

EXERCISE 8.1

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1. Write the degree of each of the following polynomials:

(i) $2x^3 + 5x^2 - 7$

(ii) $5x^2 - 3x + 2$

(iii) $2x + x^2 - 8$

(iv) $1/2y^7 - 12y^6 + 48y^5 - 10$

(v) $3x^3 + 1$

(vi) 5

(vii) $20x^3 + 12x^2y^2 - 10y^2 + 20$

Solution:

(i) $2x^3 + 5x^2 - 7$

We know that in a polynomial, degree is the highest power of the variable.
The degree of the polynomial, $2x^3 + 5x^2 - 7$ is 3.

(ii) $5x^2 - 3x + 2$

The degree of the polynomial, $5x^2 - 3x + 2$ is 2.

(iii) $2x + x^2 - 8$

The degree of the polynomial, $2x + x^2 - 8$ is 2.

(iv) $1/2y^7 - 12y^6 + 48y^5 - 10$

The degree of the polynomial, $1/2y^7 - 12y^6 + 48y^5 - 10$ is 7.

(v) $3x^3 + 1$

The degree of the polynomial, $3x^3 + 1$ is 3

(vi) 5

The degree of the polynomial, 5 is 0 (since 5 is a constant number).

(vii) $20x^3 + 12x^2y^2 - 10y^2 + 20$

The degree of the polynomial, $20x^3 + 12x^2y^2 - 10y^2 + 20$ is 4.

2. Which of the following expressions are not polynomials?

(i) $x^2 + 2x^{-2}$

(ii) $\sqrt{ax} + x^2 - x^3$

(iii) $3y^3 - \sqrt{5y} + 9$

(iv) $ax^{1/2} + ax + 9x^2 + 4$

(v) $3x^{-3} + 2x^{-1} + 4x + 5$

Solution:

(i) $x^2 + 2x^{-2}$

The given expression is not a polynomial.

Because a polynomial does not contain any negative powers or fractions.

(ii) $\sqrt{(ax)} + x^2 - x^3$

The given expression is a polynomial.

Because the polynomial has positive powers.

(iii) $3y^3 - \sqrt{5}y + 9$

The given expression is a polynomial.

Because the polynomial has positive powers.

(iv) $ax^{1/2} + ax + 9x^2 + 4$

The given expression is not a polynomial.

Because a polynomial does not contain any negative powers or fractions.

(v) $3x^{-3} + 2x^{-1} + 4x + 5$

The given expression is not a polynomial.

Because a polynomial does not contain any negative powers or fractions.

3. Write each of the following polynomials in the standard form. Also, write their degree:

(i) $x^2 + 3 + 6x + 5x^4$

(ii) $a^2 + 4 + 5a^6$

(iii) $(x^3 - 1)(x^3 - 4)$

(iv) $(y^3 - 2)(y^3 + 11)$

(v) $(a^3 - 3/8)(a^3 + 16/17)$

(vi) $(a + 3/4)(a + 4/3)$

Solution:

(i) $x^2 + 3 + 6x + 5x^4$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$3 + 6x + x^2 + 5x^4 \text{ or } 5x^4 + x^2 + 6x + 3$$

The degree of the given polynomial is 4.

(ii) $a^2 + 4 + 5a^6$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$4 + a^2 + 5a^6 \text{ or } 5a^6 + a^2 + 4$$

The degree of the given polynomial is 6.

$$\text{(iii)} (x^3 - 1)(x^3 - 4)$$

$$x^6 - 4x^3 - x^3 + 4$$

$$x^6 - 5x^3 + 4$$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$x^6 - 5x^3 + 4 \text{ or } 4 - 5x^3 + x^6$$

The degree of the given polynomial is 6.

$$\text{(iv)} (y^3 - 2)(y^3 + 11)$$

$$y^6 + 11y^3 - 2y^3 - 22$$

$$y^6 + 9y^3 - 22$$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$y^6 + 9y^3 - 22 \text{ or } -22 + 9y^3 + y^6$$

The degree of the given polynomial is 6.

$$\text{(v)} (a^3 - 3/8)(a^3 + 16/17)$$

$$a^6 + 16a^3/17 - 3a^3/8 - 6/17$$

$$a^6 + 77/136a^3 - 48/136$$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$a^6 + 77/136a^3 - 48/136 \text{ or } -48/136 + 77/136a^3 + a^6$$

The degree of the given polynomial is 6.

$$\text{(vi)} (a + 3/4)(a + 4/3)$$

$$a^2 + 4a/3 + 3a/4 + 1$$

$$a^2 + 25a/12 + 1$$

The standard form of the polynomial is written in either increasing or decreasing order of their powers.

$$a^2 + 25a/12 + 1 \text{ or } 1 + 25a/12 + a^2$$

The degree of the given polynomial is 2.

EXERCISE 8.2

PAGE NO: 8.4

Divide:

1. $6x^3y^2z^2$ by $3x^2yz$

Solution:

We have,

$$6x^3y^2z^2 / 3x^2yz$$

By using the formula $a^n / a^m = a^{n-m}$

$$6/3 x^{3-2} y^{2-1} z^{2-1}$$

$$2xyz$$

2. $15m^2n^3$ by $5m^2n^2$

Solution:

We have,

$$15m^2n^3 / 5m^2n^2$$

By using the formula $a^n / a^m = a^{n-m}$

$$15/5 m^{2-2} n^{3-2}$$

$$3n$$

3. $24a^3b^3$ by $-8ab$

Solution:

We have,

$$24a^3b^3 / -8ab$$

By using the formula $a^n / a^m = a^{n-m}$

$$24/-8 a^{3-1} b^{3-1}$$

$$-3a^2b^2$$

4. $-21abc^2$ by $7abc$

Solution:

We have,

$$-21abc^2 / 7abc$$

By using the formula $a^n / a^m = a^{n-m}$

$$-21/7 a^{1-1} b^{1-1} c^{2-1}$$

$$-3c$$

5. $72xyz^2$ by $-9xz$

Solution:

We have,

$$72xyz^2 / -9xz$$

By using the formula $a^n / a^m = a^{n-m}$
 $72/-9 x^{1-1} y z^{2-1}$
 $-8yz$

6. $-72a^4b^5c^8$ by $-9a^2b^2c^3$

Solution:

We have,

$$-72a^4b^5c^8 / -9a^2b^2c^3$$

By using the formula $a^n / a^m = a^{n-m}$

$$-72/-9 a^{4-2} b^{5-2} c^{8-3}$$

$$8a^2b^3c^5$$

Simplify:

7. $16m^3y^2 / 4m^2y$

Solution:

We have,

$$16m^3y^2 / 4m^2y$$

By using the formula $a^n / a^m = a^{n-m}$

$$16/4 m^{3-2} y^{2-1}$$

$$4my$$

8. $32m^2n^3p^2 / 4mnp$

Solution:

We have,

$$32m^2n^3p^2 / 4mnp$$

By using the formula $a^n / a^m = a^{n-m}$

$$32/4 m^{2-1} n^{3-1} p^{2-1}$$

$$8m^2np$$

EXERCISE 8.3
PAGE NO: 8.6
Divide:

1. $x + 2x^2 + 3x^4 - x^5$ by $2x$

Solution:

