

Exercise 11(A)

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1. Find which of the following sequence form a G.P.:

(i) 8, 24, 72, 216,

(ii) $\frac{1}{8}$, $\frac{1}{24}$, $\frac{1}{72}$, $\frac{1}{216}$,

(iii) 9, 12, 16, 24,

Solution:

(i) Given sequence: 8, 24, 72, 216,

Since,

$$24/8 = 3, 72/24 = 3, 216/72 = 3$$

$$\Rightarrow 24/8 = 72/24 = 216/72 = \dots = 3$$

Therefore 8, 24, 72, 216, is a G.P. with a common ratio 3.

(ii) Given sequence: $\frac{1}{8}$, $\frac{1}{24}$, $\frac{1}{72}$, $\frac{1}{216}$,

Since,

$$(\frac{1}{24})/(\frac{1}{8}) = \frac{1}{3}, (\frac{1}{72})/(\frac{1}{24}) = \frac{1}{3}, (\frac{1}{216})/(\frac{1}{72}) = \frac{1}{3}$$

$$\Rightarrow (\frac{1}{24})/(\frac{1}{8}) = (\frac{1}{72})/(\frac{1}{24}) = (\frac{1}{216})/(\frac{1}{72}) = \dots = \frac{1}{3}$$

Therefore $\frac{1}{8}$, $\frac{1}{24}$, $\frac{1}{72}$, $\frac{1}{216}$, is a G.P. with a common ratio $\frac{1}{3}$.

(iii) Given sequence: 9, 12, 16, 24,

Since,

$$12/9 = 4/3; 16/12 = 4/3; 24/16 = 3/2$$

$$12/9 = 16/12 \neq 24/16$$

Therefore, 9, 12, 16, 24 is not a G.P.

2. Find the 9th term of the series: 1, 4, 16, 64,

Solution:

It's seen that, the first term is $(a) = 1$

And, common ratio $(r) = 4/1 = 4$

We know that, the general term is

$$t_n = ar^{n-1}$$

Thus,

$$t_9 = (1)(4)^{9-1} = 4^8 = 65536$$

3. Find the seventh term of the G.P: 1, $\sqrt{3}$, 3, $3\sqrt{3}$,

Solution:

It's seen that, the first term is $(a) = 1$

And, common ratio $(r) = \sqrt{3}/1 = \sqrt{3}$

We know that, the general term is

$$t_n = ar^{n-1}$$

Thus,

$$t_7 = (1)(\sqrt{3})^{7-1} = (\sqrt{3})^6 = 27$$

4. Find the 8th term of the sequence:

$$\frac{3}{4}, 1\frac{1}{2}, 3, \dots$$

Solution:

The given sequence can be rewritten as,
 $\frac{3}{4}, \frac{3}{2}, 3, \dots$

It's seen that, the first term is $(a) = \frac{3}{4}$

And, common ratio $(r) = \frac{3/2}{3/4} = 2$

We know that, the general term is

$$t_n = ar^{n-1}$$

Thus,

$$t_8 = \left(\frac{3}{4}\right)(2)^{8-1} = \left(\frac{3}{4}\right)(2)^7 = 3 \times 2^5 = 3 \times 32 = 96$$

5. Find the 10th term of the G.P. :

$$12, 4, 1\frac{1}{3}, \dots$$

Solution:

The given sequence can be rewritten as,
 $12, 4, \frac{4}{3}, \dots$

It's seen that, the first term is $(a) = 12$

And, common ratio $(r) = \frac{4}{12} = \frac{1}{3}$

We know that, the general term is

$$t_n = ar^{n-1}$$

Thus,

$$t_{10} = (12)\left(\frac{1}{3}\right)^{10-1} = (12)\left(\frac{1}{3}\right)^9 = 12 \times \frac{1}{19683} = \frac{4}{6561}$$

6. Find the n th term of the series:

$$1, 2, 4, 8, \dots$$

Solution:

It's seen that, the first term is $(a) = 1$

And, common ratio $(r) = \frac{2}{1} = 2$

We know that, the general term is

$$t_n = ar^{n-1}$$

Thus,

$$t_n = (1)(2)^{n-1} = 2^{n-1}$$