

$$\Rightarrow x^2 = (3 \times 3 \times 5) \times (3 \times 3 \times 5)$$

$$\Rightarrow x^2 = 45 \times 45$$

$$\Rightarrow x = \sqrt{45 \times 45}$$

$$\Rightarrow x = 45$$

\therefore The number of rows = 45 and the number of plants in each rows = 45.

9. Find the smallest square number that is divisible by each of the numbers 4, 9 and 10.

Solution:

$$\begin{array}{l|l} 2 & 4, 9, 10 \\ \hline & 2, 9, 5 \end{array}$$

L.C.M of 4, 9 and 10 is $(2 \times 2 \times 9 \times 5)$ 180.

$$180 = 2 \times 2 \times 9 \times 5$$

$$= (2 \times 2) \times 3 \times 3 \times 5$$

$$= (2 \times 2) \times (3 \times 3) \times 5$$

Here, 5 cannot be paired.

\therefore we will multiply 180 by 5 to get perfect square.

Hence, the smallest square number divisible by 4, 9 and 10 = $180 \times 5 = 900$

10. Find the smallest square number that is divisible by each of the numbers 8, 15 and 20.

Solution:

$$\begin{array}{l|l} 2 & 8, 15, 20 \\ \hline 2 & 4, 15, 10 \\ \hline 5 & 2, 15, 5 \\ \hline & 2, 3, 1 \end{array}$$

L.C.M of 8, 15 and 20 is $(2 \times 2 \times 5 \times 2 \times 3)$ 120.

$$120 = 2 \times 2 \times 3 \times 5 \times 2$$

$$= (2 \times 2) \times 3 \times 5 \times 2$$

Here, 3, 5 and 2 cannot be paired.

\therefore We will multiply 120 by $(3 \times 5 \times 2)$ 30 to get perfect square.

Hence, the smallest square number divisible by 8, 15 and 20 = $120 \times 30 = 3600$

EXERCISE 6.4

1. Find the square root of each of the following numbers by Division method.

- i. 2304
- ii. 4489
- iii. 3481
- iv. 529
- v. 3249
- vi. 1369
- vii. 5776
- viii. 7921
- ix. 576
- x. 1024
- xi. 3136
- xii. 900

Solution:

i.

	48
4	$\overline{2304}$
+ 4	16
88	704
+8	704
96	0

$\therefore \sqrt{2304} = 48$

ii.

	67
6	$\overline{4489}$
+ 6	36
127	889
+7	889
134	0

$$\therefore \sqrt{4489} = 67$$

iii.

	59
5	3481
+5	25
109	981
+9	981
118	0

$$\therefore \sqrt{3481} = 59$$

iv.

	23
2	529
+2	4
43	129
+3	129
46	0

$$\therefore \sqrt{529} = 23$$

v.

	57
5	3249
+5	25
107	749
+7	749
114	0

$$\therefore \sqrt{3249} = 57$$

vi.

	37	
3	1369	
+3	9	
67	469	
+7	469	
74	0	

$$\therefore \sqrt{1369} = 37$$

vii.

	76	
7	5776	
+7	49	
146	876	
+6	876	
152	0	

$$\therefore \sqrt{5776} = 76$$

viii.

	89	
8	7921	
+8	64	
169	1521	
+9	1521	
178	0	

$$\therefore \sqrt{7921} = 89$$

ix.

$$\begin{array}{r}
 24 \\
 \hline
 2 \quad \overline{) 576} \\
 +2 \quad 4 \\
 \hline
 44 \quad 176 \\
 +4 \quad 176 \\
 \hline
 48 \quad 0
 \end{array}$$

$$\therefore \sqrt{576} = 24$$

x.

$$\begin{array}{r}
 32 \\
 \hline
 3 \quad \overline{) 1024} \\
 +3 \quad 9 \\
 \hline
 62 \quad 124 \\
 +2 \quad 124 \\
 \hline
 64 \quad 0
 \end{array}$$

$$\therefore \sqrt{1024} = 32$$

xi.

$$\begin{array}{r}
 56 \\
 \hline
 5 \quad \overline{) 3136} \\
 +5 \quad 25 \\
 \hline
 106 \quad 636 \\
 +6 \quad 636 \\
 \hline
 112 \quad 0
 \end{array}$$

$$\therefore \sqrt{3136} = 56$$

xii.

$$\begin{array}{r|l} & 30 \\ 3 & \overline{900} \\ +3 & 9 \\ \hline 60 & 00 \end{array}$$

$$\therefore \sqrt{900} = 30$$

2. Find the number of digits in the square root of each of the following numbers (without any calculation).

i. 144

ii. 4489

iii. 27225

iv. 390625

Solution:

i.

$$\begin{array}{r|l} & 12 \\ 1 & \overline{144} \\ +1 & 1 \\ \hline 22 & 44 \\ +2 & 44 \\ \hline 24 & 0 \end{array}$$

$$\therefore \sqrt{144} = 12$$

Hence, the square root of the number 144 has 2 digits.

ii.