We have,

$$(x + 2x^2 + 3x^4 - x^5) / 2x$$

$$x/2x + 2x^2/2x + 3x^4/2x - x^5/2x$$

 By using the formula $a^n / a^m = a^{n-m}$

$$1/2 x^{1-1} + x^{2-1} + 3/2 x^{4-1} - 1/2 x^{5-1}$$

$$1/2 + x + 3/2 x^3 - 1/2 x^4$$

2. $y^4 - 3y^3 + 1/2y^2$ by $3y$

Solution:

We have,

$$(y^4 - 3y^3 + 1/2y^2) / 3y$$

$$y^4/3y - 3y^3/3y + (1/2)y^2/3y$$

 By using the formula $a^n / a^m = a^{n-m}$

$$1/3 y^{4-1} - y^{3-1} + 1/6 y^{2-1}$$

$$1/3y^3 - y^2 + 1/6y$$

3. $-4a^3 + 4a^2 + a$ by $2a$

Solution:

We have,

$$(-4a^3 + 4a^2 + a) / 2a$$

$$-4a^3/2a + 4a^2/2a + a/2a$$

 By using the formula $a^n / a^m = a^{n-m}$

$$-2a^{3-1} + 2a^{2-1} + 1/2 a^{1-1}$$

$$-2a^2 + 2a + 1/2$$

4. $-x^6 + 2x^4 + 4x^3 + 2x^2$ by $\sqrt{2x^2}$

Solution:

We have,

$$(-x^6 + 2x^4 + 4x^3 + 2x^2) / \sqrt{2x^2}$$

$$-x^6/\sqrt{2x^2} + 2x^4/\sqrt{2x^2} + 4x^3/\sqrt{2x^2} + 2x^2/\sqrt{2x^2}$$

 By using the formula $a^n / a^m = a^{n-m}$

$$-1/\sqrt{2} x^{6-2} + 2/\sqrt{2} x^{4-2} + 4/\sqrt{2} x^{3-2} + 2/\sqrt{2} x^{2-2}$$

$$-1/\sqrt{2} x^4 + \sqrt{2x^2} + 2\sqrt{2x} + \sqrt{2}$$

5. $-4a^3 + 4a^2 + a$ by $2a$

Solution:

We have,

$$(-4a^3 + 4a^2 + a) / 2a$$

$$-4a^3/2a + 4a^2/2a + a/2a$$

By using the formula $a^n / a^m = a^{n-m}$

$$-2a^{3-1} + 2a^{2-1} + 1/2a^{1-1}$$

$$-2a^2 + 2a + 1/2$$

6. $\sqrt{3}a^4 + 2\sqrt{3}a^3 + 3a^2 - 6a$ by $3a$

Solution:

We have,

$$(\sqrt{3}a^4 + 2\sqrt{3}a^3 + 3a^2 - 6a) / 3a$$

$$\sqrt{3}a^4/3a + 2\sqrt{3}a^3/3a + 3a^2/3a - 6a/3a$$

By using the formula $a^n / a^m = a^{n-m}$

$$\sqrt{3}/3 a^{4-1} + 2\sqrt{3}/3 a^{3-1} + a^{2-1} - 2a^{1-1}$$

$$1/\sqrt{3} a^3 + 2/\sqrt{3} a^2 + a - 2$$

EXERCISE 8.4

PAGE NO: 8.11

Divide:

1. $5x^3 - 15x^2 + 25x$ by $5x$

Solution:

We have,

$$(5x^3 - 15x^2 + 25x) / 5x$$

$$5x^3/5x - 15x^2/5x + 25x/5x$$

By using the formula $a^n / a^m = a^{n-m}$

$$5/5 x^{3-1} - 15/5 x^{2-1} + 25/5 x^{1-1}$$

$$x^2 - 3x + 5$$

2. $4z^3 + 6z^2 - z$ by $-1/2z$

Solution:

We have,

$$(4z^3 + 6z^2 - z) / -1/2z$$

$$4z^3/(-1/2z) + 6z^2/(-1/2z) - z/(-1/2z)$$

By using the formula $a^n / a^m = a^{n-m}$

$$-8 z^{3-1} - 12z^{2-1} + 2 z^{1-1}$$

$$-8z^2 - 12z + 2$$

3. $9x^2y - 6xy + 12xy^2$ by $-3/2xy$

Solution:

We have,

$$(9x^2y - 6xy + 12xy^2) / -3/2xy$$

$$9x^2y/(-3/2xy) - 6xy/(-3/2xy) + 12xy^2/(-3/2xy)$$

By using the formula $a^n / a^m = a^{n-m}$

$$(-9 \times 2)/3 x^{2-1}y^{1-1} - (-6 \times 2)/3 x^{1-1}y^{1-1} + (-12 \times 2)/3 x^{1-1}y^{2-1}$$

$$-6x + 4 - 8y$$

4. $3x^3y^2 + 2x^2y + 15xy$ by $3xy$

Solution:

We have,

$$(3x^3y^2 + 2x^2y + 15xy) / 3xy$$

$$3x^3y^2/3xy + 2x^2y/3xy + 15xy/3xy$$

By using the formula $a^n / a^m = a^{n-m}$

$$3/3 x^{3-1}y^{2-1} + 2/3 x^{2-1}y^{1-1} + 15/3 x^{1-1}y^{1-1}$$

$$x^2y + 2/3x + 5$$

5. $x^2 + 7x + 12$ by $x + 4$

Solution:

We have,

$$(x^2 + 7x + 12) / (x + 4)$$

By using long division method

$$\begin{array}{r}
 x + 4 \overline{) x^2 + 7x + 12} \\
 \underline{-} \\
 x^2 + 4x \\
 \underline{-} \\
 3x + 12 \\
 \underline{-} \\
 3x + 12 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (x^2 + 7x + 12) / (x + 4) = x + 3$$

6. $4y^2 + 3y + 1/2$ by $2y + 1$

Solution:

We have,

$$4y^2 + 3y + 1/2 \text{ by } (2y + 1)$$

By using long division method

$$\begin{array}{r}
 2y + 1 \overline{) 4y^2 + 3y + \frac{1}{2}} \\
 \underline{-} \\
 4y^2 + 2y \\
 \underline{-} \\
 y + \frac{1}{2} \\
 \underline{-} \\
 y + \frac{1}{2} \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (4y^2 + 3y + 1/2) / (2y + 1) = 2y + 1/2$$

7. $3x^3 + 4x^2 + 5x + 18$ by $x + 2$

Solution:

We have,

$$(3x^3 + 4x^2 + 5x + 18) / (x + 2)$$

By using long division method

$$\begin{array}{r}
 3x^2 \quad -2x \quad +9 \\
 x + 2 \overline{) 3x^3 \quad +4x^2 \quad +5x \quad +18} \\
 \underline{-} \\
 3x^3 \quad +6x^2 \\
 \underline{-} \\
 -2x^2 \quad +5x \quad +18 \\
 \underline{-} \\
 -2x^2 \quad -4x \\
 \underline{-} \\
 9x \quad +18 \\
 \underline{-} \\
 9x \quad +18 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (3x^3 + 4x^2 + 5x + 18) / (x + 2) = 3x^2 - 2x + 9$$

8. $14x^2 - 53x + 45$ by $7x - 9$

Solution:

We have,

$$(14x^2 - 53x + 45) / (7x - 9)$$

By using long division method

$$\begin{array}{r}
 2x \quad -5 \\
 7x - 9 \overline{) 14x^2 \quad -53x \quad +45} \\
 \underline{-} \\
 14x^2 \quad -18x \\
 \underline{-} \\
 -35x \quad +45 \\
 \underline{-} \\
 -35x \quad +45 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (14x^2 - 53x + 45) / (7x - 9) = 2x - 5$$

9. $-21 + 71x - 31x^2 - 24x^3$ by $3 - 8x$

Solution:

We have,

$$-21 + 71x - 31x^2 - 24x^3 \text{ by } 3 - 8x$$

$$(-24x^3 - 31x^2 + 71x - 21) / (3 - 8x)$$

By using long division method

$$\begin{array}{r}
 3x^2 + 5x - 7 \\
 -8x + 3 \overline{) -24x^3 - 31x^2 + 71x - 21} \\
 \underline{-} \\
 -24x^3 + 9x^2 \\
 \underline{-} \\
 -40x^2 + 71x - 21 \\
 \underline{-} \\
 -40x^2 + 15x \\
 \underline{-} \\
 56x - 21 \\
 \underline{-} \\
 56x - 21 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (-24x^3 - 31x^2 + 71x - 21) / (3 - 8x) = 3x^2 + 5x - 7$$

10. $3y^4 - 3y^3 - 4y^2 - 4y$ by $y^2 - 2y$

Solution:

We have,

$$(3y^4 - 3y^3 - 4y^2 - 4y) / (y^2 - 2y)$$

By using long division method

$$\begin{array}{r}
 3y^2 + 3y + 2 \\
 y^2 - 2y \overline{) 3y^4 - 3y^3 - 4y^2 - 4y + 0} \\
 \underline{-} \\
 3y^4 - 6y^3 \\
 \underline{-} \\
 3y^3 - 4y^2 - 4y + 0 \\
 \underline{-} \\
 3y^3 - 6y^2 \\
 \underline{-} \\
 2y^2 - 4y + 0 \\
 \underline{-} \\
 2y^2 - 4y \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (3y^4 - 3y^3 - 4y^2 - 4y) / (y^2 - 2y) = 3y^2 + 3y + 2$$

11. $2y^5 + 10y^4 + 6y^3 + y^2 + 5y + 3$ by $2y^3 + 1$

Solution:

We have,

$$(2y^5 + 10y^4 + 6y^3 + y^2 + 5y + 3) / (2y^3 + 1)$$

By using long division method

$$\begin{array}{r}
 y^2 + 5y + 3 \\
 2y^3 + 1 \overline{) 2y^5 + 10y^4 + 6y^3 + y^2 + 5y + 3} \\
 \underline{-} \\
 2y^5 + 0y^4 + 0y^3 + y^2 \\
 \underline{-} \\
 10y^4 + 6y^3 + 0y^2 + 5y + 3 \\
 \underline{-} \\
 10y^4 + 0y^3 + 0y^2 + 5y \\
 \underline{-} \\
 6y^3 + 0y^2 + 0y + 3 \\
 \underline{-} \\
 6y^3 + 0y^2 + 0y + 3 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (2y^5 + 10y^4 + 6y^3 + y^2 + 5y + 3) / (2y^3 + 1) = y^2 + 5y + 3$$

12. $x^4 - 2x^3 + 2x^2 + x + 4$ by $x^2 + x + 1$

Solution:

We have,

$$(x^4 - 2x^3 + 2x^2 + x + 4) / (x^2 + x + 1)$$

By using long division method

$$\begin{array}{r}
 x^2 - 3x + 4 \\
 x^2 + x + 1 \overline{) x^4 - 2x^3 + 2x^2 + x + 4} \\
 \underline{-} \\
 x^4 + x^3 + x^2 \\
 \underline{-} \\
 -3x^3 + x^2 + x + 4 \\
 \underline{-} \\
 -3x^3 - 3x^2 - 3x \\
 \underline{-} \\
 4x^2 + 4x + 4 \\
 \underline{-} \\
 4x^2 + 4x + 4 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (x^4 - 2x^3 + 2x^2 + x + 4) / (x^2 + x + 1) = x^2 - 3x + 4$$

13. $m^3 - 14m^2 + 37m - 26$ by $m^2 - 12m + 13$

Solution:

We have,

$$(m^3 - 14m^2 + 37m - 26) / (m^2 - 12m + 13)$$

By using long division method

$$\begin{array}{r}
 m^2 - 12m + 13 \quad \overline{) m^3 - 14m^2 + 37m - 26} \\
 \underline{-} \\
 m^3 - 12m^2 + 13m \\
 \underline{-} \\
 -2m^2 + 24m - 26 \\
 \underline{-} \\
 -2m^2 + 24m - 26 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (m^3 - 14m^2 + 37m - 26) / (m^2 - 12m + 13) = m - 2$$

14. $x^4 + x^2 + 1$ by $x^2 + x + 1$

Solution:

We have,

$$(x^4 + x^2 + 1) / (x^2 + x + 1)$$

By using long division method

$$\begin{array}{r}
 x^2 - x + 1 \\
 x^2 + x + 1 \quad \overline{) x^4 + 0x^3 + x^2 + 0x + 1} \\
 \underline{-} \\
 x^4 + x^3 + x^2 \\
 \underline{-} \\
 -x^3 + 0x^2 + 0x + 1 \\
 \underline{-} \\
 -x^3 - x^2 - x \\
 \underline{-} \\
 x^2 + x + 1 \\
 \underline{-} \\
 x^2 + x + 1 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (x^4 + x^2 + 1) / (x^2 + x + 1) = x^2 - x + 1$$

15. $x^5 + x^4 + x^3 + x^2 + x + 1$ by $x^3 + 1$

Solution:

We have,

$$(x^5 + x^4 + x^3 + x^2 + x + 1) / (x^3 + 1)$$

By using long division method

$$\begin{array}{r}
 x^2 + x + 1 \\
 x^3 + 1 \overline{) x^5 + x^4 + x^3 + x^2 + x + 1} \\
 \underline{-} \\
 x^5 + 0x^4 + 0x^3 + x^2 \\
 \underline{-} \\
 + x^3 + 0x^2 + x + 1 \\
 \underline{-} \\
 x^4 + 0x^3 + 0x^2 + x \\
 \underline{-} \\
 + 0x^3 + 0x^2 + 0x + 1 \\
 \underline{-} \\
 + 0x^2 + 0x + 1 \\
 \underline{-} \\
 + 0x + 1 \\
 \underline{-} \\
 + 1 \\
 \underline{-} \\
 0
 \end{array}$$

$$\therefore (x^5 + x^4 + x^3 + x^2 + x + 1) / (x^3 + 1) = x^2 + x + 1$$

Divide each of the following and find the quotient and remainder:

16. $14x^3 - 5x^2 + 9x - 1$ by $2x - 1$

Solution:

We have,

$$(14x^3 - 5x^2 + 9x - 1) / (2x - 1)$$

By using long division method

$$\begin{array}{r}
 7x^2 + x + 5 \\
 2x - 1 \overline{) 14x^3 - 5x^2 + 9x - 1} \\
 \underline{-} \\
 14x^3 - 7x^2 \\
 \underline{-} \\
 2x^2 + 9x - 1 \\
 \underline{-} \\
 - x \\
 \underline{-} \\
 10x - 1 \\
 \underline{-} \\
 - 5 \\
 \underline{-} \\
 4
 \end{array}$$

\therefore Quotient is $7x^2 + x + 5$ and the Remainder is 4.

