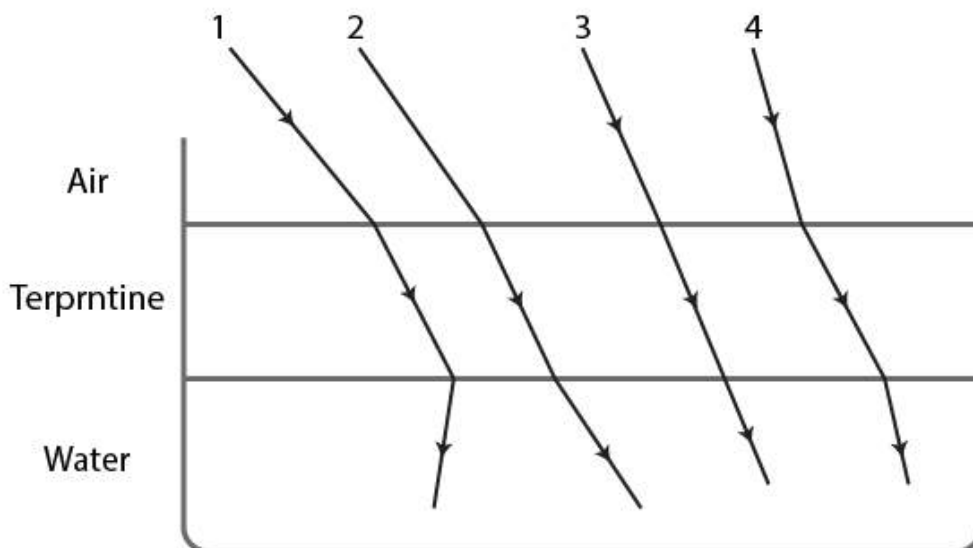

a) 1
b) 2
c) 3
d) 4
Answer:
b) 2

9.9. The optical density of turpentine is higher that that of water while its mass density is lower. The figure shows a layer of turpentine floating over water in a container. For which one of the four rays incident on

turpentine in the figure, the path shown is correct?


a) 1
b) 2
c) 3
d) 4
Answer:
b) 2

9.10 A car is moving with at a constant speed of 60 km h–1 on a straight road. Looking at the rear view mirror, the driver finds that the car following him is at a distance of 100 m and is approaching with a speed of 5 km h –1. In order to keep track of the car in the rear, the driver begins to glance alternatively at the rear and side mirror of his car after every 2 s till the other car overtakes. If the two cars were maintaining their speeds, which of the following statement (s) is/are correct?
(a) The speed of the car in the rear is 65 km h–1.
(b) In the side mirror the car in the rear would appear to approach with a speed of 5 km h–1 to the driver of the leading car.
(c) In the rear view mirror the speed of the approaching car would appear to decrease as the distance between the cars decreases.
(d) In the side mirror, the speed of the approaching car would appear to increase as the distance between the cars decreases.
Answer:
(d) In the side mirror, the speed of the approaching car would appear to increase as the distance between the cars decreases.

9.11 There are certain material developed in laboratories which have a negative refractive index (Fig. 9.3). A ray incident from air (medium 1) into such a medium (medium 2) shall follow a path given by

(a)

1

2

(b)

1

2

(c)

1

2

(d)

1

2
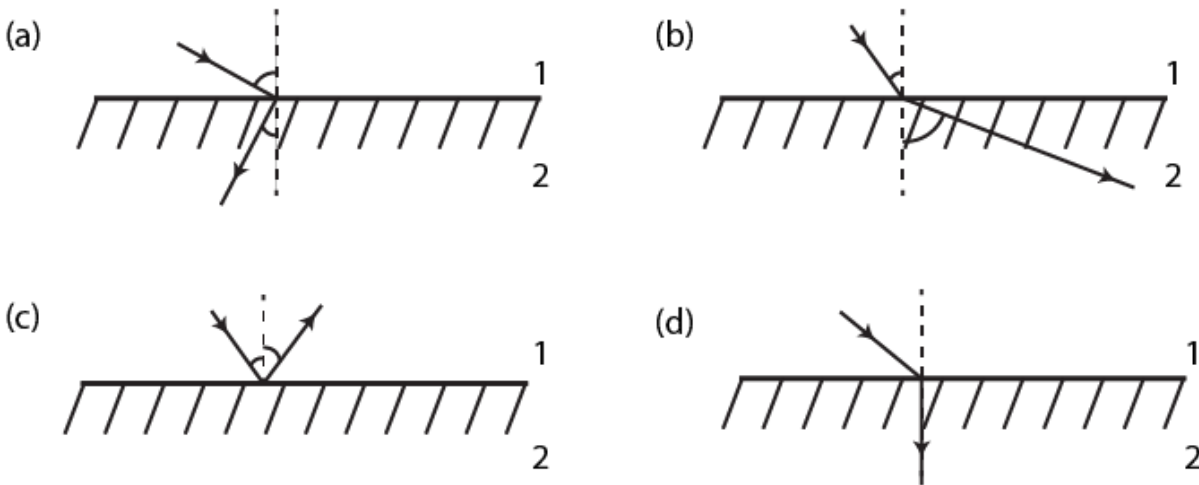
Answer:
(a)

