

EXERCISE 10(E)

1. Write the cardinal number of each of the following sets:

(i) $A = \{0, 1, 2, 4\}$

(ii) $B = \{-3, -1, 1, 3, 5, 7\}$

(iii) $C = \{\}$

(iv) $D = \{3, 2, 2, 1, 3, 1, 2\}$

(v) $E = \{\text{Natural numbers between 15 and 20}\}$

Solution:

(i) Given set is

$$A = \{0, 1, 2, 4\}$$

Here, the cardinal number i.e. $n(A) = 4$

(ii) Given set is

$$B = \{-3, -1, 1, 3, 5, 7\}$$

Here, the cardinal number i.e. $n(B) = 6$

(iii) Given set is

$$C = \{\}$$

Here, the cardinal number i.e. $n(C) = 0$

(iv) Given set is

$$D = \{3, 2, 2, 1, 3, 1, 2\}$$

$$D = \{1, 2, 3\}$$

Here, the cardinal number i.e. $n(D) = 3$

(v) Given set is

$$E = \{\text{Natural numbers between 15 and 20}\}$$

$$E = \{16, 17, 18, 19\}$$

Here, the cardinal number i.e. $n(E) = 4$

2. Given

(i) $A = \{\text{Natural numbers less than 10}\}$

$B = \{\text{Letters of the word 'PUPPET'}\}$

$C = \{\text{Squares of first four whole numbers}\}$

$D = \{\text{Odd numbers divisible by 2}\}$

Find:

(i) $n(A)$

(ii) $n(B)$

(iii) $n(C)$

(iv) $n(D)$

(v) $A \cap B$ and $(A \cup B)$

Solution:

(i) Given

$A = \{\text{Natural numbers less than } 10\}$
 $B = \{\text{Letters of the word 'PUPPET'}\}$
 $C = \{\text{Squares of first four whole numbers}\}$
 $D = \{\text{Odd numbers divisible by } 2\}$

Here,

$A = \{\text{Natural numbers less than } 10\}$

$A = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

Hence, $n(A) = 9$

(ii) Given

$A = \{\text{Natural numbers less than } 10\}$

$B = \{\text{Letters of the word 'PUPPET'}\}$

$C = \{\text{Squares of first four whole numbers}\}$

$D = \{\text{Odd numbers divisible by } 2\}$

Here,

$B = \{\text{Letters of the word 'PUPPET'}\}$

$B = \{P, U, E, T\}$

Hence, $n(B) = 4$

(iii) Given

$A = \{\text{Natural numbers less than } 10\}$

$B = \{\text{Letters of the word 'PUPPET'}\}$

$C = \{\text{Squares of first four whole numbers}\}$

$D = \{\text{Odd numbers divisible by } 2\}$

Here,

$C = \{\text{Squares of first four whole numbers}\}$

$C = \{0, 1, 4, 9\}$

Hence, $n(C) = 4$

(iv) Given

$A = \{\text{Natural numbers less than } 10\}$

$B = \{\text{Letters of the word 'PUPPET'}\}$

$C = \{\text{Squares of first four whole numbers}\}$

$D = \{\text{Odd numbers divisible by } 2\}$

Here,

$D = \{\text{Odd numbers divisible by } 2\}$

$D = \{\}$

Hence, $n(D) = 0$

(v) $A \cap B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, P, U, E, T\}$ and

$n(A \cup B) = \{13\}$

3. State true or false for each of the following. Correct the wrong statement

(i) If $A = \{0\}$, then $n(A) = 0$

(ii) $n(\varnothing) = 1$

(iii) If $T = \{a, l, a, h, b, d, h\}$, then $n(T) = 5$

(iv) If $B = \{1, 5, 51, 15, 5, 1\}$, then $n(B) = 6$

Solution:

(i) Given

If $A = \{0\}$, then $n(A) = 0$

The statement given here is false

Correct statement: If $A = \{0\}$, then $n(A) = 1$

(ii) Given

$n(\varnothing) = 1$

The statement given here is false

Correct statement: $n(\varnothing) = 0$

(iii) Given

If $T = \{a, l, a, h, b, d, h\}$, then $n(T) = 5$

$T = \{a, l, h, b, d\}$

i.e. $n(T) = 5$

Hence, the given statement is true

(iv) Given

If $B = \{1, 5, 51, 15, 5, 1\}$, then $n(B) = 6$

The statement given here is false

$B = \{1, 5, 15, 51\}$

i.e. $n(B) = 4$

Correct statement: If $B = \{1, 5, 51, 15, 5, 1\}$, then $n(B) = 4$