17. $6x^3 - x^2 - 10x - 3$ by $2x - 3$

Solution:

We have,

$$(6x^3 - x^2 - 10x - 3) / (2x - 3)$$

By using long division method

$$\begin{array}{r}
 3x^2 + 4x + 1 \\
 2x - 3 \overline{) 6x^3 - x^2 - 10x - 3} \\
 \underline{6x^3 - 9x^2} \\
 8x^2 - 10x - 3 \\
 \underline{8x^2 - 12x} \\
 2x - 3 \\
 \underline{2x - 3} \\
 0
 \end{array}$$

 \therefore Quotient is $3x^2 + 4x + 1$ and the Remainder is 0.

18. $6x^3 + 11x^2 - 39x - 65$ by $3x^2 + 13x + 13$

Solution:

We have,

$$(6x^3 + 11x^2 - 39x - 65) / (3x^2 + 13x + 13)$$

By using long division method

$$\begin{array}{r}
 2x - 5 \\
 3x^2 + 13x + 13 \overline{) 6x^3 + 11x^2 - 39x - 65} \\
 \underline{6x^3 + 26x^2 + 26x} \\
 -15x^2 - 65x - 65 \\
 \underline{-15x^2 - 65x - 65} \\
 0
 \end{array}$$

 \therefore Quotient is $2x - 5$ and the Remainder is 0.

19. $30x^4 + 11x^3 - 82x^2 - 12x + 48$ by $3x^2 + 2x - 4$

Solution:

We have,

$$(30x^4 + 11x^3 - 82x^2 - 12x + 48) / (3x^2 + 2x - 4)$$

By using long division method

$$\begin{array}{r}
 10x^2 - 3x - 12 \\
 3x^2 + 2x - 4 \overline{) 30x^4 + 11x^3 - 82x^2 - 12x + 48} \\
 \underline{30x^4 + 20x^3 - 40x^2} \\
 -9x^3 - 42x^2 - 12x + 48 \\
 \underline{-9x^3 - 6x^2 + 12x} \\
 -36x^2 - 24x + 48 \\
 \underline{-36x^2 - 24x + 48} \\
 0
 \end{array}$$

∴ Quotient is $10x^2 - 3x - 12$ and the Remainder is 0.

20. $9x^4 - 4x^2 + 4$ by $3x^2 - 4x + 2$

Solution:

We have,

$$(9x^4 - 4x^2 + 4) / (3x^2 - 4x + 2)$$

By using long division method

$$\begin{array}{r}
 3x^2 + 4x + 2 \\
 3x^2 - 4x + 2 \overline{) 9x^4 + 0x^3 - 4x^2 + 0x + 4} \\
 \underline{9x^4 - 12x^3 + 6x^2} \\
 12x^3 - 10x^2 + 0x + 4 \\
 \underline{12x^3 - 16x^2 + 8x} \\
 6x^2 - 8x + 4 \\
 \underline{6x^2 - 8x + 4} \\
 0
 \end{array}$$

∴ Quotient is $3x^2 + 4x + 2$ and the Remainder is 0.

21. Verify division algorithm i.e. $\text{Dividend} = \text{Divisor} \times \text{Quotient} + \text{Remainder}$, in each of the following. Also, write the quotient and remainder:

Dividend	divisor
(i) $14x^2 + 13x - 15$	$7x - 4$
(ii) $15z^3 - 20z^2 + 13z - 12$	$3z - 6$
(iii) $6y^5 - 28y^3 + 3y^2 + 30y - 9$	$2x^2 - 6$
(iv) $34x - 22x^3 - 12x^4 - 10x^2 - 75$	$3x + 7$
(v) $15y^4 - 16y^3 + 9y^2 - 10/3y + 6$	$3y - 2$
(vi) $4y^3 + 8y + 8y^2 + 7$	$2y^2 - y + 1$
(vii) $6y^4 + 4y^4 + 4y^3 + 7y^2 + 27y + 6$	$2y^3 + 1$

Solution:

(i) Dividend	divisor
$14x^2 + 13x - 15$	$7x - 4$

By using long division method

$$\begin{array}{r}
 2x + 3 \\
 7x - 4 \overline{) 14x^2 + 13x - 15} \\
 \underline{14x^2 \quad - 8x} \\
 21x - 15 \\
 \underline{21x \quad - 12} \\
 -3
 \end{array}$$

Let us verify, $\text{Dividend} = \text{Divisor} \times \text{Quotient} + \text{Remainder}$

$$\begin{aligned}
 14x^2 + 13x - 15 &= (7x - 4) \times (2x + 3) + (-3) \\
 &= 14x^2 + 21x - 8x - 12 - 3 \\
 &= 14x^2 + 13x - 15
 \end{aligned}$$

Hence, verified.

\therefore Quotient is $2x + 3$ and the Remainder is -3 .

(ii) Dividend	divisor
$15z^3 - 20z^2 + 13z - 12$	$3z - 6$

By using long division method

$$\begin{array}{r}
 5z^2 + \frac{10z}{3} + 11 \\
 3z - 6 \overline{) 15z^3 - 20z^2 + 13z - 12} \\
 \underline{15z^3 - 30z^2} \\
 10z^2 + 13z - 12 \\
 \underline{10z^2 - 20z} \\
 33z - 12 \\
 \underline{33z - 66} \\
 54
 \end{array}$$

Let us verify, Dividend = Divisor \times Quotient + Remainder

$$\begin{aligned}
 15z^3 - 20z^2 + 13z - 12 &= (3z - 6) \times (5z^2 + 10z/3 + 11) + 54 \\
 &= 15z^3 + 10z^2 + 33z - 30z^2 - 20z + 54 \\
 &= 15z^3 - 20z^2 + 13z - 12
 \end{aligned}$$

Hence, verified.

\therefore Quotient is $5z^2 + 10z/3 + 11$ and the Remainder is 54.

(iii) Dividend $6y^5 - 28y^3 + 3y^2 + 30y - 9$	divisor $2x^2 - 6$
---	-----------------------

By using long division method

$$\begin{array}{r}
 3y^3 - 5y + \frac{3}{2} \\
 2y^2 - 6 \overline{) 6y^5 + 0y^4 - 28y^3 + 3y^2 + 30y - 9} \\
 \underline{6y^5 + 0y^4 - 18y^3} \\
 -10y^3 + 3y^2 + 30y - 9 \\
 \underline{-10y^3 + 0y^2 + 30y} \\
 3y^2 + 0y - 9 \\
 \underline{3y^2 + 0y - 9} \\
 0
 \end{array}$$

Let us verify, Dividend = Divisor \times Quotient + Remainder

$$\begin{aligned}
 6y^5 - 28y^3 + 3y^2 + 30y - 9 &= (2x^2 - 6) \times (3y^3 - 5y + 3/2) + 0 \\
 &= 6y^5 - 10y^3 + 3y^2 - 18y^3 + 30y - 9 \\
 &= 6y^5 - 28y^3 + 3y^2 + 30y - 9
 \end{aligned}$$

Hence, verified.