9.12 Consider an extended object immersed in water contained in a plane trough. When seen from close to the edge of the trough the object looks distorted because
(a) the apparent depth of the points close to the edge are nearer the surface of the water compared to the points away from the edge.
(b) the angle subtended by the image of the object at the eye is smaller than the actual angle subtended by the object in air.
(c) some of the points of the object far away from the edge may not be visible because of total internal reflection.
(d) water in a trough acts as a lens and magnifies the object.
Answer:
(a) the apparent depth of the points close to the edge are nearer the surface of the water compared to the points away from the edge.
(b) the angle subtended by the image of the object at the eye is smaller than the actual angle subtended by the object in air.
(c) some of the points of the object far away from the edge may not be visible because of total internal reflection.

9.13 A rectangular block of glass ABCD has a refractive index 1.6. A pin is placed midway on the face AB. When observed from the face AD, the pin shall

A _____ B

D _____ C
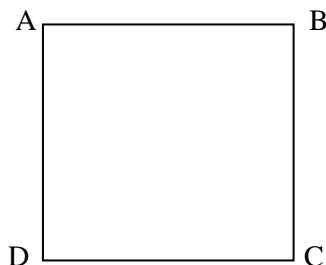
(a) appear to be near A.

(b) appear to be near D.
(c) appear to be at the centre of AD.
(d) not be seen at all.
Answer:
(a) appear to be near A.
(b) appear to be near D.

9.14 Between the primary and secondary rainbows, there is a dark band known as Alexandar's dark band. This is because
(a) light scattered into this region interfere destructively.
(b) there is no light scattered into this region
(c) light is absorbed in this region.
(d) angle made at the eye by the scattered rays with respect to the incident light of the sun lies between approximately 42° and 50°.
Answer:
(d) angle made at the eye by the scattered rays with respect to the incident light of the sun lies between approximately 42° and 50°.

9.15 A magnifying glass is used, as the object to be viewed can be brought closer to the eye than the normal near point. This results in
(a) a larger angle to be subtended by the object at the eye and hence viewed in greater detail.
(b) the formation of a virtual erect image.
(c) increase in the field of view.
(d) infinite magnification at the near point.
Answer:
(a) a larger angle to be subtended by the object at the eye and hence viewed in greater detail.
(b) the formation of a virtual erect image.

9.16 An astronomical refractive telescope has an objective of focal length 20m and an eyepiece of focal length 2cm.
(a) The length of the telescope tube is 20.02m.
(b) The magnification is 1000.
(c) The image formed is inverted.
(d) An objective of a larger aperture will increase the brightness and reduce chromatic aberration of the image.
Answer:
(a) The length of the telescope tube is 20.02m.
(b) The magnification is 1000.
(c) The image formed is inverted.

Very Short Answers

9.17 Will the focal length of a lens for red light be more, same or less than that for blue light?
Answer:
The focal length of a lens for red light will be larger than that for the blue light.

9.18 The near vision of an average person is 25cm. To view an object with an angular magnification of 10, what should be the power of the microscope?
Answer:
D = 25 cm

u = -f
v = -25
m = v/u
f = 0.025 m
p = 1/f = 40 D

9.19 An unsymmetrical double convex thin lens forms the image of a point object on its axis. Will the position of the image change if the lens is reversed?
Answer:
The position of the image will not change if the lens is reversed.