	67	
6	44	89
+ 6	36	
127	88	9
+ 7	88	9
134	0	

$\therefore \sqrt{4489} = 67$

Hence, the square root of the number 4489 has 2 digits.

iii.

	165	
1	27	225
+ 1	1	
26	17	2
+ 6	15	6
325	16	25
+ 5	16	25
350	0	

$\sqrt{27225} = 165$

Hence, the square root of the number 27225 has 3 digits.

iv.

	625	
6	39	0625
+ 6	36	
122	30	6
+ 2	24	4
1245	6	225
+ 5	6	225
1250	0	

$$\therefore \sqrt{390625} = 625$$

Hence, the square root of the number 390625 has 3 digits.

3. Find the square root of the following decimal numbers.

i. 2.56

ii. 7.29

iii. 51.84

iv. 42.25

v. 31.36

Solution:

i.

	1.6
1	2.56
+1	1
26	156
+6	156
32	0

$$\therefore \sqrt{2.56} = 1.6$$

ii.

	2.7
2	7.29
+2	4
47	329
+7	329
54	0

$$\therefore \sqrt{7.29} = 2.7$$

iii.

$$\begin{array}{r}
 7.2 \\
 7 \overline{) 51.84} \\
 \underline{+7} \quad 49 \\
 142 \quad 284 \\
 \underline{+2} \quad 284 \\
 144 \quad 0
 \end{array}$$

$$\therefore \sqrt{51.84} = 7.2$$

iv.

$$\begin{array}{r}
 6.5 \\
 6 \overline{) 42.25} \\
 \underline{+6} \quad 36 \\
 125 \quad 625 \\
 \underline{+5} \quad 625 \\
 130 \quad 0
 \end{array}$$

$$\therefore \sqrt{42.25} = 6.5$$

v.

$$\begin{array}{r}
 5.6 \\
 5 \overline{) 31.36} \\
 \underline{+5} \quad 25 \\
 106 \quad 636 \\
 \underline{+6} \quad 636 \\
 112 \quad 0
 \end{array}$$

$$\therefore \sqrt{31.36} = 5.6$$

4. Find the least number which must be subtracted from each of the following numbers so as to get a perfect square. Also find the square root of the perfect square so obtained.

i. 402

ii. 1989

iii. 3250

iv. 825

v. 4000

Solution:

i.

	2	
2	402	
+2	4	
4	02	

$\therefore \sqrt{400} = 20$

\therefore We must subtracted 2 from 402 to get a perfect square.

New number = $402 - 2 = 400$

	20	
2	400	
+2	4	
40	00	

$$\therefore \sqrt{400} = 20$$

ii.

	44	
4	1989	
+4	16	
84	389	
+4	336	
88	53	

\therefore We must subtracted 53 from 1989 to get a perfect square. New number = $1989 - 53 = 1936$

$$\begin{array}{r}
 44 \\
 4 \overline{) 1936} \\
 +4 \quad 16 \\
 \hline
 84 \quad 336 \\
 +4 \quad 336 \\
 \hline
 88 \quad 0
 \end{array}$$

$\therefore \sqrt{1936} = 44$

iii.

$$\begin{array}{r}
 57 \\
 5 \overline{) 3250} \\
 +5 \quad 25 \\
 \hline
 107 \quad 750 \\
 +7 \quad 749 \\
 \hline
 114 \quad 1
 \end{array}$$

\therefore We must subtracted 1 from 3250 to get a perfect square.
 New number = $3250 - 1 = 3249$

$$\begin{array}{r}
 57 \\
 5 \overline{) 3249} \\
 +5 \quad 25 \\
 \hline
 107 \quad 749 \\
 +7 \quad 749 \\
 \hline
 114 \quad 0
 \end{array}$$

$\therefore \sqrt{3249} = 57$

iv.

$$\begin{array}{r|l}
 & 28 \\
 2 & \overline{825} \\
 +2 & 4 \\
 \hline
 48 & 425 \\
 +8 & 384 \\
 \hline
 56 & 41
 \end{array}$$

∴ We must subtracted 41 from 825 to get a perfect square.