∴ Quotient is $3y^3 - 5y + 3/2$ and the Remainder is 0.

(iv) Dividend divisor
 $34x - 22x^3 - 12x^4 - 10x^2 - 75$ $3x + 7$
 $-12x^4 - 22x^3 - 10x^2 + 34x - 75$
 By using long division method

$$\begin{array}{r}
 -4x^3 + 2x^2 - 8x + 30 \\
 3x + 7 \overline{) -12x^4 - 22x^3 - 10x^2 + 34x - 75} \\
 \underline{-12x^4 - 28x^3} \\
 6x^3 - 10x^2 + 34x - 75 \\
 \underline{6x^3 + 14x^2} \\
 -24x^2 + 34x - 75 \\
 \underline{-24x^2 - 56x} \\
 90x - 75 \\
 \underline{90x + 210} \\
 -285
 \end{array}$$

Let us verify, Dividend = Divisor × Quotient + Remainder

$$\begin{aligned}
 -12x^4 - 22x^3 - 10x^2 + 34x - 75 &= (3x + 7) \times (-4x^3 + 2x^2 - 8x + 30) - 285 \\
 &= -12x^4 + 6x^3 - 24x^2 - 28x^3 + 14x^2 + 90x - 56x + 210 - 285 \\
 &= -12x^4 - 22x^3 - 10x^2 + 34x - 75
 \end{aligned}$$

Hence, verified.

∴ Quotient is $-4x^3 + 2x^2 - 8x + 30$ and the Remainder is -285.

(v) Dividend divisor
 $15y^4 - 16y^3 + 9y^2 - 10/3y + 6$ $3y - 2$
 By using long division method

$$\begin{array}{r}
 5y^3 - 2y^2 + \frac{5y}{3} \\
 3y - 2 \overline{) 15y^4 - 16y^3 + 9y^2 - \frac{10y}{3} + 6} \\
 \underline{15y^4 - 10y^3} \phantom{+ 9y^2 - \frac{10y}{3} + 6} \\
 -6y^3 + 9y^2 - \frac{10y}{3} + 6 \\
 \underline{-6y^3 + 4y^2} \phantom{- \frac{10y}{3} + 6} \\
 5y^2 - \frac{10y}{3} + 6 \\
 \underline{5y^2 - \frac{10y}{3}} \\
 0 \quad 6
 \end{array}$$

Let us verify, Dividend = Divisor \times Quotient + Remainder

$$\begin{aligned}
 15y^4 - 16y^3 + 9y^2 - 10/3y + 6 &= (3y - 2) \times (5y^3 - 2y^2 + 5y/3) + 6 \\
 &= 15y^4 - 6y^3 + 5y^2 - 10y^3 + 4y^2 - 10y/3 + 6 \\
 &= 15y^4 - 16y^3 + 9y^2 - 10/3y + 6
 \end{aligned}$$

Hence, verified.

\therefore Quotient is $5y^3 - 2y^2 + 5y/3$ and the Remainder is 6.

<p>(vi) Dividend $4y^3 + 8y + 8y^2 + 7$ $4y^3 + 8y^2 + 8y + 7$</p>	<p>divisor $2y^2 - y + 1$</p>
--	---

By using long division method

$$\begin{array}{r}
 2y + 5 \\
 2y^2 - y + 1 \overline{) 4y^3 + 8y^2 + 8y + 7} \\
 \underline{4y^3 - 2y^2 + 2y} \\
 10y^2 + 6y + 7 \\
 \underline{10y^2 - 5y + 5} \\
 11y + 2
 \end{array}$$

Let us verify, Dividend = Divisor \times Quotient + Remainder

$$4y^3 + 8y^2 + 8y + 7 = (2y^2 - y + 1) \times (2y + 5) + 11y + 2$$

$$\begin{aligned}
 &= 4y^3 + 10y^2 - 2y^2 - 5y + 2y + 5 + 11y + 2 \\
 &= 4y^3 + 8y^2 + 8y + 7
 \end{aligned}$$

Hence, verified.

∴ Quotient is $2y + 5$ and the Remainder is $11y + 2$.

(vii) Dividend $6y^5 + 4y^4 + 4y^3 + 7y^2 + 27y + 6$	divisor $2y^3 + 1$
---	-----------------------

By using long division method

$$\begin{array}{r}
 \quad \quad \quad 3y^2 + 2y + 2 \\
 \hline
 2y^3 + 1 \quad \bigg) \quad 6y^5 + 4y^4 + 4y^3 + 7y^2 + 27y + 6 \\
 \quad \quad \quad \underline{6y^5 + 0y^4 + 0y^3 + 3y^2} \\
 \quad \quad \quad 4y^4 + 4y^3 + 4y^2 + 27y + 6 \\
 \quad \quad \quad \underline{4y^4 + 0y^3 + 0y^2 + 2y} \\
 \quad \quad \quad 4y^3 + 4y^2 + 25y + 6 \\
 \quad \quad \quad \underline{4y^3 + 0y^2 + 0y + 2} \\
 \quad \quad \quad 4y^2 + 25y + 4
 \end{array}$$

Let us verify, Dividend = Divisor × Quotient + Remainder

$$\begin{aligned}
 6y^5 + 4y^4 + 4y^3 + 7y^2 + 27y + 6 &= (2y^3 + 1) \times (3y^2 + 2y + 2) + 4y^2 + 25y + 4 \\
 &= 6y^5 + 4y^4 + 4y^3 + 3y^2 + 2y + 2 + 4y^2 + 25y + 4 \\
 &= 6y^5 + 4y^4 + 4y^3 + 7y^2 + 27y + 6
 \end{aligned}$$

Hence, verified.

∴ Quotient is $3y^2 + 2y + 2$ and the Remainder is $4y^2 + 25y + 4$.

22. Divide $15y^4 + 16y^3 + 10/3y - 9y^2 - 6$ by $3y - 2$ Write down the coefficients of the terms in the quotient.

Solution:

We have,

$$(15y^4 + 16y^3 + 10/3y - 9y^2 - 6) / (3y - 2)$$

By using long division method

$$\begin{array}{r}
 5y^3 + \frac{26y^2}{3} + \frac{25y}{9} + \frac{80}{27} \\
 3y - 2 \overline{) 15y^4 + 16y^3 - 9y^2 + \frac{10y}{3} - 6} \\
 \underline{15y^4 - 10y^3} \phantom{- 9y^2 + \frac{10y}{3} - 6} \\
 26y^3 - 9y^2 + \frac{10y}{3} - 6 \\
 \underline{26y^3 - \frac{52y^2}{3}} \phantom{+ \frac{10y}{3} - 6} \\
 \frac{25y^2}{3} + \frac{10y}{3} - 6 \\
 \underline{\phantom{\frac{25y^2}{3}} + \frac{50y}{9}} \\
 \frac{80y}{9} - 6 \\
 \underline{\phantom{\frac{80y}{9}} - \frac{160}{27}} \\
 -\frac{2}{27}
 \end{array}$$