9.20 Three immiscible liquids of densities d1 > d2 > d3 and refractive indices µ1 > µ2 > µ3 are put in a beaker. The height of each liquid column is h/3. A dot is made at the bottom of the beaker. For near normal vision, find the apparent depth of the dot.
Answer:
h1 = -µ2/ µ1 h/3
h2 = - µ3/ µ2(µ2/ µ1 h/3 + h/3) = -h/3 (µ3/ µ2 + µ2/ µ1)
h3(1/ µ1 + 1/ µ2 + 1/ µ3) is the required depth.

9.21 For a glass prism (µ = √3) the angle of minimum deviation is equal to the angle of the prism. Find the angle of the prism.
Answer:
µ = sin[(A + δm)/2]/sin (A/2)
Substituting the values of µ = sin A/sin A/2
µ = sin A/sin A/2 = 2 cos A/2
A = 60°
Therefore, the required angle is 60°

Short Answers

9.22 A short object of length L is placed along the principal axis of a concave mirror away from focus. The object distance is u. If the mirror has a focal length f, what will be the length of the image? You may take L << |v-f|
Answer:
The mirror formula is
1/v + 1/u = 1/f
u is the object distance
v is the image distance
du = |u1 – u2| = L
Differentiating on the both sides we get,
dv/v² = -du/u²
v/u = f/u-f
du = L, therefore, image length is f²/(u-f)²L

9.23 A circular disc of radius 'R' is placed co-axially and horizontally inside an opaque hemispherical bowl of radius 'a'. The far edge of the disc is just visible when viewed from the edge of the bowl. The bowl is filled with transparent liquid of refractive index µ and the near edge of the disc becomes just visible. How far below the top of the bowl is the disc placed?
Answer:
Distance at which the bowl should be placed in the disc is given as:

$d = \mu(a^2 - b^2)/\sqrt{(a + r)^2 - \mu(a - r)^2}$

9.24 A thin convex lens of focal length 25 cm is cut into two pieces 0.5 cm above the principal axis. The top part is placed at (0,0) and an object placed at (–50 cm, 0). Find the coordinates of the image.
Answer:
$1/v = 1/u + 1/f = 1/-50 + 1/25 = 1/50$
$v = 50$ cm
Magnification is $m = v/u = -50/50 = -1$
Therefore, the coordinates of the image are (50 cm, -1 cm)

9.25 In many experimental set-ups the source and screen are fixed at a distance say D and the lens is movable. Show that there are two positions for the lens for which an image is formed on the screen. Find the distance between these points and the ratio of the image sizes for these two points.
Answer:
$u = -x1$
$v = +(D - x1)$
$1/D - x1 - 1/(-x1) = 1/f$
$u = -x2$
$v = +(D - x2)$
$1/D - x2 - 1/(-x2) = 1/f$
$D = x1 + x2$
$d = x2 - x1$
$x1 = D - d/2$
$D - x1 = D + d/2$
$u = D/2 + d/2$
$v = D/2 - d/2$
$m1 = D - d/D + d$
$m2/m1 = (D+d/D-d)^2$

9.26 A jar of height h is filled with a transparent liquid of refractive index μ. At the centre of the jar on the bottom surface is a dot. Find the minimum diameter of a disc, such that when placed on the top surface symmetrically about the centre, the dot is invisible.
Answer:
$\tan i_c$ $d/2/h$
$ic = d/2h$
$d = 2h \tan i_c$
$d = 2h \times 1/\sqrt{\mu^2} - 1$

9.27 A myopic adult has a far point at 0.1 m. His power of accomodation is 4 diopters. (i) What power lenses are required to see distant objects? (ii) What is his near point without glasses? (iii) What is his near point with glasses? (Take the image distance from the lens of the eye to the retina to be 2 cm.)
Answer:
i) Power lenses are required to see distant objects
$1/f = 1/v - 1/u$
$1/f = 1/10$
$f = -10$ cm $= -0.1$ m
$P = 1/f$
$P = 1/(-0.1)$
$P = -10$ diopter

ii) When no corrective lens used
Pn = Pf + Pa
u = -10 cm = -0.1 m
v = 2 cm = 0.02 m
1/f = 1/v – 1/u = 60
Pn = Pf + Pa = 64 D
u = xn
xn = 1/14 m = 100/14 cm = 7 cm

iii) When used corrective lens
u = infinity
v = 2 cm = 0.02 m
1/f = 1/v – 1/u
P = 50
Pn = 50 + 0
Pn = 50 D
u = xnm
xm = ¼ m = 0.25 m

