

Exercise 14(C)

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1. Find the equation of a line whose: y - intercept = 2 and slope = 3. Solution:

Given,

y - intercept = c = 2 and slope = m = 3. The line equation is given by: y = mx + cOn substituting the values of c and m, we get y = 3x + 2The above is the required line equation.

2. Find the equation of a line whose: y - intercept = -1 and inclination = 45°. Solution:

Given, y - intercept = c = -1 and inclination = 45°. So, slope = $m = \tan 45^\circ = 1$ Hence, on substituting the values of c and m in the line equation y = mx + c, we get y = x - 1The above is the required line equation.

3. Find the equation of the line whose slope is -4/3 and which passes through (-3, 4). Solution:

Given, slope = -4/3The line passes through the point (-3, 4) = (x₁, y₁) Now, on substituting the values in y - y₁ = m(x - x₁), we have y - 4 = -4/3 (x + 3) 3y - 12 = -4x - 124x + 3y = 0 Hence, the above is the required line equation.

4. Find the equation of a line which passes through (5, 4) and makes an angle of 60° with the positive direction of the x-axis. Solution:

The slope of the line, $m = \tan 60^\circ = \sqrt{3}$ And, the line passes through the point $(5, 4) = (x_1, y_1)$ Hence, on substituting the values in $y - y_1 = m(x - x_1)$, we have $y - 4 = \sqrt{3} (x - 5)$ $y - 4 = \sqrt{3}x - 5\sqrt{3}$ $y = \sqrt{3}x + 4 - 5\sqrt{3}$, which is the required line equation.



5. Find the equation of the line passing through: (i) (0, 1) and (1, 2) (ii) (-1, -4) and (3, 0) Solution:

(i) Let $(0, 1) = (x_1, y_1)$ and $(1, 2) = (x_2, y_2)$ So. Slope of the line = (2 - 1)/(1 - 0) = 1Now. The required line equation is given by, $y - y_1 = m(x - x_1)$ y - 1 = 1(x - 0)y - 1 = xy = x + 1(ii) Let $(-1, -4) = (x_1, y_1)$ and $(3, 0) = (x_2, y_2)$ So. Slope of the line = (0 + 4)/(3 + 1) = 4/4 = 1The required line equation is given by, $y - y_1 = m(x - x_1)$ y + 4 = 1(x + 1)y + 4 = x + 1y = x - 3

6. The co-ordinates of two points P and Q are (2, 6) and (-3, 5) respectively. Find:
(i) the gradient of PQ;
(ii) the equation of PQ;
(iii) the co-ordinates of the point where PQ intersects the x-axis.
Solution:

Given, The co-ordinates of two points P and Q are (2, 6) and (-3, 5) respectively. (i) Gradient of PQ = (5 - 6)/(-3 - 2) = -1/-5 = 1/5

(ii) The line equation of PQ is given by $y_{ij} = m(y_{ij}, y_{ij})$

 $y - y_1 = m(x - x_1)$ y - 6 = 1/5 (x - 2) 5y - 30 = x - 2 5y = x + 28

(iii) Let the line PQ intersect the x-axis at point A (x, 0). So, on putting y = 0 in the line equation of PQ, we get 0 = x + 28x = -28Hence, the co-ordinates of the point where PQ intersects the x-axis are A (-28, 0).



7. The co-ordinates of two points A and B are (-3, 4) and (2, -1). Find:
(i) the equation of AB;
(ii) the co-ordinates of the point where the line AB intersects the y-axis. Solution:

(i) Given, co-ordinates of two points A and B are (-3, 4) and (2, -1). Slope = (-1 - 4)/(2 + 3) = -5/5 = -1The equation of the line AB is given by: $y - y_1 = m(x - x_1)$ y + 1 = -1(x - 2) y + 1 = -x + 2x + y = 1

(ii) Let's consider the line AB intersect the y-axis at point (0, y).