∴ Quotient is $5y^3 + 26y^2/3 + 25y/9 + 80/27$

So the coefficients of the terms in the quotient are:

Coefficient of $y^3 = 5$

Coefficient of $y^2 = 26/3$

Coefficient of $y = 25/9$

Constant term = $80/27$

23. Using division of polynomials state whether

(i) $x + 6$ is a factor of $x^2 - x - 42$

(ii) $4x - 1$ is a factor of $4x^2 - 13x - 12$

(iii) $2y - 5$ is a factor of $4y^4 - 10y^3 - 10y^2 + 30y - 15$

(iv) $3y^2 + 5$ is a factor of $6y^5 + 15y^4 + 16y^3 + 4y^2 + 10y - 35$

(v) $z^2 + 3$ is a factor of $z^5 - 9z$

(vi) $2x^2 - x + 3$ is a factor of $6x^5 - x^4 + 4x^3 - 5x^2 - x - 15$

Solution:

(i) $x + 6$ is a factor of $x^2 - x - 42$

Firstly let us perform long division method

$$\begin{array}{r}
 x - 7 \\
 x + 6 \overline{) x^2 - x - 42} \\
 \underline{-} \\
 x^2 + 6x \\
 \underline{-} \\
 -7x - 42 \\
 \underline{-} \\
 -7x - 42 \\
 \underline{-} \\
 0
 \end{array}$$

Since the remainder is 0, we can say that $x + 6$ is a factor of $x^2 - x - 42$

(ii) $4x - 1$ is a factor of $4x^2 - 13x - 12$

Firstly let us perform long division method

$$\begin{array}{r}
 x - 3 \\
 4x - 1 \overline{) 4x^2 - 13x - 12} \\
 \underline{-} \\
 4x^2 - x \\
 \underline{-} \\
 -12x - 12 \\
 \underline{-} \\
 -12x + 3 \\
 \underline{-} \\
 -15
 \end{array}$$

Since the remainder is -15, $4x - 1$ is not a factor of $4x^2 - 13x - 12$

(iii) $2y - 5$ is a factor of $4y^4 - 10y^3 - 10y^2 + 30y - 15$

Firstly let us perform long division method

$$\begin{array}{r}
 2y^3 - 5y + \frac{5}{2} \\
 2y - 5 \overline{) 4y^4 - 10y^3 - 10y^2 + 30y - 15} \\
 \underline{-} \\
 4y^4 - 10y^3 \\
 \underline{-} \\
 0 - 10y^2 + 30y - 15 \\
 \underline{-} \\
 -10y^3 + 25y^2 \\
 \underline{-} \\
 10y^3 - 35y^2 + 30y - 15 \\
 \underline{-} \\
 5y^3 - \frac{25y^2}{2} \\
 \underline{-} \\
 5y^3 - \frac{45y^2}{2} + 30y - 15
 \end{array}$$

Since the remainder is $5y^3 - 45y^2/2 + 30y - 15$, $2y - 5$ is not a factor of $4y^4 - 10y^3 - 10y^2 + 30y - 15$

(iv) $3y^2 + 5$ is a factor of $6y^5 + 15y^4 + 16y^3 + 4y^2 + 10y - 35$

Firstly let us perform long division method

$$\begin{array}{r}
 2y^3 + 5y^2 + 2y - 7 \\
 3y^2 + 5 \overline{) 6y^5 + 15y^4 + 16y^3 + 4y^2 + 10y - 35} \\
 \underline{6y^5 + 15y^4 + 10y^3} \\
 6y^3 + 4y^2 + 10y - 35 \\
 \underline{6y^3 + 10y^2 + 25y} \\
 -6y^2 - 15y - 35 \\
 \underline{-6y^2 - 10y - 25} \\
 -5y - 10 \\
 \underline{-5y - 10} \\
 0
 \end{array}$$

Since the remainder is 0, $3y^2 + 5$ is a factor of $6y^5 + 15y^4 + 16y^3 + 4y^2 + 10y - 35$

(v) $z^2 + 3$ is a factor of $z^5 - 9z$

Firstly let us perform long division method

$$\begin{array}{r}
 z^3 - 3z \\
 z^2 + 3 \overline{) z^5 + 0z^4 + 0z^3 + 0z^2 - 9z + 0} \\
 \underline{z^5 + 0z^4 + 3z^3} \\
 -3z^3 + 0z^2 - 9z + 0 \\
 \underline{-3z^3 + 0z^2 - 9z} \\
 0
 \end{array}$$

Since the remainder is 0, $z^2 + 3$ is a factor of $z^5 - 9z$

(vi) $2x^2 - x + 3$ is a factor of $6x^5 - x^4 + 4x^3 - 5x^2 - x - 15$

Firstly let us perform long division method

$$\begin{array}{r}
 3x^3 + x^2 - 2x - 5 \\
 2x^2 - x + 3 \overline{) 6x^5 - x^4 + 4x^3 - 5x^2 - x - 15} \\
 \underline{6x^5 - 3x^4 + 9x^3} \\
 2x^4 - 5x^3 - 5x^2 - x - 15 \\
 \underline{2x^4 - x^3 + 3x^2} \\
 -4x^3 - 8x^2 - x - 15 \\
 \underline{-4x^3 + 2x^2 - 6x} \\
 -10x^2 + 5x - 15 \\
 \underline{-10x^2 + 5x - 15} \\
 0
 \end{array}$$

Since the remainder is 0, $2x^2 - x + 3$ is a factor of $6x^5 - x^4 + 4x^3 - 5x^2 - x - 15$

24. Find the value of a, if $x + 2$ is a factor of $4x^4 + 2x^3 - 3x^2 + 8x + 5a$

Solution:

We know that $x + 2$ is a factor of $4x^4 + 2x^3 - 3x^2 + 8x + 5a$

Let us equate $x + 2 = 0$

$$x = -2$$

Now let us substitute $x = -2$ in the equation $4x^4 + 2x^3 - 3x^2 + 8x + 5a$

$$4(-2)^4 + 2(-2)^3 - 3(-2)^2 + 8(-2) + 5a = 0$$

$$64 - 16 - 12 - 16 + 5a = 0$$

$$20 + 5a = 0$$

$$5a = -20$$

$$a = -20/5$$

$$= -4$$

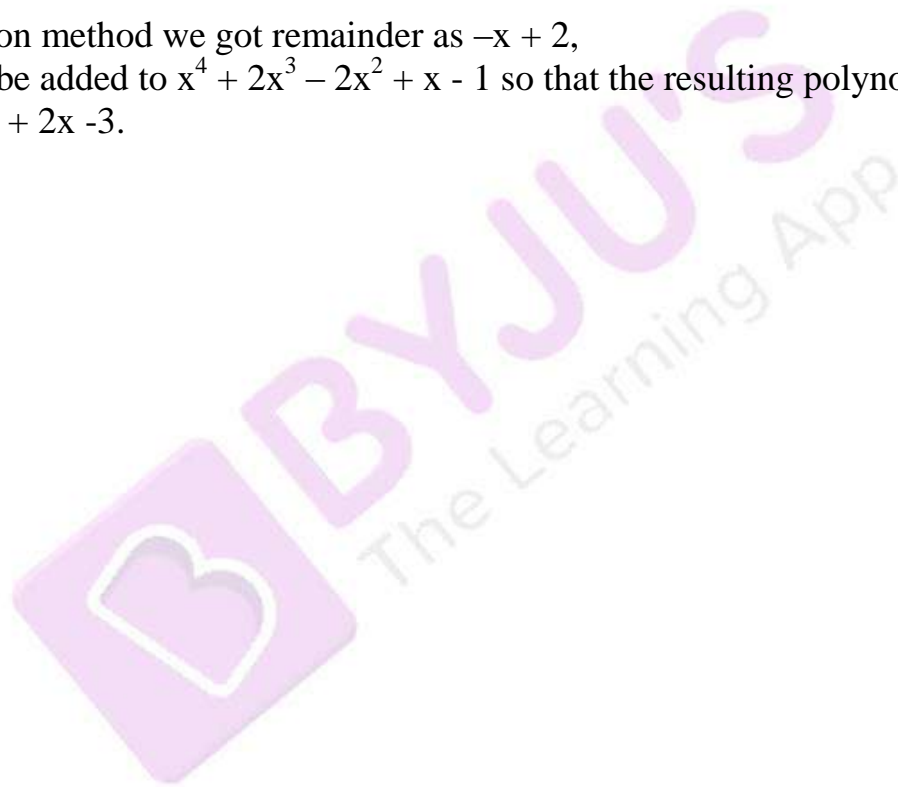
25. What must be added to $x^4 + 2x^3 - 2x^2 + x - 1$ so that the resulting polynomial is exactly divisible by $x^2 + 2x - 3$.

Solution:

Firstly let us perform long division method

$$\begin{array}{r}
 x^2 + 1 \\
 x^2 + 2x - 3 \overline{) x^4 + 2x^3 - 2x^2 + x - 1} \\
 \underline{-} \\
 x^4 + 2x^3 - 3x^2 \\
 \underline{-} \\
 x^2 + x - 1 \\
 \underline{-} \\
 x^2 + 2x - 3 \\
 \underline{-} \\
 -x + 2
 \end{array}$$

By long division method we got remainder as $-x + 2$,
 $\therefore x - 2$ has to be added to $x^4 + 2x^3 - 2x^2 + x - 1$ so that the resulting polynomial is exactly divisible by $x^2 + 2x - 3$.



EXERCISE 8.5
PAGE NO: 8.15

1. Divide the first polynomial by the second polynomial in each of the following. Also, write the quotient and remainder:

(i) $3x^2 + 4x + 5, x - 2$

(ii) $10x^2 - 7x + 8, 5x - 3$

(iii) $5y^3 - 6y^2 + 6y - 1, 5y - 1$

(iv) $x^4 - x^3 + 5x, x - 1$

(v) $y^4 + y^2, y^2 - 2$

Solution:

(i) $3x^2 + 4x + 5, x - 2$

By using long division method

$$\begin{array}{r}
 3x + 10 \\
 x - 2 \overline{) 3x^2 + 4x + 5} \\
 \underline{-} \\
 3x^2 - 6x \\
 \hline
 10x + 5 \\
 \underline{-} \\
 10x - 20 \\
 \hline
 25
 \end{array}$$

∴ the Quotient is $3x + 10$ and the Remainder is 25.

(ii) $10x^2 - 7x + 8, 5x - 3$

By using long division method

$$\begin{array}{r}
 2x - \frac{1}{5} \\
 5x - 3 \overline{) 10x^2 - 7x + 8} \\
 \underline{-} \\
 10x^2 - 6x \\
 \hline
 -x + 8 \\
 \underline{-} \\
 -x + \frac{3}{5} \\
 \hline
 \frac{37}{5}
 \end{array}$$

∴ the Quotient is $2x - 1/5$ and the Remainder is $37/5$.

(iii) $5y^3 - 6y^2 + 6y - 1$, $5y - 1$

By using long division method

$$\begin{array}{r}
 y^2 - y + 1 \\
 5y - 1 \overline{) 5y^3 - 6y^2 + 6y - 1} \\
 \underline{5y^3 + 5y^2 - 5y^2} \\
 -y^2 + 6y - 1 \\
 \underline{-y^2 + 5y - 1} \\
 5y - 1 \\
 \underline{5y - 1} \\
 0
 \end{array}$$

∴ the Quotient is $y^2 - y + 1$ and the Remainder is 0.

(iv) $x^4 - x^3 + 5x$, $x - 1$

By using long division method

$$\begin{array}{r}
 x^3 + 5 \\
 x - 1 \overline{) x^4 - x^3 + 0x^2 + 5x + 0} \\
 \underline{x^4 - x^3} \\
 0 + 0x^2 + 5x + 0 \\
 \underline{5x^3 - 5x^2} \\
 -5x^3 + 5x^2 + 5x + 0
 \end{array}$$

∴ the Quotient is $x^3 + 5$ and the Remainder is 5.

(v) $y^4 + y^2$, $y^2 - 2$

By using long division method

$$\begin{array}{r}
 y^2 + 3 \\
 y^2 - 2 \overline{) y^4 + 0y^3 + y^2 + 0y + 0} \\
 \underline{-} \\
 y^4 + 0y^3 - 2y^2 \\
 \underline{-} \\
 3y^2 + 0y + 0 \\
 \underline{-} \\
 3y^2 + 0y - 6 \\
 \underline{-} \\
 6
 \end{array}$$

∴ the Quotient is $y^2 + 3$ and the Remainder is 6.

2. Find Whether or not the first polynomial is a factor of the second:

- (i) $x + 1, 2x^2 + 5x + 4$
- (ii) $y - 2, 3y^3 + 5y^2 + 5y + 2$
- (iii) $4x^2 - 5, 4x^4 + 7x^2 + 15$
- (iv) $4 - z, 3z^2 - 13z + 4$
- (v) $2a - 3, 10a^2 - 9a - 5$
- (vi) $4y + 1, 8y^2 - 2y + 1$

Solution:

- (i) $x + 1, 2x^2 + 5x + 4$

Let us perform long division method,

$$\begin{array}{r}
 2x + 3 \\
 x + 1 \overline{) 2x^2 + 5x + 4} \\
 \underline{-} \\
 2x^2 + 2x \\
 \underline{-} \\
 3x + 4 \\
 \underline{-} \\
 3x + 3 \\
 \underline{-} \\
 1
 \end{array}$$

Since remainder is 1 therefore the first polynomial is not a factor of the second polynomial.

- (ii) $y - 2, 3y^3 + 5y^2 + 5y + 2$

Let us perform long division method,

$$\begin{array}{r}
 3y^2 + 11y + 27 \\
 y - 2 \overline{) 3y^3 + 5y^2 + 5y + 2} \\
 \underline{-} \\
 3y^3 - 6y^2 \\
 \underline{-} \\
 11y^2 + 5y + 2 \\
 \underline{-} \\
 11y^2 - 22y \\
 \underline{-} \\
 27y + 2 \\
 \underline{-} \\
 27y - 54 \\
 \underline{-} \\
 56
 \end{array}$$

Since remainder is 56 therefore the first polynomial is not a factor of the second polynomial.