9.28 Show that for a material with refractive index μ ≥ 2 , light incident at any angle shall be guided along a length perpendicular to the incident face.
Answer:
Let the refractive index of the rectangular slab be μ ≥ √2.
μ = 1/sin i_c
sin i_c > 1/ μ
cos r ≥ 1/ μ
sin i/sin r = μ
From Snell's law
Sin I = μ sin r
i = 90°
1 + 1 ≤ μ²
2 ≤ μ²
Taking the square root
√2 ≤ μ

9.29 The mixture a pure liquid and a solution in a long vertical column (i.e, horizontal dimensions << vertical dimensions) produces diffusion of solute particles and hence a refractive index gradient along the vertical dimension. A ray of light entering the column at right angles to the vertical is deviated from its original path. Find the deviation in travelling a horizontal distance d << h, the height of the column.
Answer:
Let the height of the long vertical column with transparent liquid be h and dx be the thickness
The angle at which the ray AB enters is θ
Let y be the new height of the liquid
(θ + d θ) is the emerging angle while (y + dy) is the height.
From Snell's law,
μ(y) sin θ = μ (y + dy) sin (θ + d θ)
After integration we get,
θ = -1/ μ d μ/dy d

9.30 If light passes near a massive object, the gravitational interaction causes a bending of the ray. This can

be thought of as happening due to a change in the effective refrative index of the medium given by $n(r) = 1 + 2GM/rc^2$ where r is the distance of the point of consideration from the centre of the mass of the massive body, G is the universal gravitational constant, M the mass of the body and c the speed of light in vacuum. Considering a spherical object find the deviation of the ray from the original path as it grazes the object.
Answer:
$n(r) = 1 + 2GM/rc^2$

9.31 An infinitely long cylinder of radius R is made of an unusual exotic material with refractive index –1. The cylinder is placed between two planes whose normals are along the y direction. The center of the cylinder O lies along the y-axis. A narrow laser beam is directed along the y direction from the lower plate. The laser source is at a horizontal distance x from the diameter in the y direction. Find the range of x such that light emitted from the lower plane does not reach the upper plane.
Answer:
The refractive index of the cylinder is -1 and is placed in the air of $\mu = 1$
AB is incident at B to the cylinder such that θr will be negative
$\theta 1 = \theta i = \theta r$
Total deviation of the out coming ray is $4\theta 1$.
When the angles are measured clockwise, the planes $\pi/3 \le 4\theta \le 3\pi/2$
If the plane is at $R \pi/r \le x \le 3R \pi/8$, the light emitted from the source shall not reach the plane.

9.32 (i) Consider a thin lens placed between a source (S) and an observer (O). Let the thickness of the lens vary as $2 0 () – \alpha = b\ wb\ w$, where b is the verticle distance from the pole. $w0$ is a constant. Using Fermat's principle i.e. the time of transit for a ray between the source and observer is an extremum, find the condition that all paraxial rays starting from the source will converge at a point O on the axis. Find the focal length.
ii) A gravitational lens may be assumed to have a varying width of the form $w(b) = k1\ ln\ (k2/b) = k1\ ln\ (k2/bmin)$. Show that an observer will see an image of a point object as a ring about the centre of the lens with an angular radius.
$\beta = \sqrt{(n-1)k1}\ u/v\ /\ u + v$
Answer:
i) Time taken by the ray to travel from S to P1 is $= t1 = \sqrt{u^2 + b^2}/c$
Time taken by the ray to travel from P1 to O is $= t2 = v/c\ (1 + \frac{1}{2}\ b^2/v^2)$
Time taken to travel through the lens is $= tl = (n – 1)w(b)/c$
Total time is $= t = 1/c\ (u + v + \frac{1}{2}\ b^2/D + (n – 1)(wo + b^2/a))$
D is the focal length as $1/D = 1/u + 1/v$

ii) Differentiating the expression for time, we get
$\beta = b/v = \sqrt{(n-1)k1u/(u + v)v}$