New number = $825 - 41 = 784$

$$\begin{array}{r|l}
 & 28 \\
 2 & \overline{784} \\
 +2 & 4 \\
 \hline
 48 & 384 \\
 +8 & 384 \\
 \hline
 56 & 0
 \end{array}$$

∴ $\sqrt{784} = 28$

$$\begin{array}{r|l}
 & 63 \\
 6 & \overline{4000} \\
 +6 & 36 \\
 \hline
 123 & 400 \\
 +3 & 369 \\
 \hline
 126 & 31
 \end{array}$$

∴ We must subtracted 31 from 4000 to get a perfect square. New number = $4000 - 31 = 3969$

∴ $\sqrt{3969} = 63$

5. Find the least number which must be added to each of the following numbers so as to get a perfect square. Also find the square root of the perfect square so obtained.

- (i) 525
- (ii) 1750
- (iii) 252
- (iv) 1825
- (v) 6412

Solution:

(i)

	22
2	525
+2	4
42	125
+2	84
44	41

	23
2	525
+2	4
43	125
+3	129

Here, $(22)^2 < 525 > (23)^2$

We can say 525 is $(129 - 125) 4$ less than $(23)^2$.

\therefore If we add 4 to 525, it will be perfect square. New number = $525 + 4 = 529$

$$\begin{array}{r|l}
 & 23 \\
 2 & 529 \\
 +2 & 4 \\
 \hline
 43 & 129 \\
 +3 & 129 \\
 \hline
 46 & 0
 \end{array}$$

$\therefore \sqrt{529} = 23$

(ii)

$$\begin{array}{r|l}
 & 41 \\
 4 & 1750 \\
 +4 & 16 \\
 \hline
 81 & 150 \\
 +1 & 81 \\
 \hline
 82 & 69
 \end{array}$$

$$\begin{array}{r|l}
 & 42 \\
 4 & 1750 \\
 4 & 16 \\
 \hline
 82 & 150 \\
 +2 & 164
 \end{array}$$

Here, $(41)^2 < 1750 < (42)^2$

We can say 1750 is (164 - 150) 14 less than $(42)^2$.

\therefore If we add 14 to 1750, it will be perfect square.

New number = $1750 + 14 = 1764$

$$\begin{array}{r}
 42 \\
 4 \overline{) 1764} \\
 \underline{4 \quad 16} \\
 82 \quad 164 \\
 \underline{+2 \quad 164} \\
 \hline
 \end{array}$$

$\therefore \sqrt{1764} = 42$

(iii)

$$\begin{array}{r}
 15 \\
 1 \overline{) 252} \\
 \underline{+1 \quad 1} \\
 25 \quad 152 \\
 \underline{+5 \quad 125} \\
 30 \quad 27
 \end{array}$$

$$\begin{array}{r}
 16 \\
 1 \overline{) 252} \\
 \underline{+1 \quad 1} \\
 26 \quad 152 \\
 \underline{+6 \quad 156} \\
 \hline
 \end{array}$$

Here, $(15)^2 < 252 > (16)^2$

We can say 252 is $(156 - 152)$ 4 less than $(16)^2$.

\therefore If we add 4 to 252, it will be perfect square.

New number = $252 + 4 = 256$

	16	
1	256	
+1	1	
26	156	
+6	156	
32	0	

$\therefore \sqrt{256} = 16$

(iv)

	42	
4	1825	
+4	16	
82	225	
+2	162	
84	63	

	43	
4	1825	
+4	16	
83	225	
+3	249	

Here, $(42)^2 < 1825 > (43)^2$

We can say 1825 is $(249 - 225) 24$ less than $(43)^2$.

\therefore If we add 24 to 1825, it will be perfect square.

New number = $1825 + 24 = 1849$

$$\begin{array}{r}
 43 \\
 \hline
 4 \quad \overline{1849} \\
 +4 \quad 16 \\
 \hline
 83 \quad 249 \\
 +3 \quad 249 \\
 \hline
 86 \quad 0
 \end{array}$$

$\therefore \sqrt{1849} = 43$

(v)

$$\begin{array}{r}
 80 \\
 \hline
 8 \quad \overline{6412} \\
 +8 \quad 64 \\
 \hline
 160 \quad 120 \\
 0 \quad 0
 \end{array}$$

$$\begin{array}{r}
 81 \\
 \hline
 8 \quad \overline{6412} \\
 +8 \quad 64 \\
 \hline
 161 \quad 12 \\
 +1 \quad 161
 \end{array}$$

Here, $(80)^2 < 6412 > (81)^2$

We can say 6412 is $(161 - 12)$ 149 less than $(81)^2$.