(iii) $4x^2 - 5$, $4x^4 + 7x^2 + 15$

Let us perform long division method,

$$\begin{array}{r}
 x^2 + 3 \\
 4x^2 - 5 \overline{) 4x^4 + 0x^3 + 7x^2 + 0x + 15} \\
 \underline{-} \\
 4x^4 + 0x^3 - 5x^2 \\
 \underline{-} \\
 12x^2 + 0x + 15 \\
 \underline{-} \\
 12x^2 + 0x - 15 \\
 \underline{-} \\
 30
 \end{array}$$

Since remainder is 30 therefore the first polynomial is not a factor of the second polynomial.

(iv) $4 - z$, $3z^2 - 13z + 4$

Let us perform long division method,

$$\begin{array}{r}
 -3z + 1 \\
 -z + 4 \overline{) 3z^2 - 13z + 4} \\
 \underline{-} \\
 3z^2 - 12z \\
 \underline{-} \\
 -z + 4 \\
 \underline{-} \\
 -z + 4 \\
 \underline{-} \\
 0
 \end{array}$$

Since remainder is 0 therefore the first polynomial is a factor of the second polynomial.

(v) $2a - 3, 10a^2 - 9a - 5$

Let us perform long division method,

$$\begin{array}{r}
 5a + 3 \\
 2a - 3 \overline{) 10a^2 - 9a - 5} \\
 \underline{-} \\
 10a^2 - 15a \\
 \underline{-} \\
 6a - 5 \\
 \underline{-} \\
 6a - 9 \\
 \underline{-} \\
 4
 \end{array}$$

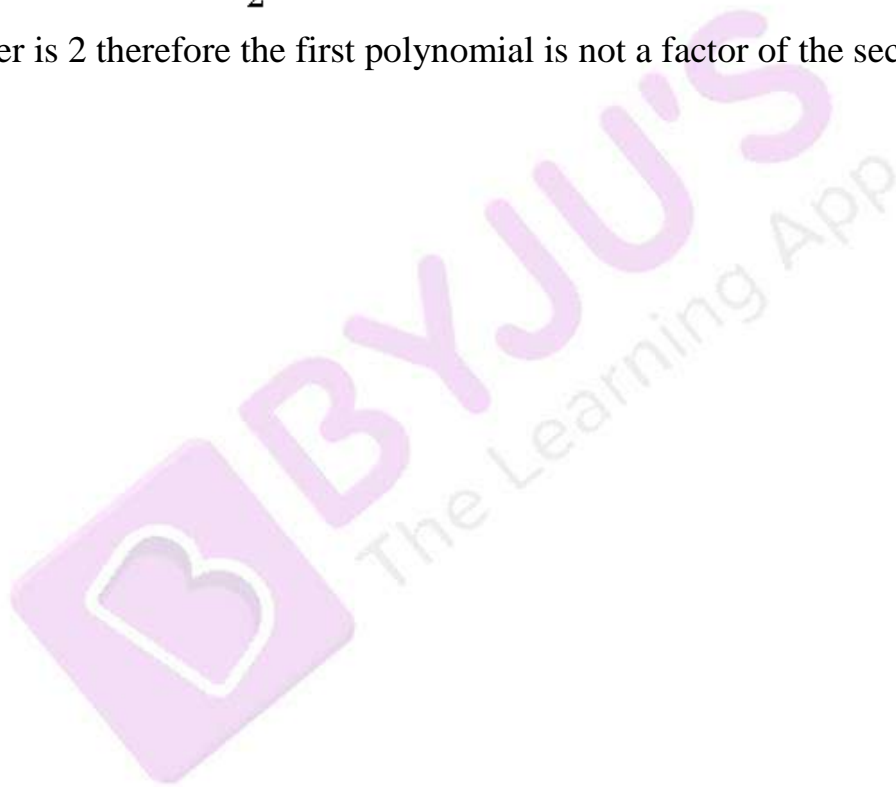
Since remainder is 4 therefore the first polynomial is not a factor of the second polynomial.

(vi) $4y + 1, 8y^2 - 2y + 1$

Let us perform long division method,

$$\begin{array}{r} 2y - 1 \\ 4y + 1 \overline{) 8y^2 - 2y + 1} \\ \underline{8y^2 + 2y} \\ -4y + 1 \\ \underline{-4y - 1} \\ 2 \end{array}$$

Since remainder is 2 therefore the first polynomial is not a factor of the second polynomial.



EXERCISE 8.6

PAGE NO: 8.17

Divide:

1. $x^2 - 5x + 6$ by $x - 3$

Solution:

We have,

$$(x^2 - 5x + 6) / (x - 3)$$

Let us perform long division method,

$$\begin{array}{r}
 x - 2 \\
 x - 3 \overline{) x^2 - 5x + 6} \\
 \underline{-} \\
 x^2 - 3x \\
 \underline{-} \\
 -2x + 6 \\
 \underline{-} \\
 -2x + 6 \\
 \underline{-} \\
 0
 \end{array}$$

∴ the Quotient is $x - 2$

2. $ax^2 - ay^2$ by $ax+ay$

Solution:

We have,

$$(ax^2 - ay^2) / (ax+ay)$$

$$\begin{aligned}
 (ax^2 - ay^2) / (ax+ay) &= (x - y) + 0/(ax+ay) \\
 &= (x - y)
 \end{aligned}$$

∴ the answer is $(x - y)$

3. $x^4 - y^4$ by $x^2 - y^2$

Solution:

We have,

$$(x^4 - y^4) / (x^2 - y^2)$$

$$\begin{aligned}
 (x^4 - y^4) / (x^2 - y^2) &= x^2 + y^2 + 0/(x^2 - y^2) \\
 &= x^2 + y^2
 \end{aligned}$$

∴ the answer is $(x^2 + y^2)$

4. $acx^2 + (bc + ad)x + bd$ by $(ax + b)$

Solution:

We have,

$$\begin{aligned} & (acx^2 + (bc + ad)x + bd) / (ax + b) \\ & (acx^2 + (bc + ad)x + bd) / (ax + b) = cx + d + 0 / (ax + b) \\ & \qquad \qquad \qquad = cx + d \end{aligned}$$

∴ the answer is $(cx + d)$

5. $(a^2 + 2ab + b^2) - (a^2 + 2ac + c^2)$ by $2a + b + c$

Solution:

We have,

$$\begin{aligned} & [(a^2 + 2ab + b^2) - (a^2 + 2ac + c^2)] / (2a + b + c) \\ & [(a^2 + 2ab + b^2) - (a^2 + 2ac + c^2)] / (2a + b + c) = b - c + 0 / (2a + b + c) \\ & \qquad \qquad \qquad = b - c \end{aligned}$$

∴ the answer is $(b - c)$

6. $1/4x^2 - 1/2x - 12$ by $1/2x - 4$

Solution:

We have,

$$(1/4x^2 - 1/2x - 12) / (1/2x - 4)$$

Let us perform long division method,

$$\begin{array}{r} \frac{x}{2} + 3 \\ \frac{x}{2} - 4 \overline{) \frac{x^2}{4} - \frac{x}{2} + 0} \\ \underline{-} \\ \frac{x^2}{4} - 2x \\ \underline{-} \\ \frac{3x}{2} + 0 \\ \underline{-} \\ \frac{3x}{2} - 12 \\ \underline{-} \\ 12 \end{array}$$

∴ the Quotient is $x/2 + 3$