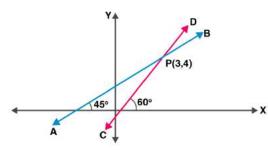
On putting x = 0 in the line equation, we get

0 + y = 1

y = 1

Thus, the co-ordinates of the point where the line AB intersects the y-axis are (0, 1).

8. The figure given below shows two straight lines AB and CD intersecting each other at point P (3, 4). Find the equation of AB and CD.



Solution:

The slope of line AB = $\tan 45^\circ = 1$ And, the line AB passes through P (3, 4). Hence, the equation of the line AB is given by $y - y_1 = m(x - x_1)$ y - 4 = 1(x - 3)y - 4 = x - 3y = x + 1

The slope of line CD = tan $60^\circ = \sqrt{3}$ And, the line CD passes through P (3, 4). Hence, the equation of the line CD is given by $y - y_1 = m(x - x_1)$ $y - 4 = \sqrt{3} (x - 3)$ $y - 4 = \sqrt{3x} - 3\sqrt{3}$



 $y = \sqrt{3}x + 4 - 3\sqrt{3}$

9. In $\triangle ABC$, A = (3, 5), B = (7, 8) and C = (1, -10). Find the equation of the median through A. Solution:

Given,

Vertices of $\triangle ABC$, A = (3, 5), B = (7, 8) and C = (1, -10). Coordinates of the mid-point D of BC = $(x_1 + x_2) / 2$, $(y_1 + y_2) / 2$

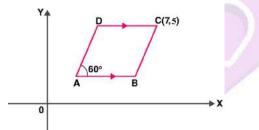
$$= \left(\frac{7+1}{2}, \frac{8+(-10)}{2}\right)$$
$$= \left(\frac{8}{2}, \frac{-2}{2}\right)$$
$$= (4, -1)$$

The slope of AD = $(y_2 - y_1)/(x_2 - x_1)$ = (-1 - 5)/(4 - 3)= -6/1= -6

Hence, the equation of the median AD through A is given by

 $y - y_1 = m (x - x_1)$ y - 5 = -6(x - 3) y - 5 = -6x + 186x + y = 23

10. The following figure shows a parallelogram ABCD whose side AB is parallel to the x-axis, $\angle A = 60^{\circ}$ and vertex C = (7, 5). Find the equations of BC and CD.



Solution:

Given, $\angle A = 60^{\circ}$ and vertex C = (7, 5)As, ABCD is a parallelogram, we have $\angle A + \angle B = 180^{\circ}$ [corresponding angles] $\angle B = 180^{\circ} - 60^{\circ} = 120^{\circ}$ Slope of BC = tan 120° = tan (90° + 30°) = cot 30° = $\sqrt{3}$ So, the equation of line BC is given by $y - y_1 = m(x - x_1)$ $y - 5 = \sqrt{3} (x - 7)$ $y - 5 = \sqrt{3x} - 7\sqrt{3}$



 $y = \sqrt{3x + 5} - 7\sqrt{3}$ As, CD || AB and AB || x-axis Slope of CD = Slope of AB = 0 [As slope of x-axis is zero] So, the equation of the line CD is given by $y - y_1 = m(x - x_1)$ y - 5 = 0(x - 7)y = 5

11. Find the equation of the straight line passing through origin and the point of intersection of the lines x + 2y = 7 and x - y = 4. Solution:

The given line equations are: $x + 2y = 7 \dots (1)$ $x - y = 4 \dots (2)$ On solving the above line equations, we can find the point of intersection of the two lines. So, subtracting (2) from (1), we get 3y = 3y = 1 Now, x = 4 + y = 4 + 1 = 5 [From (2)] It's given that, The required line passes through (0, 0) and (5, 1). The slope of the line = (1 - 0)/(5 - 0) = 1/5Hence, the required equation of the line is given by $y - y_1 = m(x - x_1)$ y - 0 = 1/5(x - 0)5y = xx - 5y = 0

