

RD Sharma Solutions for Class 7 Maths Chapter 15 Properties of Triangles

EXERCISE 15.4

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1. In each of the following, there are three positive numbers. State if these numbers could possibly be the lengths of the sides of a triangle:

(i) 5, 7, 9
(ii) 2, 10, 15
(iii) 3, 4, 5
(iv) 2, 5, 7
(v) 5, 8, 20

Solution:

(i) Given 5, 7, 9

Yes, these numbers can be the lengths of the sides of a triangle because the sum of any two sides of a triangle is always greater than the third side.

Here, 5 + 7 > 9, 5 + 9 > 7, 9 + 7 > 5

(ii) Given 2, 10, 15

No, these numbers cannot be the lengths of the sides of a triangle because the sum of any two sides of a triangle is always greater than the third side, which is not true in this case.

Here, 2 + 10 < 15

(iii) Given 3, 4, 5

Yes, these numbers can be the lengths of the sides of a triangle because the sum of any two sides of triangle is always greater than the third side.

Here, 3 + 4 > 5, 3 + 5 > 4, 4 + 5 > 3

(iv) Given 2, 5, 7

No, these numbers cannot be the lengths of the sides of a triangle because the sum of any two sides of a triangle is always greater than the third side, which is not true in this case.

Here, 2 + 5 = 7

(v) Given 5, 8, 20

No, these numbers cannot be the lengths of the sides of a triangle because the sum of any two sides of a triangle is always greater than the third side, which is not true in this case.

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Here, 5 + 8 < 20

2. In Fig. 46, P is the point on the side BC. Complete each of the following statements using symbol '=',' > 'or '< 'so as to make it true:

(i) AP... AB+ BP

(ii) AP... AC + PC

(iii) AP.... ½ (AB + AC + BC)



Solution:

(i) In $\triangle APB$, AP < AB + BP because the sum of any two sides of a triangle is greater than the third side.

(ii) In \triangle APC, AP < AC + PC because the sum of any two sides of a triangle is greater than the third side.

(iii) $AP < \frac{1}{2} (AB + AC + BC)$ In $\triangle ABP$ and $\triangle ACP$, we can write as AP < AB + BP... (i) (Because the sum of any two sides of a triangle is greater than the third side) AP < AC + PC ... (ii) (Because the sum of any two sides of a triangle is greater than the third side) On adding (i) and (ii), we have: AP + AP < AB + BP + AC + PC2AP < AB + AC + BC (BC = BP + PC) $AP < \frac{1}{2} (AB + AC + BC)$

3. P is a point in the interior of △ABC as shown in Fig. 47. State which of the following statements are true (T) or false (F):
(i) AP + PB < AB
(ii) AP + PC > AC

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Solution:

(i) False

Explanation:

We know that the sum of any two sides of a triangle is greater than the third side, it is not true for the given triangle.

(ii) True

Explanation:

We know that the sum of any two sides of a triangle is greater than the third side, it is true for the given triangle.

(iii) False

Explanation:

We know that the sum of any two sides of a triangle is greater than the third side, it is not true for the given triangle.

4. O is a point in the exterior of \triangle ABC. What symbol '>','<' or '=' will you see to complete the statement OA+OB....AB? Write two other similar statements and show that OA + OB + OC > $\frac{1}{2}$ (AB + BC +CA)

Solution:

We know that the sum of any two sides of a triangle is always greater than the third side, in $\triangle OAB$, we have,

 $OA + OB > AB \dots$ (i) In $\triangle OBC$ we have

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OB + OC > BC (ii) In \triangle OCA we have OA + OC > CA (iii) On adding equations (i), (ii) and (iii) we get: OA + OB + OB + OC + OA + OC > AB + BC + CA 2(OA + OB + OC) > AB + BC + CA OA + OB + OC > (AB + BC + CA)/2 Or OA + OB + OC > $\frac{1}{2}$ (AB + BC + CA) Hence the proof.

5. In $\triangle ABC$, $\angle A = 100^{\circ}$, $\angle B = 30^{\circ}$, $\angle C = 50^{\circ}$. Name the smallest and the largest sides of the triangle.

Solution:

We know that the smallest side is always opposite to the smallest angle, which in this case is 30°, it is AC.

Also, because the largest side is always opposite to the largest angle, which in this case is 100°, it is BC.