\therefore If we add 149 to 6412, it will be perfect square.

New number = $6412 + 149 = 656$

$$\begin{array}{r}
 81 \\
 8 \overline{) 6561} \\
 +8 \quad 64 \\
 \hline
 161 \quad 161 \\
 +1 \quad 161 \\
 \hline
 162 \quad 0
 \end{array}$$

$\therefore \sqrt{6561} = 81$

6. Find the length of the side of a square whose area is 441 m².

Solution:

Let the length of each side of the field = a Then, area of the field = 441 m²

$\Rightarrow a^2 = 441 \text{ m}^2$

$\Rightarrow a = \sqrt{441} \text{ m}$

$$\begin{array}{r}
 21 \\
 2 \overline{) 441} \\
 +2 \quad 4 \\
 \hline
 41 \quad 41 \\
 +1 \quad 41 \\
 \hline
 42 \quad 0
 \end{array}$$

\therefore The length of each side of the field = a m = 21 m.

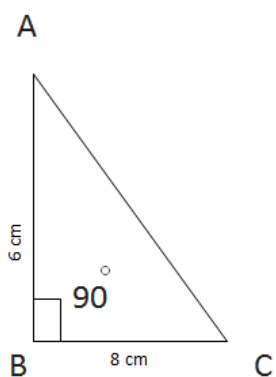
7. In a right triangle ABC, $\angle B = 90^\circ$.

a. If AB = 6 cm, BC = 8 cm, find AC

b. If AC = 13 cm, BC = 5 cm, find AB

Solution:

a.



Given, $AB = 6 \text{ cm}$, $BC = 8 \text{ cm}$

Let AC be $x \text{ cm}$.

$$\therefore AC^2 = AB^2 + BC^2$$

$$AC = \sqrt{AB^2 + BC^2}$$

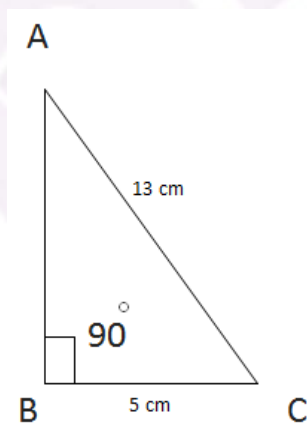
$$= \sqrt{6^2 + 8^2}$$

$$= \sqrt{36 + 64}$$

$$= \sqrt{100} = 10$$

Hence, $AC = 10 \text{ cm}$.

b.



Given, $AC = 13 \text{ cm}$, $BC = 5 \text{ cm}$

Let AB be $x \text{ cm}$.

$$\therefore AC^2 = AB^2 + BC^2$$

$$\Rightarrow AC^2 - BC^2 = AB^2$$

$$\begin{aligned}
 AB &= \sqrt{AC^2 - BC^2} \\
 &= \sqrt{13^2 - 5^2} \\
 &= \sqrt{169 - 25} \\
 &= \sqrt{144} = 12
 \end{aligned}$$

Hence, $AB = 12$ cm

8. A gardener has 1000 plants. He wants to plant these in such a way that the number of rows and the number of columns remain same. Find the minimum number of plants he needs more for this.

Solution:

Let the number of rows and column be, x .

\therefore Total number of row and column = $x \times x = x^2$ As per question, $x^2 = 1000$

$\Rightarrow x = \sqrt{1000}$

$$\begin{array}{r|l}
 & 31 \\
 3 & \overline{1000} \\
 +3 & 9 \\
 \hline
 61 & 100 \\
 +1 & 61 \\
 \hline
 &
 \end{array}$$

$$\begin{array}{r|l}
 & 32 \\
 3 & \overline{1000} \\
 +3 & 9 \\
 \hline
 62 & 100 \\
 +2 & 124 \\
 \hline
 &
 \end{array}$$

Here, $(31)^2 < 1000 < (32)^2$

We can say 1000 is $(124 - 100) 24$ less than $(32)^2$.

\therefore 24 more plants are needed.

9. There are 500 children in a school. For a P.T. drill they have to stand in such a manner that the number of rows is equal to number of columns. How many children would be left out in this arrangement.

Solution:

Let the number of rows and column be, x .

\therefore Total number of row and column = $x \times x = x^2$ As per question, $x^2 = 500$

$x = \sqrt{500}$

$$\begin{array}{r|l} & 22 \\ 2 & \overline{500} \\ +2 & 4 \\ \hline 42 & 100 \\ +2 & 84 \\ \hline 44 & 16 \end{array}$$

Hence, 16 children would be left out in the arrangement

